Chebyshev's Inequality  $P(|X-E(X)|\geq k)\leq \frac{V_{ar}(X)}{L^2}$ , for  $k\geq 0$ 

Why? Use Markov's Inequality with (X-E(X))2 instead of X and 12 instead of a.

Markov's laequality says:

$$P((X-E(X))^{2} \ge k^{2}) \le \frac{E((X-E(X))^{2})}{k^{2}}$$

$$P(|X-E(X)| \ge k) \le \frac{Var(X)}{k^2}$$

another version, use kox instead of k

k 2 Var(X) instead of k2, we get!

$$P(|X-E(X)| \ge ko_X) \le \frac{Vac(X)}{k^2 Vac(X)}$$

$$P(|X-E(X)| \ge k\sigma_X) \le \frac{1}{k^2}$$

i.e. The probability that X is more than k Standard Javiations away from its mean is no larger than 1/2.

Equivalently,

$$P(|X-E(X)| \leq k\sigma_X) \geq 1 - \frac{1}{k^2}$$

1.e. the probability X is within k standard deviations of its mean is at least  $1-\frac{1}{k^2}$ .