

# STRING

Algorithm Problem Solving – Samsung Vietnam R&D Center

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# Agenda

- ASCII
- Unicode
- String in C/C++
- String in Java
- Naive algorithm for Pattern Searching
- KMP (Knuth Morris Pratt) Pattern Searching
- Boyer Moore Bad Character Heuristic
- Boyer Moore Good Suffix heuristic
- Boyer Moore Strong Good Suffix heuristic



# **Characters Before ASCII/Unicode**

Fundamentally, computers just deal with numbers. They store letters and other characters by assigning a number for each one. Before Unicode was invented, there were hundreds of different systems, called character encodings, for assigning these numbers.

These early character encodings were limited and could not contain enough characters to cover all the world's languages. Even for a single language like English no single encoding was adequate for all the letters, punctuation, and technical symbols in common use.

Early character encodings also conflicted with one another. That is, two encodings could use the same number for two different characters, or use different numbers for the same character. Any given computer (especially servers) would need to support many different encodings.

However, when data is passed through different computers or between different encodings, that data runs the risk of corruption.



# **Brief History of ASCII code**

The American Standard Code for Information Interchange, or ASCII code, was created in 1963 by the "American Standards Association" Committee or "ASA", the agency changed its name in 1969 by "American National Standards Institute" or "ANSI" as it is known since.

This code arises from reorder and expand the set of symbols and characters already used in telegraphy at that time by the Bell company.

At first only included capital letters and numbers, but in 1967 was added the lowercase letters and some control characters, forming what is known as US-ASCII (**Standard ASCII**), ie the characters 0 through 127.

So with this set of only 128 characters was published in 1967 as standard, containing all you need to write in English language.

**Standard ASCII** can represent 128 characters. It uses 7 bits to represent each character since the first bit of the byte is always 0. For instance, a capital "T" is represented by 84, or 01010100 in binary. A lowercase "t" is represented by 116 or 01110100 in binary.

Dec Hx Oct Char	Dec Hx Oct Html Chr	Dec Hx Oct Html Chr	Dec Hx Oct Html Chr
0 0 000 NUL (null)	32 20 040 @#32; Space	64 40 100 <b>@</b> #64; 0	96 60 140 @#96;
l 1 001 SOH (start of heading)	33 21 041 @#33; !	65 41 101 @#65; A	97 61 141 @#97; 👊
2 2 002 STX (start of text)	34 22 042 " "	66 42 102 B B	98 62 142 b b
3 3 003 ETX (end of text)	35 23 043 # #	67 43 103 «#67; C	99 63 143 c C
4 4 004 EOT (end of transmission)	36 24 044 \$ \$	68 44 104 D D	100 64 144 d d
5 5 005 <b>ENQ</b> (enquiry)	37 25 045 % %	69 45 105 E <b>E</b>	101 65 145 e e
6 6 006 <mark>ACK</mark> (acknowledge)	38 26 046 & &	70 46 106 F <b>F</b>	102 66 146 f <b>f</b>
7 7 007 BEL (bell)	39 27 047 ' '	71 47 107 @#71; G	103 67 147 g g
8 8 010 <mark>BS</mark> (backspace)	40 28 050 ( (	72 48 110 @#72; H	104 68 150 h h
9 9 011 TAB (horizontal tab)	41 29 051 4#41; )	73 49 111 I <mark>I</mark>	105 69 151 i i
10 A 012 LF (NL line feed, new line)	42 2A 052 * *	74 4A 112 @#74; J	106 6A 152 j j
ll B 013 VT (vertical tab)	43 2B 053 + +	75 4B 113 6#75; K	107 6B 153 k k
12 C 014 FF (NP form feed, new page)	44 2C 054 , ,	76 4C 114 L L	108 6C 154 l 1
13 D 015 CR (carriage return)	45 2D 055 - -	77 4D 115 6#77; M	109 6D 155 m m
14 E 016 <mark>SO</mark> (shift out)	46 2E 056 . .	78 4E 116 N N	110 6E 156 n n
15 F 017 SI (shift in)	47 2F 057 / /	79 4F 117 O 0	111 6F 157 o 0
16 10 020 DLE (data link escape)	48 30 060 0 0	80 50 120 P <b>P</b>	112 70 160 p p
17 11 021 DC1 (device control 1)	49 31 061 6#49; 1	81 51 121 Q <b>Q</b>	113 71 161 q q
18 12 022 DC2 (device control 2)	50 32 062 2 2	82 52 122 R R	114 72 162 r r
19 13 023 DC3 (device control 3)	51 33 063 3 3	83 53 123 S <mark>\$</mark>	115 73 163 s 3
20 14 024 DC4 (device control 4)	52 34 064 4 4	84 54 124 T T	116 74 164 t t
21 15 025 NAK (negative acknowledge)	53 35 065 4#53; 5	85 55 125 U U	117 75 165 u u
22 16 026 SYN (synchronous idle)	54 36 066 6 6	86 56 126 V V	118 76 166 v ♥
23 17 027 ETB (end of trans. block)	55 37 067 7 <b>7</b>	87 57 127 <b>6#87; ₩</b>	119 77 167 w ₩
24 18 030 CAN (cancel)	56 38 070 <b>6#56;</b> 8	88 58 130 X X	120 78 170 x ×
25 19 031 EM (end of medium)	57 39 071 9 <mark>9</mark>	89 59 131 Y <b>Y</b>	121 79 171 y Y
26 1A 032 <mark>SUB</mark> (substitute)	58 3A 072 6#58;:	90 5A 132 @#90; Z	122 7A 172 z Z
27 1B 033 ESC (escape)	59 3B 073 ;;	91 5B 133 [ [	123 7B 173 { {
28 1C 034 FS (file separator)	60 3C 074 < <	92 5C 134 @#92; \	124 7C 174
29 1D 035 GS (group separator)	61 3D 075 = =	93 5D 135 ] ]	125 7D 175 } }
30 1E 036 RS (record separator)	62 3E 076 >>		126 7E 176 ~ ~
31 1F 037 <mark>US</mark> (unit separator)	63 3F 077 ? ?	95 5F 137 _ _	127 7F 177  DEL
	•		· <del>-</del>

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# **Brief History of ASCII code**

In 1981, IBM developed an extension of 8-bit ASCII code, called "code page 437", in this version were replaced some obsolete control characters for graphic characters. Also 128 characters were added, with new symbols, signs, graphics and latin letters, all punctuation signs and characters needed to write texts in other languages, such as Spanish.

In this way was added the ASCII characters ranging from 128 to 255. (Extended ASCII)

The 128 (2^7) characters supported by **Standard ASCII** are enough to represent all standard English letters, numbers, and punctuation symbols.

However, it is not sufficient to represent all special characters and characters from other languages.

**Extended ASCII** helps solve this problem by adding an extra 128 values, for a total of 256 (2^8) characters. The additional binary values start with a 1 instead of a 0.

For example, in extended ASCII, the character "é" is represented by 233, or 11101001 in binary.

**Extended ASCII** is programmable; characters are based on the language of your operating system or program you are using. Foreign letters are also placed in this section.

128	Ç	144	É	160	á	176		192	L	208	Т	224	α	240	≡
129	ü	145	æ	161	í	177	*****	193	$\perp$	209	₸	225	В	241	±
130	é	146	Æ	162	ó	178		194	т	210	π	226	Γ	242	≥
131	â	147	ô	163	ú	179	-1	195	H	211	Ш	227	π	243	≤
132	ä	148	ö	164	ñ	180	4	196	- (	212	F	228	Σ	244	- (
133	à	149	ò	165	Ñ	181	╡	197	+	213	F	229	σ	245	J
134	å	150	û	166	•	182	1	198	F	214	П	230	μ	246	÷
135	ç	151	ù	167	۰	183	П	199	╟	215	#	231	τ	247	æ
136	ê	152	ÿ	168	ż	184	4	200	L	216	+	232	Φ	248	۰
137	ë	153	Ö	169	Ė	185	4	201	F	217	7	233	Θ	249	
138	è	154	Ü	170	4	186		202	쁘	218	Г	234	Ω	250	
139	ï	155	¢	171	1/2	187	a	203	īF	219		235	δ	251	A
140	î	156	£	172	1/4	188	ᆁ	204	ŀ	220		236	00	252	n
141	ì	157	¥	173	i	189	Ш	205	=	221		237	φ	253	2
142	Ä	158	R	174	«	190	4	206	#	222		238	ε	254	
143	Å	159	f	175	»	191	٦	207	<u></u>	223		239	$\Diamond$	255	

Source: www.LookupTables.com

### What is Unicode?

In computer systems, characters are transformed and stored as numbers (sequences of bits) that can be handled by the processor. A code page is an encoding scheme that maps a specific sequence of bits to its character representation. The pre-Unicode world was populated with hundreds of different encoding schemes that assigned a number to each letter or character. Many such schemes included code pages that contained only 256 characters - each character requiring 8 bits of storage.

While this was relatively compact, it was insufficient to hold ideographic character sets containing thousands of characters such as Vietnamese and Japanese, and also did not allow the character sets of many languages to co-exist with each other.

Unicode is an attempt to include all the different schemes into one universal text-encoding standard.



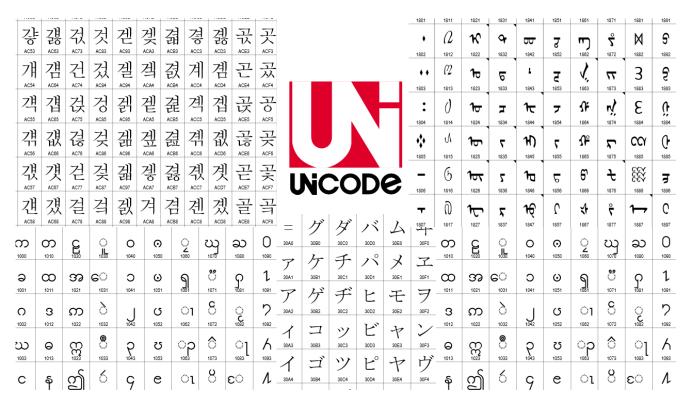
A Brief Introduction to Unicode for Everybody

### The importance of Unicode

Unicode represents a mechanism to support more regionally popular encoding systems

From a translation/localization point of view, Unicode is an important step towards standardization, at least from a tools and file format standpoint.

- Unicode enables a single software product or a single website to be designed for multiple platforms, languages and countries (no need for re-engineering) which can lead to a significant reduction in cost over the use of legacy character sets.
- Unicode data can be used through many different systems without data corruption.
- Unicode represents a single encoding scheme for all languages and characters.
- Unicode is a common point in the conversion between other character encoding schemes. Since it is a superset of all of the other common character encoding systems, you can convert from one encoding scheme to Unicode, and then from Unicode to the other encoding scheme.
- Unicode is the preferred encoding scheme used by XMLbased tools and applications.



**Bottom line**: Unicode is a worldwide character-encoding standard, published by the Unicode Consortium. Computers store numbers that represent a character; Unicode provides a unique number for every character.



# String in C

Strings are defined as an array of characters. The difference between a character array and a string is the string is terminated with a special character '\0'.

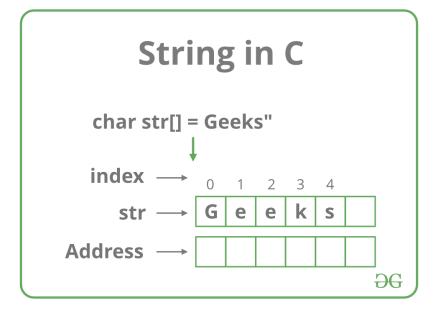
**Declaration of strings:** Declaring a string is as simple as declaring a one dimensional array. Below is the basic syntax for declaring a string.

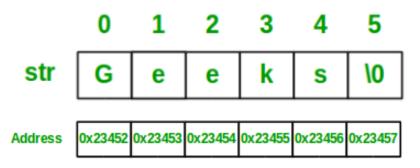
#### char str\_name[size];

Please keep in mind that there is an extra terminating character which is the **Null** character ('\**0**') used to indicate termination of string which differs strings from normal character arrays.

**Initializing a String:** A string can be initialized in different ways. We will explain this with the help of an example. Below is an example to declare a string with name as str and initialize it with "GeeksforGeeks".

```
    char str[] = "GeeksforGeeks";
    char str[50] = "GeeksforGeeks";
    char str[] = {'G', 'e', 'e', 'k', 's', 'f', 'o', 'r', 'G', 'e', 'e', 'k', 's', '\0'};
    char str[14] = {'G', 'e', 'e', 'k', 's', 'f', 'o', 'r', 'G', 'e', 'e', 'k', 's', '\0'};
```





# Reading String & Passing to function

Below is a sample program to read a string from user:

**Passing strings to function:** As strings are character arrays, so we can pass strings to function in a same way we pass an array to a function. Below is a sample program to do this:

```
// C program to read strings

#include<stdio.h>

int main()
{
    // declaring string
    char str[50];

    // reading string
    scanf("%s",str);

    // print string
    printf("%s",str);

    return 0;
}
```

```
// C program to illustrate how to
     // pass string to functions
     #include<stdio.h>
     void printStr(char str[])
         printf("String is : %s",str);
     int main()
         // declare and initialize string
         char str[] = "GeeksforGeeks";
         // print string by passing string
         // to a different function
         printStr(str);
         return 0;
Output:
 String is: GeeksforGeeks
```

### Read a Word

Notice that, in the second example only "Programming" is displayed instead of "Programming is fun".

This is because the extraction operator >> works as **scanf()** in C and considers a space " " has a terminating character.

#### Example 1: C++ String to read a word

C++ program to display a string entered by user.

```
#include <iostream>
using namespace std;

int main()
{
    char str[100];

    cout << "Enter a string: ";
    cin >> str;
    cout << "You entered: " << str << endl;

    cout << "\nEnter another string: ";
    cin >> str;
    cout << "You entered: "<<str<<endl;

    return 0;
}</pre>
```

#### Output

```
Enter a string: C++
You entered: C++
Enter another string: Programming is fun.
You entered: Programming
```

### Read a Line of Text

To read the text containing blank space, **cin.get** function can be used. This function takes two arguments.

First argument is the **name of the string** (address of first element of string) and second argument is the **maximum size of the array**.

In the above program, str is the name of the string and 100 is the maximum size of the array.

#### Example 2: C++ String to read a line of text

C++ program to read and display an entire line entered by user.

```
#include <iostream>
using namespace std;

int main()
{
    char str[100];
    cout << "Enter a string: ";
    cin.get(str, 100);

    cout << "You entered: " << str << endl;
    return 0;
}</pre>
```

#### Output

```
Enter a string: Programming is fun.
You entered: Programming is fun.
```

# Functions for manipulating C strings



No	Function & Purpose
1	strcpy(s1, s2); Copies string s2 into string s1.
2	strcat(s1, s2); Concatenates string s2 onto the end of string s1.
3	strlen(s1); Returns the length of string s1.
4	strcmp(s1, s2); Returns 0 if s1 and s2 are the same; less than 0 if s1 <s2; greater than 0 if s1&gt;s2.</s2; 
5	strchr(s1, ch); Returns a pointer to the first occurrence of character ch in string s1.
6	strstr(s1, s2); Returns a pointer to the first occurrence of string s2 in string s1.

```
strcpy( str3, str1) : Hello
strcat( str1, str2): HelloWorld
strlen(str1) : 10
```

```
#include <iostream>
#include <cstring>
using namespace std;
int main () {
char str1[10] = "Hello";
char str2[10] = "World";
char str3[10];
int len ;
// copy str1 into str3
strcpy(str3, str1);
cout << "strcpy( str3, str1) : " << str3 << endl;</pre>
// concatenates str1 and str2
strcat( str1, str2); cout << "strcat( str1, str2): "</pre>
<< str1 << endl;
// total lenghth of str1 after concatenation
len = strlen(strl);
cout << "strlen(str1) : " << len << endl;</pre>
return 0;
```

# **String Class in C++**

C++ provides following two types of string representations –

- The C-style character string.
- The string class type introduced with Standard C++.

C++ has in its definition a way to represent sequence of characters as an object of class. This class is called std:: string. String class stores the characters as a sequence of bytes with a functionality of allowing access to single byte character.

```
str3: Hello
str1 + str2: HelloWorld
str3.size(): 10
```

```
#include <iostream>
#include <string>
using namespace std;
int main () {
   string str1 = "Hello";
   string str2 = "World";
   string str3;
   int len;
   // copy str1 into str3
   str3 = str1;
   cout << "str3 : " << str3 << endl;</pre>
   // concatenates str1 and str2
   str3 = str1 + str2;
   cout << "str1 + str2 : " << str3 << endl;</pre>
   // total length of str3 after concatenation
   len = str3.size();
   cout << "str3.size() : " << len << endl;</pre>
   return 0;
```

# Character Array vs std:: string

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A character array is simply **an array of characters** can terminated by a null character. A string is a **class which defines objects** that be represented as stream of characters.

Size of the character array has to **allocated statically**, more memory cannot be allocated at run time if required. Unused allocated **memory is wasted** in case of character array. In case of strings, memory is **allocated dynamically**. More memory can be allocated at run time on demand. As no memory is preallocated, **no memory is wasted**.

Implementation of **character array is faster** than std:: string. **Strings are slower** when compared to implementation than character array.

Character array **do not offer** much **inbuilt functions** to manipulate strings. String class defines **a number of functionalities** which allow manifold operations on strings.

# **Input String Data Type**



In this program, a **string str** is declared. Then the string is asked from the user.

Instead of using cin>> or cin.get() function, you can get the entered line of text using getline().

**getline()** function takes the input stream as the first parameter which is **cin** and **str** as the location of the line to be stored.

#### Example 3: C++ string using string data type

```
#include <iostream>
using namespace std;

int main()
{
    // Declaring a string object
    string str;
    cout << "Enter a string: ";
    getline(cin, str);

    cout << "You entered: " << str << endl;
    return 0;
}</pre>
```

#### Output

```
Enter a string: Programming is fun.
You entered: Programming is fun.
```



# **String in Java**

In Java, strings are special. For example, to create the **string** objects you **need not to use 'new'** keyword. Where as to create **other type of objects** you **have to use 'new'** keyword.

JVM divides the allocated memory to a Java program into two parts. one is **Stack** and another one is **heap**. Stack is used for **execution purpose** and heap is used for **storage purpose**.

In that heap memory, JVM allocates some memory specially meant for string literals. This part of the heap memory is called **String Constant Pool**.

Whenever you create a string object **using string literal**, that object is stored in the **string constant pool** and whenever you create a string object using **new** keyword, such object is stored in the **heap memory**.

#### String Constant Pool.

```
String s1 = "abc";

String s2 = "xyz";

String s3 = "123";

String s4 = "A";
```

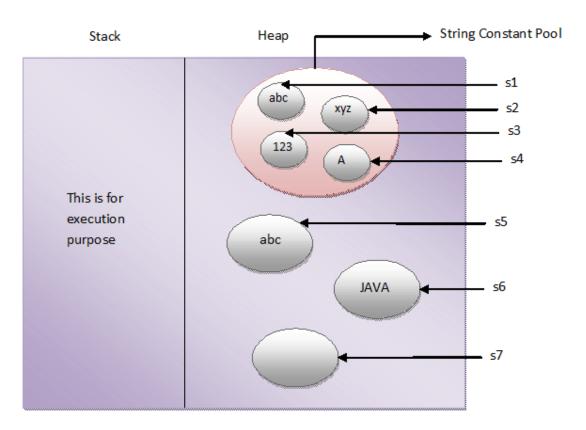
#### Heap memory.

```
String s5 = new String("abc");

char[] c = {'J', 'A', 'V', 'A'};

String s6 = new String(c);

String s7 = new String(new StringBuffer());
```



# **String in Java**

Pool space is allocated to an object depending upon it's content. There will be **no two objects** in the pool having the **same content**.

This is what happens when you create string objects using string literal,

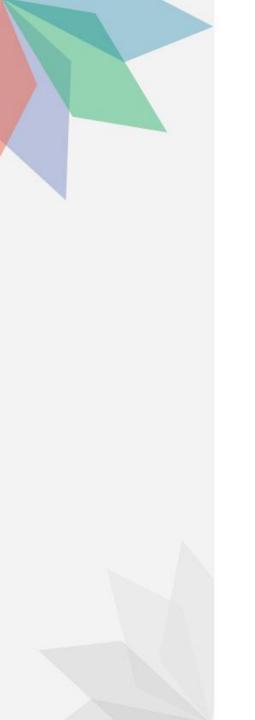
"When you create a string object using string literal, JVM first checks the content of to be created object. If there exist an object in the pool with the same content, then it returns the reference of that object. It doesn't create new object. If the content is different from the existing objects then only it creates new object."

When you create string objects using new keyword, a new object is created **whether the content is same or not**.

This can be proved by using "==" operator. As "==" operator returns true if two objects have **same physical address** in the memory otherwise it will return false.

In simple words, there can not be two string objects with same content in the string constant pool. But, there can be two string objects with the same content in the heap memory.

```
public class StringExamples
         public static void main(String[] args)
             //Creating string objects using literals
             String s1 = "abc";
             String s2 = "abc";
10
             System.out.println(s1 == s2);
                                                  //Output : true
12
             //Creating string objects using new operator
14
15
             String s3 = new String("abc");
16
17
             String s4 = new String("abc");
18
19
             System.out.println(s3 == s4);
                                                  //Output : false
20
```



# SEARCH

### **Problem**

Given a text txt[0..n-1] and a pattern pat[0..m-1], write a function search(char pat[], char txt[]) that prints all occurrences of pat[] in txt[]. You may assume that n > m.

Input: txt[] = "THIS IS A TEST TEXT"

pat[] = "TEST"

Output: Pattern found at index 10

Input: txt[] = "AABAACAADAABAABA"

pat[] = "AABA"

Output: Pattern found at index 0

Pattern found at index 9
Pattern found at index 12

Text: A A B A A C A A D A A B A A B A

Pattern: A A B A

A A B A A C A A D A A B A A B A

O 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

A A B A

Pattern Found at 0, 9 and 12

Pattern searching is an important problem in computer science. When we do search for a string in notepad/word file or browser or database, pattern searching algorithms are used to show the search results.

# Naive algorithm for Pattern Searching

Slide the pattern over text one by one and check for a match. If a match is found, then slides by 1 again to check for subsequent matches.

```
// C++ program for Naive Pattern
// Searching algorithm
#include <bits/stdc++.h>
using namespace std;
void search(char* pat, char* txt)
    int M = strlen(pat);
    int N = strlen(txt);
    /* A loop to slide pat[] one by one */
    for (int i = 0; i <= N - M; i++) {
        int j;
        /* For current index i, check for pattern match */
        for (j = 0; j < M; j++)
            if (txt[i + j] != pat[j])
                break:
        if (j == M) // if pat[0...M-1] = txt[i, i+1, ...i+M-1]
            cout << "Pattern found at index
                 << i << endl;
// Driver Code
int main()
    char txt[] = "AABAACAADAABAAABAA";
    char pat[] = "AABA";
    search(pat, txt);
    return 0;
// This code is contributed
// by Akanksha Rai
```

```
// Java program for Naive Pattern Searching
public class NaiveSearch {
   public static void search(String txt, String pat)
       int M = pat.length();
       int N = txt.length();
       /* A loop to slide pat one by one */
       for (int i = 0; i <= N - M; i++) {
           int j;
           /* For current index i, check for pattern
             match */
           for (j = 0; j < M; j++)
               if (txt.charAt(i + j) != pat.charAt(j))
                   break;
           if (j == M) // if pat[0...M-1] = txt[i, i+1, ...i+M-1]
               System.out.println("Pattern found at index " + i);
                                                           Output:
   public static void main(String[] args)
                                                            Pattern found at index 0
       String txt = "AABAACAADAABAAABAA";
       String pat = "AABA";
                                                            Pattern found at index 9
       search(txt, pat);
                                                            Pattern found at index 13
// This code is contributed by Harikishore
```

The Naive pattern searching algorithm doesn't work well in cases where we see many matching characters followed by a mismatching character. Following are some examples.

```
txt[] = "AAAAAAAAAAAAAAAB"
pat[] = "ABABABCABABABCBC"
pat[] = "ABABAC" (not a worst case, but a bad case for Naive)
```

The basic idea behind KMP's algorithm is: whenever we detect a mismatch (after some matches), we already know some of the characters in the text of the next window. We take advantage of this information to avoid matching the characters that we know will anyway match. Let us consider below example to understand this.

#### Matching Overview

txt = "AAAAABAAABA"

pat = "AAAA"

We compare first window of txt with pat

txt = "AAAAABAAABA"

pat = "AAAA" [Initial position]

We find a match. This is same as Naive String Matching.

In the next step, we compare next window of txt with pat.

txt = "AAAAABAABA"

pat = "AAAA" [Pattern shifted one position]

This is where KMP does optimization over Naive. In this second window, we only compare fourth A of pattern with fourth character of current window of text to decide whether current window matches or not. Since we know first three characters will anyway match, we skipped matching first three characters.

#### Need of Preprocessing?

An important question arises from the above explanation, how to know how many characters to be skipped. To know this, we pre-process pattern and prepare an integer array lps[] that tells us the count of characters to be skipped.

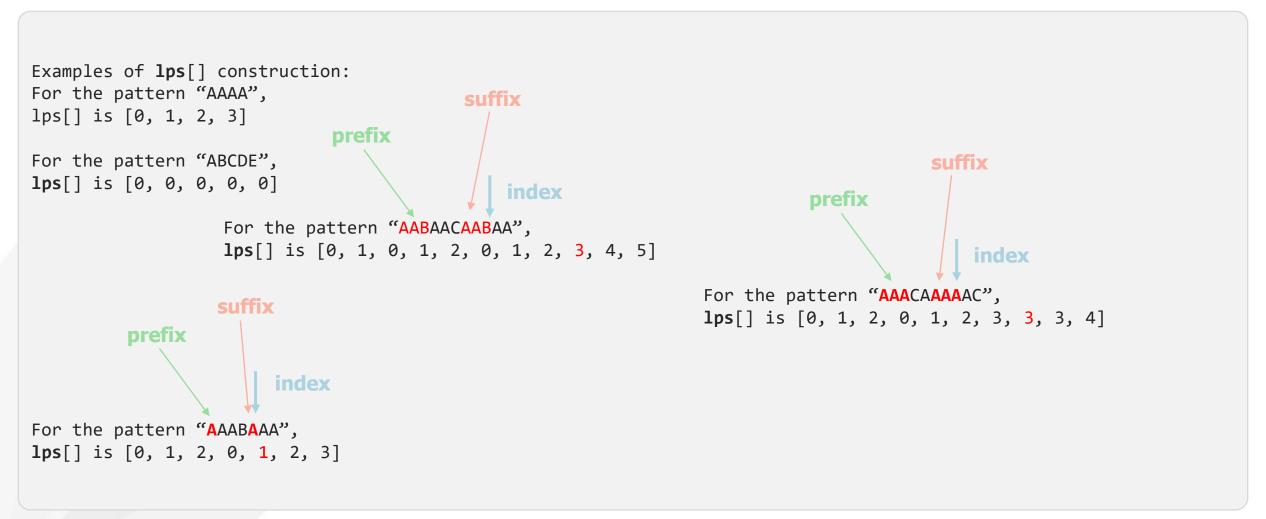


#### **Preprocessing Overview:**

- KMP algorithm preprocesses pat[] and constructs an auxiliary lps[] of size m (same as size of pattern) which is used to skip characters while matching.
- name lps indicates longest proper prefix which is also suffix.. A proper prefix is prefix with whole string not allowed. For example, prefixes of "ABC" are "", "A", "AB" and "ABC". Proper prefixes are "", "A" and "AB". Suffixes of the string are "", "C", "BC" and "ABC".
- We search for lps in sub-patterns. More clearly we focus on sub-strings of patterns that are either prefix and suffix.
- For each sub-pattern **pat**[0..i] where i = 0 to m-1, **lps**[i] stores length of the maximum matching proper prefix which is also a suffix of the sub-pattern **pat**[0..i].

**Note: Ips**[i] could also be defined as **longest prefix** which is also **proper suffix**. We need to use properly at one place to make sure that the whole substring is not considered.

### **Preprocessing Overview:**



#### **Searching Algorithm:**

Unlike Naive algorithm, where we slide the pattern by one and compare all characters at each shift, we use a value from lps[] to decide the next characters to be matched. The idea is to not match a character that we know will anyway match.

How to use **lps**[] to decide next positions (or to know a number of characters to be skipped)?

- We start comparison of pat[j] with j = 0 with characters of current window of text.
- We keep matching characters txt[i] and pat[j] and keep incrementing i and j while pat[j] and txt[i] keep matching.
- When we see a mismatch
  - We know that characters **pat**[0..j-1] match with **txt**[i-j...i-1] (Note that j starts with 0 and increment it only when there is a match).
  - We also know (from above definition) that **lps**[j-1] is count of characters of **pat**[0...j-1] that are both proper prefix and suffix.
  - From above two points, we can conclude that we do not need to match these **lps**[j-1] characters with **txt**[i-j...i-1] because we know that these characters will anyway match.

```
txt[] = "AAAAABAAABA"
pat[] = "AAAA"
lps[] = {0, 1, 2, 3}
i = 0, j = 0
txt[] = "AAAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] match, do i++, j++
i = 1, j = 1
txt[] = "AAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] match, do i++, j++
i = 2, j = 2
txt[] = "AAAAABAAABA"
pat[] = "AAAA"
pat[i] and pat[j] match, do i++, j++
i = 3, j = 3
txt[] = "AAAAABAABA"
pat[] = "AAAA"
txt[i] and pat[j] match, do i++, j++
```

```
i = 4, j = 4
Since j == M, print pattern found and reset j,
i = lps[i-1] = lps[3] = 3
Here unlike Naive algorithm, we do not match first three characters of this window. Value of lps[j-1] (in above
step) gave us index of next character to match.
i = 4, j = 3
txt[] = "AAAAABAABA"
pat[] = "AAAA"
txt[i] and pat[j] match, do i++, j++
i = 5, i = 4
Since j == M, print pattern found and reset j,
j = lps[j-1] = lps[3] = 3
Again unlike Naive algorithm, we do not match first three characters of this window. Value of lps[j-1] (in above
step) gave us index of next character to match.
i = 5, j = 3
txt[] = "AAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] do NOT match and j > 0, change only j
j = lps[j-1] = lps[2] = 2
```

```
i = 5, j = 2
txt[] = "AAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] do NOT match and j > 0, change only j
i = lps[i-1] = lps[1] = 1
i = 5, j = 1
txt[] = "AAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] do NOT match and j > 0, change only j
j = lps[j-1] = lps[0] = 0
i = 5, j = 0
txt[] = "AAAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] do NOT match and j is 0, we do i++.
```

```
i = 6, j = 0
txt[] = "AAAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] match, do i++ and j++

i = 7, j = 1
txt[] = "AAAAABAAABA"
pat[] = "AAAA"
txt[i] and pat[j] match, do i++ and j++
We continue this way...
```

#### **Preprocessing Algorithm:**

In the preprocessing part, we calculate values in <code>lps[]</code>. To do that, we keep track of the length of the longest prefix suffix value (we use <code>len</code> variable for this purpose) for the previous index. We initialize <code>lps[0]</code> and <code>len</code> as 0. If <code>pat[len]</code> and <code>pat[i]</code> match, we increment <code>len</code> by <code>1</code> and assign the incremented value to <code>lps[i]</code>. If <code>pat[i]</code> and <code>pat[len]</code> do not match and <code>len</code> is not 0, we update <code>len</code> to <code>lps[len-1]</code>. See computeLPSArray () in the below code for details.

```
pat[] = "AAACAAAA"
len = 0, i = 0.
lps[0] is always 0, we move
to i = 1
len = 0, i = 1.
Since pat[len] and pat[i] match, do len++,
store it in lps[i] and do i++.
len = 1, lps[1] = 1, i = 2
len = 1, i = 2.
Since pat[len] and pat[i] match, do len++,
store it in lps[i] and do i++.
len = 2, lps[2] = 2, i = 3
```

```
len = 2, i = 3.
Since pat[len] and pat[i] do not match, and len > 0,
set len = lps[len-1] = lps[1] = 1
len = 1, i = 3.
Since pat[len] and pat[i] do not match and len > 0,
len = lps[len-1] = lps[0] = 0
len = 0, i = 3.
Since pat[len] and pat[i] do not match and len = 0,
Set lps[3] = 0 and i = 4.
We know that characters pat
len = 0, i = 4.
Since pat[len] and pat[i] match, do len++,
store it in lps[i] and do i++.
len = 1, lps[4] = 1, i = 5
len = 1, i = 5.
Since pat[len] and pat[i] match, do len++,
store it in lps[i] and do i++.
len = 2, lps[5] = 2, i = 6
```

```
len = 2, i = 6.
Since pat[len] and pat[i] match, do len++,
store it in lps[i] and do i++.
len = 3, lps[6] = 3, i = 7
len = 3, i = 7.
Since pat[len] and pat[i] do not match and len > 0,
set len = lps[len-1] = lps[2] = 2
len = 2, i = 7.
Since pat[len] and pat[i] match, do len++,
store it in lps[i] and do i++.
len = 3, lps[7] = 3, i = 8
We stop here as we have constructed the whole lps[].
```

# **Problem Solving**

Implement KMP (Knuth Morris Pratt) Pattern Searching

Problem Solving





# **Boyer Moore Algorithm**



Boyer Moore is a combination of following two approaches.

- 1) Bad Character Heuristic
- 2) Good Suffix Heuristic

Both of the above heuristics can also be used independently to search a pattern in a text. Let us first understand how two independent approaches work together in the Boyer Moore algorithm.

It processes the pattern and creates different arrays for both heuristics. At every step, it slides the pattern by the max of the slides suggested by the two heuristics. So it **uses best of the two heuristics at every step**.

### **Boyer Moore - Bad Character Heuristic**

Unlike the previous pattern searching algorithms, Boyer Moore algorithm **starts matching from the last character** of the pattern.

The idea of bad character heuristic is simple. The character of the text which doesn't match with the current character of the pattern is called the **Bad Character**. Upon mismatch, we shift the pattern until –

- 1) The mismatch becomes a match
- 2) Pattern P move past the mismatched character.

#### **Case 1 – Mismatch become match**

We will lookup the position of last occurrence of mismatching character in pattern and if mismatching character exist in pattern then we'll shift the pattern such that it get aligned to the mismatching character in text T.

**Explanation:** In the above example, we got a mismatch at position 3. Here our mismatching character is "A". Now we will search for last occurrence of "A" in pattern. We got "A" at position 1 in pattern (displayed in Blue) and this is the last occurrence of it. Now we will shift pattern 2 times so that "A" in pattern get aligned with "A" in text.

```
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
G C A A T G C C T A T G T G A C C
T A T G T G

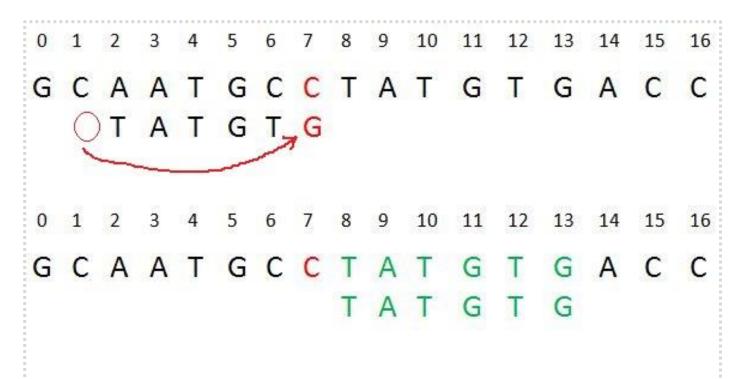
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
G C A A T G C C T A T G T G A C C
T A T G T G
```

### **Boyer Moore - Bad Character Heuristic**

#### **Case 2 – Pattern move past the mismatch character**

We'll lookup the position of last occurrence of mismatching character in pattern and if character does not exist we will shift pattern past the mismatching character.

**Explanation:** Here we have a mismatch at position 7. The mismatching character "C" does not exist in pattern before position 7 so we'll shift pattern past to the position 7 and eventually in above example we have got a perfect match of pattern (displayed in Green). We are doing this because, "C" do not exist in pattern so at every shift before position 7 we will get mismatch and our search will be fruitless.



### **Boyer Moore**

We preprocess the pattern and store the last occurrence of every possible character in an array of size equal to alphabet size. If the character is not present at all, then it may result in a shift by m (length of pattern).

```
/* Driver code */
int main()
     string txt= "ABAAABCD";
     string pat = "ABC";
     search(txt, pat);
     return 0;
 // This code is contributed by rathbhupendra
// The preprocessing function for Boyer Moore's
// bad character heuristic
void badCharHeuristic( string str, int size,
                        int badchar[NO OF CHARS])
    int i;
    // Initialize all occurrences as -1
    for (i = 0; i < NO OF CHARS; i++)</pre>
        badchar[i] = -1:
    // Fill the actual value of last occurrence
   // of a character
   for (i = 0; i < size; i++)</pre>
        badchar[(int) str[i]] = i;
```

```
/* A pattern searching function that uses Bad
Character Heuristic of Boyer Moore Algorithm */
void search( string txt, string pat)
    int m = pat.size();
   int n = txt.size();
    int badchar[NO_OF_CHARS];
    /* Fill the bad character array by calling
    the preprocessing function badCharHeuristic()
    for given pattern */
    badCharHeuristic(pat, m, badchar);
    int s = 0; // s is shift of the pattern with
               // respect to text
    while(s <= (n - m))
        int j = m - 1;
        /* Keep reducing index j of pattern while
        characters of pattern and text are
        matching at this shift s */
        while(j >= 0 && pat[j] == txt[s + j])
        /* If the pattern is present at current
        shift, then index j will become -1 after
        the above loop */
        if (j < 0)
            cout << "pattern occurs at shift = " << s << endl;
            /* Shift the pattern so that the next
            character in text aligns with the last
            occurrence of it in pattern.
            The condition s+m < n is necessary for
            the case when pattern occurs at the end
            s += (s + m < n)? m-badchar[txt[s + m]] : 1;
            /* Shift the pattern so that the bad character
            in text aligns with the last occurrence of
            it in pattern. The max function is used to
            make sure that we get a positive shift.
            We may get a negative shift if the last
            occurrence of bad character in pattern
           is on the right side of the current
            character. */
            s += max(1, j - badchar[txt[s + j]]);
```



Just like bad character heuristic, a preprocessing table is generated for good suffix heuristic.

Let t be substring of text T which is matched with substring of pattern P. Now we shift pattern until:

- 1) Another occurrence of t in P matched with t in T.
- 2) A prefix of P, which matches with suffix of t
- 3) P moves past t



#### Case 1: Another occurrence of t in P matched with t in T

Pattern P might contain few more occurrences of t. In such case, we will try to shift the pattern to align that occurrence with t in text T. For example:

**Explanation:** In the above example, we have got a substring t of text T matched with pattern P (in **green**) before mismatch at index 2. Now we will search for occurrence of t ("AB") in P. We have found an occurrence starting at position 1 (in **yellow** background) so we will right shift the pattern 2 times to align t in P with t in T. This is weak rule of original Boyer Moore and not much effective, we will discuss a Strong Good Suffix rule shortly.

i.	0	1	2	3	4	5	6	7	8	9	10
Т	Α	В	Α	Α	В	Α	В	Α	С	В	Α
р	С	Α	В	Α	В				8 8		

i	0	1	2	3	4	5	6	7	8	9	10
Т	Α	В	A	A	В	Α	В	Α	С	В	Α
Р			С	Α	В	Α	В		£)		

Figure - Case 1



#### Case 2: A prefix of P, which matches with suffix of t in T

It is not always likely that we will find the occurrence of t in P. Sometimes there is no occurrence at all, in such cases sometimes we can search for some suffix of t matching with some prefix of P and try to align them by shifting P. For example:

**Explanation:** In above example, we have got t ("BAB") matched with P (in **green**) at index 2-4 before mismatch. But because there exists no occurrence of t in P we will search for some prefix of P which matches with some suffix of t. We have found prefix "AB" (in the **yellow** background) starting at index 0 which matches not with whole t but the suffix of t "AB" starting at index 3. So now we will shift pattern 3 times to align prefix with the suffix.

1	0	1	2	3	4	5	6	7	8	9	10
Т	Α	Α	В	Α	В	Α	В	Α	С	В	Α
р	Α	В	В	Α	В	9		S 05			i i

i	0	1	2	3	4	5	6	7	8	9	10
Т	Α	Α	В	Α	В	Α	В	Α	С	В	Α
Р		3		Α	В	В	Α	В			

Figure - Case 2



#### Case 3: P moves past t

If the above two cases are not satisfied, we will shift the pattern past the t. For example:

**Explanation:** If above example, there exist no occurrence of t ("AB") in P and also there is no prefix in P which matches with the suffix of t. So, in that case, we can never find any perfect match before index 4, so we will shift the P past the t ie. to index 5.

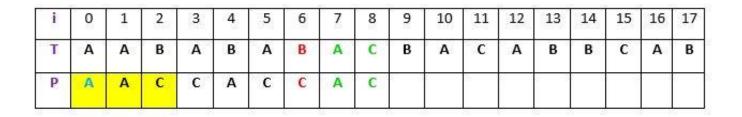
i	0	1	2	3	4	5	6	7	8	9	10
Т	Α	Α	C	Α	В	Α	В	Α	С	В	Α
Р	С	В	A	Α	В						

i	0	1	2	3	4	5	6	7	8	9	10
Т	Α	В	Α	А	В	А	В	А	С	В	Α
Р	i i	)	\$3 ÷		in i	С	В	Α	Α	В	

Figure - Case 3

Suppose substring q = P[i to n] got matched with t in T and c = P[i-1] is the mismatching character. Now unlike case 1 we will search for t in P which is not preceded by character c. The closest such occurrence is then aligned with t in T by shifting pattern P. For example:

**Explanation:** In above example, **q = P[7 to 8]** got matched with t in T. The mismatching character **c** is "C" at position P[6]. Now if we start searching t in P we will get the first occurrence of t starting at position 4. But this occurrence is preceded by "C" which is equal to **c**, so we will skip this and carry on searching. At position 1 we got another occurrence of t (in the **yellow** background). This occurrence is preceded by "A" (in **blue**) which is not equivalent to **c**. So we will shift pattern P 6 times to align this occurrence with t in T. We are doing this because we already know that character **c = "C"** causes the mismatch. So any occurrence of t preceded by c will again cause mismatch when aligned with t, so that's why it is better to skip this.



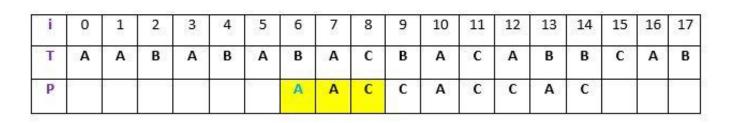


Figure - strong suffix rule

As a part of preprocessing, an array **shift** is created. Each entry **shift[i]** contain the distance pattern will shift if **mismatch** occur at position **i-1**. That is, the suffix of pattern starting at position **i is matched** and a **mismatch** occur at position **i-1**. Preprocessing is done separately for strong good suffix and case 2 discussed above.

#### 1) Preprocessing for Strong Good Suffix

Before discussing preprocessing, let us first discuss the idea of border. A **border** is a substring which is both **proper suffix** and **proper prefix**. For example, in string "**ccacc**", "**c**" is a border, "**cc**" is a border because it appears in both end of string but "**cca**" is not a border.

As a part of preprocessing an array **bpos** (border position) is calculated. Each entry **bpos[i]** contains the starting index of border for suffix starting at index i in given pattern P.

The suffix  $\phi$  beginning at position m has no border, so **bpos**[m] is set to m+1 where m is the **length of the pattern**.

The shift position is obtained by the borders which cannot be extended to the left. Following is the code for preprocessing.

**Explanation:** Consider pattern P = "ABBABAB", m = 7.

The widest border of suffix "AB" beginning at position i = 5 is  $\phi(nothing)$  starting at position 7 so **bpos[5] = 7**.

At position i = 2 the suffix is "BABAB". The widest border for this suffix is "BAB" starting at position 4, so j = bpos[2] = 4.

We can understand **bpos[i] = j** using following example

```
0 1 2 3 4 5 6 7

A B B A B A B

B A B A B

border
```

```
void preprocess strong suffix(int *shift, int *bpos,
                  char *pat, int m)
   int i = m, j = m+1;
   bpos[i] = j;
   while(i > 0)
        while(j <= m && pat[i-1] != pat[j-1])
            if (shift[i] == 0)
                shift[j] = j-i;
            j = bpos[j];
        i--; j--;
        bpos[i] = j;
```

i	0	1	2	3	 (i-1)	i.	***	(j-1)	j	***	m
Р	Α	Α	В	Α	 #	х	***	3	х		Φ

If character # Which is at position i-1 is equivalent (==) to character? at position j-1, we know that border of suffix at i-1 begin at j-1 or bpos[i-1] = j-1 or in the code.

```
i--;
j--;
bpos[i] = j
```

i	0	1	2	3	 (i-1)	i	****	(j-1)	j	****	m
Р	Α	Α	В	Α	 #	х	***	?	х	***	Φ

But if character # at position i-1 do not match with character? at position j-1 then we continue our search to the right. Now we know that.

- 1. Border width will be smaller than the border starting at position j ie. smaller than **x...φ**
- 2. Border has to begin with # and end with  $\phi$  or could be empty (no border exist).

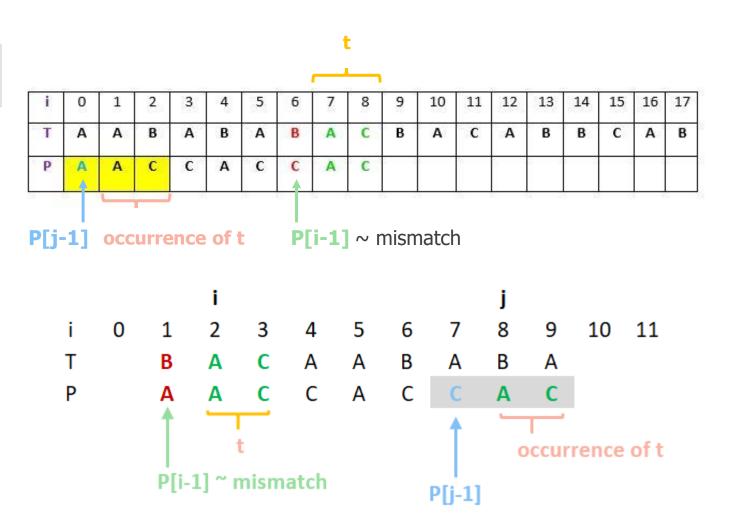
With above two facts we will continue our search in sub string  $\mathbf{x}...\mathbf{\phi}$  from position  $\mathbf{j}$  to  $\mathbf{m}$ . The next border should be at  $\mathbf{j} = \mathbf{bpos[j]}$  (because  $\mathbf{bpos[j]}$  is the border position of  $\mathbf{j} => \mathbf{p[j]} == \mathbf{p[bpos[j]]}$ ). After updating  $\mathbf{j}$ , we again compare character at position  $\mathbf{j-1}$  (?) with  $\mathbf{m}$  and if they are equal then we got our border otherwise we continue our search to right  $\mathbf{m}$  (out of pattern). This process is shown by code

```
while(j <= m && pat[i-1] != pat[j-1])
{
    j = bpos[j];
}
i--; j--;
bpos[i]=j;</pre>
```

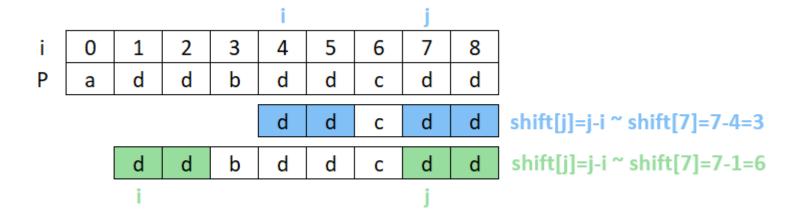
i	0	1	2	3	 (i-1)	i	<b>555</b> (3)	(j-1)	j	****	m
Р	Α	Α	В	Α	 #	x	***	?	x	***	Φ

In above code look at these conditions:

This is the condition which we discussed in case 2 (in Strong Good Suffix Heuristic). When the **character preceding** the **occurrence** of **t** in pattern P is different than mismatching character in P (**P[i-1**]), we **stop** skipping the occurrences and shift the pattern. So here **P[i]** == **P[j]** but **P[i-1]**!= **P[j-1]** so we shift pattern **from i to j**. So **shift[j]** = **j-i** is recorder for **j**. So whenever any mismatch occur at position **j** we will shift the pattern **shift[j+1]** positions to the right.



In above code the following condition is very important.



This condition prevent modification of **shift[j]** value from suffix having same border. For example, Consider pattern P = "addbddcdd", when we calculate **bpos[i-1]** for i = 4 then j = 7 in this case. we will be eventually setting value of **shift[7]** = 3.

Now if we calculate **bpos[i-1]** for i = 1 then j = 7 and we will be setting value **shift[7]** = 6 again, if there is no test shift[j] == 0. This mean if we have a **mismatch at position 6** we will **shift pattern P 3 positions** to right **not 6 position**.

=> DO NOT MISS ANY CASES.

#### 2) Preprocessing for Case 2

In the preprocessing for case 2, for each suffix **the widest border of the whole pattern** that is contained in that suffix is determined.

The starting position of the widest border of the pattern at all is stored in **bpos[0]** 

In the following preprocessing algorithm, this value **bpos[0]** is stored initially in all free entries of array shift. But when the suffix of the pattern becomes shorter than **bpos[0]**, the algorithm continues with the next-wider border of the pattern, i.e. with **bpos[j]**.

# **Boyer Moore | Code of Strong Good Suffin**

```
// preprocessing for strong good suffix rule
void preprocess_strong_suffix(int *shift, int *bpos,
                                char *pat, int m)
   // m is the length of pattern
   int i=m, j=m+1;
   bpos[i]=j;
   while(i>0)
        /*if character at position i-1 is not equivalent to
          character at j-1, then continue searching to right
          of the pattern for border */
        while(j<=m && pat[i-1] != pat[j-1])</pre>
            /* the character preceding the occurrence of t in
               pattern P is different than the mismatching character in P,
               we stop skipping the occurrences and shift the pattern
               from i to j */
            if (shift[j]==0)
                shift[j] = j-i;
            //Update the position of next border
            j = bpos[j];
        /* p[i-1] matched with p[j-1], border is found.
           store the beginning position of border */
        i--;j--;
        bpos[i] = j;
```

## **Boyer Moore | Code of Strong Good Suffix**

```
//Driver
int main()
{
    char text[] = "ABAAAABAACD";
    char pat[] = "ABA";
    search(text, pat);
    return 0;
}
```

```
/*Search for a pattern in given text using
 Boyer Moore algorithm with Good suffix rule */
void search(char *text, char *pat)
   // s is shift of the pattern with respect to text
   int s=0, j;
   int m = strlen(pat);
   int n = strlen(text);
   int bpos[m+1], shift[m+1];
   //initialize all occurrence of shift to 0
   for(int i=0;i<m+1;i++) shift[i]=0;</pre>
   //do preprocessing
   preprocess_strong_suffix(shift, bpos, pat, m);
   preprocess_case2(shift, bpos, pat, m);
   while(s <= n-m)</pre>
       j = m-1;
       /* Keep reducing index j of pattern while characters of
             pattern and text are matching at this shift s*/
       while(j \ge 0 \&\& pat[j] == text[s+j])
           j--;
       /* If the pattern is present at the current shift, then index j
            will become -1 after the above loop */
       if (j<0)
           printf("pattern occurs at shift = %d\n", s);
           s += shift[0];
       else
           /*pat[i] != pat[s+j] so shift the pattern
             shift[j+1] times */
           s += shift[j+1];
```

#### **Output:**

```
pattern occurs at shift = 0
pattern occurs at shift = 5
```



# Thank you!

**Algorithm Problem Solving – Samsung Vietnam R&D Center** 

Compose by phuong.ndp@samsung.com



https://theasciicode.com.ar/

https://techterms.com/definition/ascii

https://www.computerhope.com/jargon/a/ascii.htm

https://www.interproinc.com/blog/unicode-101-introduction-unicode-standard

https://unicode.org/standard/WhatIsUnicode.html

https://www.geeksforgeeks.org/strings-in-c-2/

https://www.tutorialspoint.com/cplusplus/cpp\_strings.htm

https://www.programiz.com/cpp-programming/strings

https://javaconceptoftheday.com/how-the-strings-are-stored-in-the-

memory/#:~:text=This%20part%20of%20the%20heap,stored%20in%20the%20heap%20memory.

https://thuytrangcoding.wordpress.com/2018/02/11/string-match-kmp/

https://stackjava.com/algorithm/thuat-toan-tim-kiem-knuth-morris-pratt.html

https://www.geeksforgeeks.org/kmp-algorithm-for-pattern-searching/

https://www.geeksforgeeks.org/boyer-moore-algorithm-good-suffix-heuristic/?ref=rp