Memoryless property of geometric random variables.

Note: these are the only discrete random variable to have such a property. Say X is Geometric (p) random variable,

$$P(X>8|X>3) = \frac{P(X>8 & X>3)}{P(X>3)} = \frac{P(X>8)}{P(X>3)} = \frac{8}{3} = \frac{5}{3}$$

$$= \frac{1}{3} = \frac{5}{3} = \frac{5$$

$$P(X > i+j \mid X > i) = \frac{P(X > i+j \mid \delta X > i)}{P(X > i)} = \frac{P(X > i+j)}{P(X > i)} = \frac{2^{i+j}}{P(X > i)}$$