Closeness

Introduction to Network Science Carlos Castillo Topic 17



Sources

- Networks, Crowds, and Markets Ch 3.6B
- Barabási 2016 Section 9.3.2
- P. Boldi and S. Vigna: Axioms for Centrality in Internet Mathematics 2014.
- Esposito and Pesce: Survey of Centrality 2015.
- C. Castillo: Other centrality slides 2016

Types of centrality measure

- Spectral
 - HITS
 - PageRank

Non-spectral

- Degree
- Closeness and harmonic closeness
- Betweenness

Is u a well-connected person?

- Degree: u has many connections
- Eigenvector: u is connected to the well-connected
- Closeness: *u* is close to many people
 - Average distance from u is small
- Betweenness: many connections pass through u
 - Large number of shortest paths pass through u

Closeness

Closeness

- Distance between two nodes is d(u, v)
- Closeness is the reciprocal of distances

closeness
$$(u) = \frac{1}{\sum_{v \in V, v \neq u} d(u, v)}$$

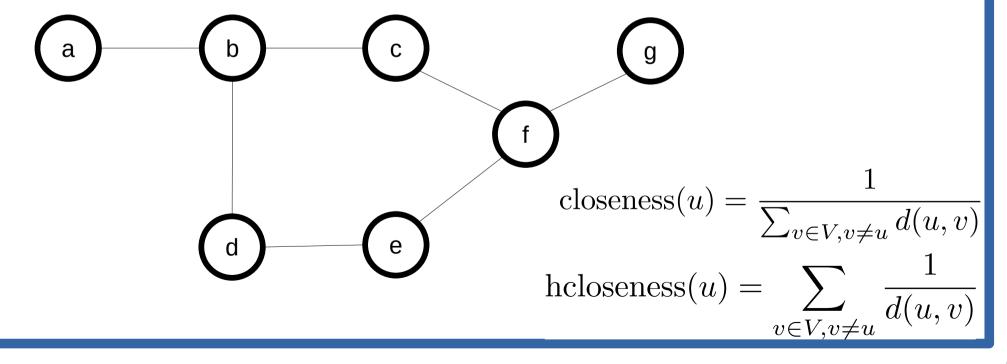
• Some graphs are not connected, in that case d(u,v) can be ∞ ; assuming $1/\infty = 0$ one can define the **harmonic closeness**:

$$hcloseness(u) = \sum_{v \neq u} \frac{1}{d(u, v)}$$

Exercise

Answer in Google Spreadsheet

Compute closeness and harmonic closeness for all the nodes d(u,v) = 1 if v is a neighbor of u



Summary

Things to remember

- Closeness and harmonic closeness definitions
- Try to compute them on your own on a graph