HomeWork 6

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1 Modular Exponentiation

1. Compute the binary expansion of 2019

ANSWER:

011111100011

2. Compute the $13^{2019} \pmod{37}$

WORK:

0111111100011

$$2^{0} + 2^{1} + 2^{6} + 2^{7} + 2^{8} + 2^{9} + 2^{10} + 2^{11}$$

$$1 + 2 + 64 + 128 + 256 + 512 + 1024 + 2048$$

 $13^{(1+2+64+128+256+512+1024+2048)} \mod 37$

$$13^1*13^2*13^{64}*13^{128}*13^{256}*13^{512}*13^{1024}*13^{2048} \ \mathrm{mod} \ 37$$

 $(13^1 \mod 37 * 13^2 \mod 37 * 13^{64} \mod 37 * 13^{128} \mod 37 * 13^{256} \mod 37 * 13^{512} \mod 37 * 13^{1024} \mod 37 * 13^{2048} \mod 37) \mod 37$

$$13^{2019} \mod 37 = (13 * 21 * 33 * 16 * 34 * 9 * 7 * 12) \mod 37$$

ANSWER:

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2 Greatest Common Divisor

1. gcd(288, 126)

WORK:

$$\frac{288}{126} = 2 \text{ R } 36$$

$$\frac{126}{36} = 3 \text{ R } 18$$

$$\frac{36}{18} = 2 R 0$$

ANSWER:

18

 $2. \gcd(899,703)$

WORK:

$$\frac{899}{703} = 1 \text{ R } 196$$

$$\frac{703}{196} = 3 \text{ R } 115$$

$$\frac{196}{115} = 1 \text{ R } 81$$

$$\frac{115}{81} = 1 \text{ R } 34$$

$$\frac{81}{34} = 2 \text{ R } 13$$

$$\frac{34}{13} = 2 \text{ R } 8$$

$$\frac{13}{8} = 1 \text{ R } 5$$

$$\frac{8}{5} = 1 \text{ R } 3$$

$$\frac{5}{3} = 1 \text{ R } 2$$

$$\frac{3}{2} = 1 \text{ R } 1$$

$$\tfrac{2}{1}=2~\mathrm{R}~0$$

ANSWER:

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