

# ReQFlow: Rectified Quaternion Flow for Efficient and High-Quality Protein Backbone Generation



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## Background & Contributions

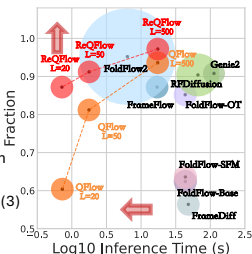
**Task:** Protein backbone generation

**Previous works:**

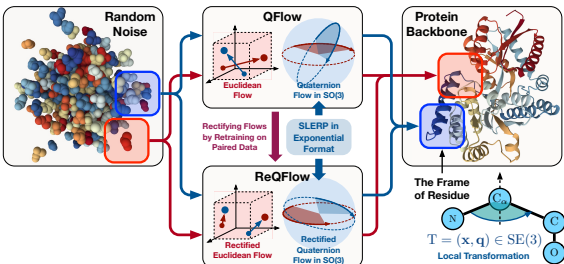
- Low generation designability
- Long inference time

**Highlight of our method:**

- Use unit **quaternions** to represent rotations
- Construct SO(3) flow with **SLERP** in an exponential format (**QFlow**)
- **First paper** explores **ReFlow** in SO(3) to accelerate inference (**ReQFlow**)
- **SOTA** on designability, **37× faster** than RFDiffusion and **62× faster** than Genie2 when best tradeoff



## Our Method

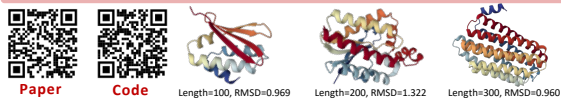


$$\text{Train: } q = \exp\left(\frac{1}{2}\omega\right) = \left[\cos\frac{\phi}{2}, \sin\frac{\phi}{2}u^\top\right]^\top \in \mathbb{S}^3 \Rightarrow \omega_{\theta,t} = \frac{2\log(q_t^{-1} \otimes q_{\theta,1})}{1-t}$$

$$q_t = q_0 \otimes \exp(t\log(q_0^{-1} \otimes q_1)) \Rightarrow \mathcal{L}_{\text{SO}(3)} = \mathbb{E}_{t, Q_0, Q_1} [\|\omega - \omega_{\theta,t}\|^2]$$

$$\text{Inference: } q_{t+\Delta t} = q_t \otimes \exp\left(\frac{1}{2}\Delta t \cdot \gamma e^{-\gamma t} \omega_{\theta,t}\right) \Rightarrow \text{ReFlow}$$

## Experiment



| Method                   | Efficiency |         | Designability |                    | Diversity Novelty |              |
|--------------------------|------------|---------|---------------|--------------------|-------------------|--------------|
|                          | Step       | Time(s) | Fraction↑     | scRMSD↓            | TM↓               | TM↓          |
| RFDiffusion              | 50         | 66.23   | 0.904         | 1.102±1.617        | 0.382             | 0.527        |
| Genie2                   | 1000       | 112.93  | 0.908         | 1.132±1.389        | 0.370             | <b>0.475</b> |
|                          | 500        | 55.86   | 0.000         | 18.169±5.963       | -                 | -            |
| FrameDiff                | 500        | 48.12   | 0.564         | 2.936±3.093        | 0.441             | 0.591        |
| FoldFlow <sub>Base</sub> | 500        | 43.52   | 0.624         | 3.080±3.449        | 0.469             | 0.645        |
| FoldFlow <sub>SFM</sub>  | 500        | 43.63   | 0.636         | 3.031±3.589        | 0.411             | 0.604        |
| FoldFlow <sub>OT</sub>   | 500        | 43.35   | 0.852         | 1.760±2.593        | 0.434             | 0.617        |
| FoldFlow2                | 50         | 6.35    | 0.952         | 1.083±1.308        | 0.373             | 0.527        |
|                          | 20         | 2.63    | 0.644         | 3.060±3.210        | 0.339             | 0.492        |
| FrameFlow                | 500        | 17.05   | 0.872         | 1.380±1.392        | 0.346             | 0.562        |
|                          | 200        | 6.77    | 0.864         | 1.542±1.889        | 0.348             | 0.564        |
|                          | 100        | 3.46    | 0.708         | 2.167±2.373        | 0.332             | 0.560        |
|                          | 50         | 1.73    | 0.704         | 2.639±3.079        | 0.334             | 0.536        |
|                          | 20         | 0.71    | 0.436         | 4.652±4.390        | 0.319             | 0.501        |
|                          | 10         | 0.37    | 0.180         | 7.343±5.125        | 0.317             | 0.482        |
| QFlow                    | 500        | 17.37   | 0.936         | 1.163±0.938        | 0.356             | 0.635        |
|                          | 200        | 7.10    | 0.864         | 1.400±1.259        | <b>0.344</b>      | 0.620        |
|                          | 100        | 3.48    | 0.916         | 1.342±1.364        | 0.348             | 0.614        |
|                          | 50         | 1.77    | 0.812         | 1.785±2.151        | <b>0.344</b>      | 0.571        |
|                          | 20         | 0.73    | 0.604         | 3.090±3.374        | 0.325             | 0.537        |
|                          | 10         | 0.38    | 0.332         | 5.032±4.303        | 0.313             | 0.528        |
| ReQFlow                  | 500        | 17.42   | <b>0.972</b>  | <b>1.071±0.482</b> | 0.377             | 0.645        |
|                          | 200        | 6.94    | 0.932         | 1.160±0.782        | 0.384             | 0.648        |
|                          | 100        | 3.58    | 0.928         | 1.245±1.059        | 0.369             | 0.629        |
|                          | 50         | 1.78    | 0.912         | 1.254±0.915        | 0.369             | 0.608        |
|                          | 20         | 0.72    | 0.872         | 1.418±0.998        | 0.355             | 0.581        |
|                          | 10         | 0.38    | 0.676         | 2.443±2.382        | 0.337             | 0.540        |

