	NAME	NIA		GRADE	
	Introduction to Network Science (2019-2020)				
	WRITE YOUR ANSWERS CI TO COMMUNICATE SOMETHING IN WRITE. IF FOR SOME REASON (FO THAT THERE IS SOME MISTAKE THA YOUR EXAM. IN THIS CASE, INDICA ALSO, YOU MAY USE OTHER SHEET	WRITTEN TO ANOTHER PERS R EXAMPLE, IF AFTER YOU I T YOU WOULD LIKE TO CORR ATE CLEARLY THAT THE SOLU	SPACES. WRITE AS ON WHO IS GOING TO FOUND THE SOURCET) YOU CAN ATTACH UTION CAN BE FOUND IT	EVALUATE WHAT YOU LUTION YOU REALIZE AN EXTRA SHEET TO	
Prob	lem 1			1	point
a linkare of	nalyst investigating reports of police of between two nodes if the officers has ften connected to each other. Indicate	we ever gone on patrol togeth	ner. In this network, it is	s found that corrupt of	
1.					
2.					
Prob	lem 2			1	point
1.	Write a formula for the average degree the sum of the degree of nodes, S .	ree $\langle k \rangle$ of a network as a func	tion of the number of ne	odes of the network, N	7, and
2.	Write a formula for the expected num degree $\langle k \rangle$.	nber of links L of an ER (Erdö	s-Renyi) graph of N nod	les that has expected av	⁄erage
Prob	lem 3			1	point
Defin	ne briefly but precisely :				
1.	Connected graph				
2.	Clique				
3.	Bi-partite graph				
4.	ER (Erdös-Renyi) graph				

Draw a connected and bi-partite directed graph of 5 nodes and 15 links in which there are no nodes with degree zero. Draw the degree distribution for this graph, indicating clearly the label of each axis. Write its adjacency matrix.

Problem 5 2 points

Indicate the local clustering coefficient of each node in the figure.



• B.



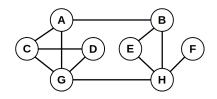
• D.

• E.

• F.

• G.

• H.



Problem 6 1 point

- 1. Indicate if an ER network of 192,244 nodes and 609,066 edges is in sub-critical, critical, super-critical, or connected regime, justifying briefly your answer.
- 2. Explain briefly what this means.
- 3. Indicate what is the minimum number of links this graph would need to be in connected regime.
- 4. Having $\langle k \rangle \geq 1$ is necessary, sufficient, or necessary and sufficient for an ER graph to be connected?

Problem 7 3 points

Imagine a **connected** network of N=1,000,000 nodes and average degree $\langle k \rangle = 5$ (indicate in each case the formula you are using and the result):

