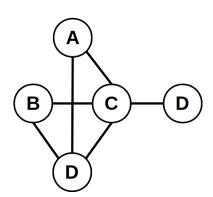
	NAME	NIA	GRADE
	Introduc	tion to Network Science (2018  —— RECOVERY EXAM ———	,
		— RECOVERY EXAM ——	
	TO COMMUNICATE SOMETHING IN W WRITE. IF FOR SOME REASON (FOR THAT THERE IS SOME MISTAKE THAT YOUR EXAM. IN THIS CASE, INDICATE	EARLY IN THE BLANK SPACES.  VRITTEN TO ANOTHER PERSON WHO IS REXAMPLE, IF AFTER YOU HAVE WRITT IT YOU WOULD LIKE TO CORRECT) YOU CE CLEARLY THAT THE SOLUTION CAN ITS TO PERFORM YOUR CALCULATIONS.	GOING TO EVALUATE WHAT YOU EN THE SOLUTION YOU REALIZE AN ATTACH AN EXTRA SHEET TO
Prol	olem 1		1 point
Indi	cate the characteristics of an adjacency	matrix representing:	
1.	A directed graph in which node $i$ has	out-degree $r$ .	
2.	A directed graph in which node $i$ has	in-degree $r$ .	
3.	A directed graph in which node $i$ has	a self-loop.	
4.	An undirected graph.		
5.	An undirected graph made of two con	nected components.	
Prob	olem 2		1 point
In a	random graph (Erdös-Rényi) of $n$ node	es with connection probability $p$ , what is	
1.	the expected number of links $\langle L \rangle$ .		
2.	the average degree $\langle k \rangle$ .		
3.	the mode (most frequent value) of the	e degree distribution.	
4.	the total number of nodes at distance	es $1, 2, \ldots, d$ , i.e., the number of nodes at	distance $\leq d$ .

Problem 3 1 point

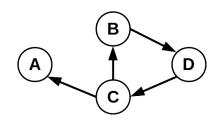
Indicate the following:

- 1. clustering coefficient of node A
- 2. clustering coefficient of node B
- 3. clustering coefficient of node C
- 4. clustering coefficient of node D
- 5. diameter of the graph

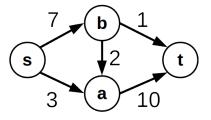


Problem 4 2 point

Compute two iterations of the hubs and authorities algorithm on this graph. Initialize all nodes to have a hub score of 1.0. Indicate all intermediate values of the hub and authority scores for every node.



1. Write the linear program ("minimize objective function subject to constraints") for minimum cut from s to t in this graph. Name the unknown variables  $u_s, u_a, u_b, u_t, y_{sb}, y_{sa}, y_{bt}, y_{at}, y_{ab}$ . Remember  $y_{ij}$  will be 1 if the edge from i to j is part of the minimum cut. Two constraints you must include are  $u_s = 1$  and  $u_t = 0$ .



2. Guess the solution by visual inspection, indicate the value of all the  $u_i$  and  $y_{ij}$  variables in your solution.

- 3. Indicate the value of the objective function.
- 4. Show that each of the constraints is held.

## Explain the following:

1. Why in the SI model, the derivative of the number of infected nodes i(t) at time t is ...?

$$\frac{di(t)}{dt} = i(t) \langle k \rangle (1 - i(t)) \beta$$

- 2. In the previous equation, what does the  $\beta$  parameter represent precisely?
- 3. Why in the SIS model, the derivative of the number of infected nodes i(t) at time t is ...?

$$\frac{di(t)}{dt} = i(t) \langle k \rangle (1 - i(t)) \beta - \mu i(t)$$

- 4. In the previous equation, what does the  $\mu$  parameter represent precisely?
- 5. For the SIR model, write the equations for  $\frac{di(t)}{dt}$ ,  $\frac{dr(t)}{dt}$ ,  $\frac{ds(t)}{dt}$ , where at time t, i(t) are the number of infected nodes, r(t) the number of recovered nodes, and s(t) the number of susceptible nodes.

6. In the SIR model, what is the limit of i(t) when  $t \to \infty$ ?