COMP S265F

Assignment 1

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Question 1 (15 morks)

(a)
$$(265,380) \rightarrow (265,115) \rightarrow (150,115) \rightarrow (35,115)$$

 $\rightarrow (35,80) \rightarrow (35,45) \rightarrow (35,10)$
 $\rightarrow (25,10) \rightarrow (15,10) \rightarrow (5,10)$
 $\rightarrow (5,5) \rightarrow 9.c.d=5$

(b)
$$(265,380) \rightarrow (265,115) \rightarrow (115,35) \rightarrow (35,10)$$

 $\rightarrow (10,5) \Rightarrow 9.c.d = 5$

Question 2 (35 morks)

on 2 (35 mers)

(a) line 3 takes average
$$\frac{0+l+2+m+n-l}{n} = \lfloor \frac{n-l}{2} \rfloor$$
 additions. — $O(n)$ time line 4 takes $O(1)$ time to store the sum to Y[i][j] — $O(1)$ time so the for-loop in line 1 and line 2 takes $O(n+l+2+m+n-l) \cdot O(n+l)$ line 1 and line 2 $O(n+l) = O(n+l) \cdot O(n+l)$ line 3 and line 4.

Therefore, the time complexity of function is $O(n^3)$

- (b) The bottleneck is that there are a lot of repeated Calculations. For example: the value of adding all the entries $X[\frac{1}{Z}]$ to X[n-1] We do this addition for about $\frac{1}{Z}$ times, we can reuse the sum we already put into Y.
- (C) Please check 92.Py function func1()

Question 2 (cont'd)

(d) the pseudo-code of 92.py func1():

```
from line 3 to line 6:
1. for i < 0 to n-1 do
                                                takes 0(1) time
       for jet to not do
                                              so the for-loop in line 1 and lin2:
          计力约0
                                                takes (0+1+2+ = + H-1) . O(1)
            then Ycillj1 = Xcol
                                                   = \frac{n(n-1)}{2} \cdot O(1) = O(n^2) \text{ time}
         end if
          else Yrizrj1 = Yrizrj-1] + Xrj1
                                            Therefore, the time complexity of func1() is O(n^2)
        end for
7.
8, end for
```

Question 3 (25 marks)

- left complete binary tree: O right complete bimosy tree: |
- Please check 93.py. function: traversel()
- (C) In function traverse1(). I used a property of the local minimum number: - We must have at least one local minimum number in every possible toute from the top of the tree to bottom.

So we just need to search one route to find one of the local minimum number.

In the worst case, I traverse from top to bottom, and the local minimum is on the leaf. I called traverses (node left) recursively till I hit the leaf. Then we have:

In the worst case:

$$T(n) = T(\frac{n}{Z}) + O(1)$$
Since $n^{\log_2 n} = n^{\log_2 1} = 1$, we can apply case 2 of the master thereom.

We can conclude that the time complexity of our function is $O(n^{\circ} \log n) = O(\log n)$.

Question 4 (25 marks)

(a) please theck 94. py.

(b) The algorithm in (a) is a greedy algorithm.

— Every step we try to find the largest value of coin to minimize the total amount of coins.

Because of that, we can make sure our final output; is the minimal list of coins in descending order.

In each amount of coins, first we caculate the number of it by using "/1" then we substract the total value of this amount coins to make sure the When value // 1" is zero, which means the final coin value equals \$ police. final coin value equals \$value.