

## Ch-1 Integers

### Introductory Activity

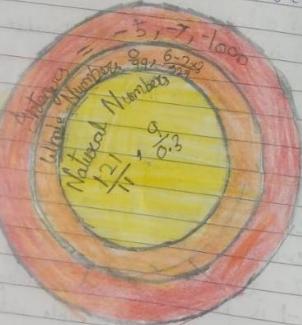
In this magic square, sum of the numbers in every row, column and each of the ~~diag~~ diagonals is -2.  
Fill in the blanks.

7	-7	-6	4
-4	2	1	-1
0	-2	-3	3
-5	5	6	-8

and less than every positive integer.  
Diagrammatic representation of integers (version diagram)

Where could you place the given integers?

$$\left\{ -5, \frac{12}{11}, -7, \frac{9}{0.3}, \frac{0}{99}, -1000, 6 - 2 \times 9, \frac{529}{3} \right\}$$



## NATURAL NUMBERS

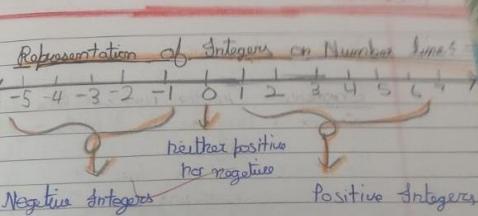
- \* Natural numbers are counting numbers.
- \* It doesn't include 0
- \*  $N = \{1, 2, 3, 4, \dots\}$
- \* The largest natural number is undefined.

### Whole Numbers

- \* The set of natural nos. together with zero.
- \*  $W = \{0, 1, 2, \dots\}$
- \* Zero is the smallest whole number.

### Integers

- \* The set of natural numbers together with whole nos.
- \* Denoted by ' $\mathbb{Z}$ '
- \* ' $\mathbb{Z}$ ' comes from the german word 'zahlen' which means to count.
- \*  $\mathbb{Z} = \{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$
- \* -1 is the greatest negative integer.
- \* 1 is the smallest possible integer.
- \* Zero is neither positive nor negative.
- \* Zero is greater than every negative integer.



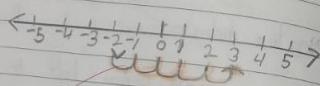
- \* As you move from left to right on a number line, the value of the integer increases.
- \* From right to left the value decreases.

### Ordering of Integers

- \* Order of integers on the left side of the number line are smaller than 0 and order of integers on the right side of the number line.
- \* All positive integers are greater than negative integers.
- \* On the number line all integers are equivalent.

from each other.

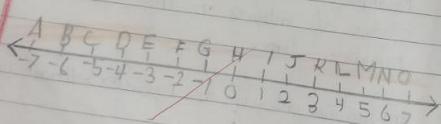
Example:- On the number line which number is 5 units right of 2



Sol. 3 is 5 units right of -2

### Try These

- 1) A number line representing integers is given below:

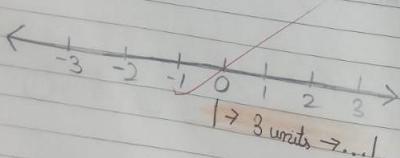


### Absolute Value of Integers :-

- \* Absolute value of a number is the distance from zero to that number on the number line.
- \* That distance is always positive.
- \* The symbol of absolute value is "||".
- \*  $|x| = x$  and  $|x| = -x$  where  $x$  is any integer.

### Example of absolute value

- \* The distance from 0 to 3 is three units. Thus  $|3| = 3$  and the absolute value of 3 is 3.



-3 and -2 are marked by E and F respectively. Which integers are marked by B, D, H, J, M, O

Sol  
B = -6  
D = -4  
H = 0  
J = 2  
M = 5  
O = 7

- 2) Arrange the numbers, 7, -5, 4, 0 in ascending order and then mark them in a number line to check your answer.

Sol Ascending order = -5, 0, 4, 7



- \* Similarly, the distance from 0 to -3 is also 3 units. Thus -3 is also equal to 3.

### NOTE:-

- \* The absolute value of a positive number is positive  $|5| = 5$ .
- \* The absolute value of a negative number is positive  $|-5| = 5$ .
- \* The absolute value of 0 is 0.

Additive Inverse

- \* If the sum of any two integers is zero, then each integer is called the additive inverse of the other.
- \* If 'A' is any integer then,  $a + (-a) = a - a = 0$
- \* Examples:-
- \* Additive inverse of 10 is  $-10$ , as  $10 + (-10) = 0$
- \* Additive inverse of  $9$  is  $-9$ , as  $(-9) + 9 = 0$
- Note:-
- \* Additive inverse of  $0$  is  $0$  itself.
- \* Additive inverse is also called the opposite of the number.

Negative (-)

Decrease

Lose

Below

Down

Withdraw

Decrease

Fall

Lower

Drop

Reduce

POSITIVE

Increase

Gain

Above

Up

Deposit

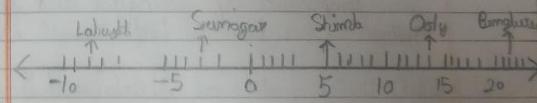
Climb

Rise

Raise

Grow

Warm

Ex 1.1 (Pg -4)

a. Lahulspiti =  $-8^{\circ}\text{C}$   
 Srinagar =  $-2^{\circ}\text{C}$   
 Shimla =  $5^{\circ}\text{C}$   
 Ooty =  $22^{\circ}\text{C}$

- Bengaluru =  $22^{\circ}\text{C}$
- b. Hottest place = Bengaluru =  $22^{\circ}\text{C}$   
 Coldest place = Lahulspiti =  $-8^{\circ}\text{C}$   
 Difference =  $22^{\circ}\text{C} - (-8)^{\circ}\text{C}$   
 $= 22^{\circ}\text{C} + 8^{\circ}\text{C}$   
 $= 30^{\circ}\text{C}$
- c. Difference between Lahulspiti and Srinagar:  
 $\Rightarrow -8^{\circ}\text{C} - (-2)^{\circ}\text{C}$   
 $\Rightarrow -8^{\circ}\text{C} + 2^{\circ}\text{C}$   
 $\Rightarrow -6^{\circ}\text{C}$
- d. Temperature of Srinagar and Shimla  
 Yes, temperature of Srinagar and Shimla together is less than the temperature at Shimla.  
 No, the temperature of Shimla and Srinagar together is not less than the temperature at Srinagar.

## HW

2. Jack scores in 5 successive seconds are  $25, -5, -10, 15$  and  $10$ .

Sol. Total score  $\Rightarrow 25 + 15 + 10 + (-5) + (-10)$   
 $\Rightarrow$

Positive	Negative	Total
25	-5	20
+15	-10	-15
+10	-15	35
50		

 $\Rightarrow 35$ Temperature at Srinagar on Monday =  $-5^{\circ}\text{C}$ Temperature at Srinagar dropped by  $-2^{\circ}\text{C}$  =  $-7^{\circ}\text{C}$ Temperature at Srinagar on Tuesday =  $-7^{\circ}\text{C}$ Temperature at Srinagar on Wednesday rose by  $4^{\circ}\text{C}$  $= -7^{\circ}\text{C} + 4^{\circ}\text{C}$  $= -3^{\circ}\text{C}$

4. Given:-

$$\begin{aligned} \text{Height of a plane above sea level} &= +5000 \\ \text{Submarine floating below sea level} &= -12000 \\ \text{Vertical distance between them} &= 5000 - (-12000) \\ &= 5000 + 12000 \\ &= 17000 \end{aligned}$$

Given:-

$$\begin{aligned} \text{Distance travelled by Rita towards east} &= +20 \text{ km} \\ \text{Distance travelled by Rita towards west} &= -30 \text{ km} \\ \text{Distance travelled by Rita towards} & \\ \text{The distance travelled towards west is expressed} & \\ \text{by negative sign.} & \\ \text{Final Position} &= 20 - 30 = -10 \text{ km} \end{aligned}$$

HW

5. Money Mohan deposited in her bank = ₹ 2000  
Money Mohan withdrew in her bank = ₹ 1642

If deposit withdrawal money is denoted by -, then  
deposited money is denoted by +

$$\begin{aligned} \text{Money left after withdrawal} &= 2000 - 1642 \\ &= 358 \end{aligned}$$

7

(i)			(ii)		
5	-1	-4	-6	1	-10
-5	-2	7	0	-4	-3
0	3	-3	-6	4	-7
0	0	0	-9	-9	-9

Since a diagonal isn't equal to 0, (i) isn't a magic square

Since all sides and diagonals are equal.  
(ii) is a magic square

8. Verify  $a - (-b) = a + b$

(iii)  $a = 75, b = 84$   
 $a - (-b) = a + b$   
 $75 - (-84) = 75 + 84$   
 $75 + 84 = 159$   
 $LHS = RHS$   
Hence verified

(iv)  $a = 28, b = 11$

$$\begin{aligned} a - (-b) &= a + b \\ 28 - (-11) &= 28 + 11 \\ 28 + 11 &= 28 + 11 \\ 39 &= 39 \checkmark \\ LHS &= RHS \\ \text{Hence Verified} & \end{aligned}$$

8 (i)

$$a = 21, b = 18$$

HW

$$a - (-b) = a + b$$

$$\begin{aligned} a + b & \\ 21 - (-18) &= 21 + 18 \\ 21 + 18 &= 21 + 18 \\ 39 &= 39 \\ LHS &= RHS \end{aligned}$$

(ii)  $a = 118, b = 125$

$$\begin{aligned} a - (-b) &= a + b \\ 118 - (-125) &= 118 + 125 \\ 118 + 125 &= 118 + 125 \\ 243 &= 243 \\ LHS &= RHS \end{aligned}$$

9.  $>, <, =$

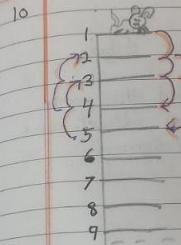
a.  $(-8) + (-4) \quad \boxed{<} \quad -8 - (-4)$   
 $\begin{array}{r} -8 \\ -4 \\ \hline -12 \end{array} \quad \begin{array}{r} -8 \\ +4 \\ \hline -4 \end{array}$

b.  $(-3) + (7) \div (-19) \quad \boxed{<} \quad 15 - 8 + (-9)$   
 $\begin{array}{r} -3 \\ +7 \\ \hline -15 \end{array} \quad \begin{array}{r} 15 \\ -8 \\ -9 \\ \hline -2 \end{array}$

c)  $23 - 41 + 11$   
 $34 - 41$  D  $23 - 41 - 11$   
 $-7$   $-29$

d)  $39 + (-24) - (+5)$   
 $39 - 24 - 15$  R  $36 + (-5) - (+3)$   
 $15 - 15$   $36 - 52 + 38$   
 $0$   $72 - 52$   
 $20$

(e)  $-231 + 79 + 51$   
 $-231 + 180$  D  $-399 + 159 + 81$   
 $-101$   $-399 + 240$   
 $-159$



(i) Jump 1 :-  $1+3+4$   
Jump 2 :-  $4-2=2$   
Jump 3 :-  $2+3=5$   
Jump 4 :-  $5-2=3$   
Jump 5 :-  $3+3=6$   
Jump 6 :-  $6-2=4$   
Jump 7 :-  $4+3=7$   
Jump 8 :-  $7-2=5$   
Jump 9 :-  $5+3=8$   
Jump 10 :-  $8-2=6$   
Jump 11 :-  $6+3=9$

Note: Downwards  
is taken as positive  
and above is negative

∴ By 11<sup>th</sup> Jump, the monkey  
reaching to water level 9

(ii) The monkey reaches stop 1 at 5<sup>th</sup> stop  
24/12/22

## Addition and Subtraction of Integers

\* Same sign add and put the same sign and opposite sign subtract and put the greater number sign.

Eg. 1)  $-15 - 10 = -25$   
2)  $+60 - 30 = 30$   
3)  $-99 + 1 = -98$   
4)  $100 - (-25) = 125$

## Multiplication of Integers

\* When the product is  
positive

\* When the product is  
negative

Eg: 1)  
2)  
3)  
4)

## Addition and Subtraction of Integers

Green box █ = +1

Red box █ = -1

1.  $5+4=$    $+$   = 9

 $=$       = 9

2.  $5-4=$    $-$   =  = 1

 $=$      $-$     =  = 1

## Multiplication of two integers

- \* When the integers are of like signs -  
product is positive
- \* When the integers are of unlike signs -  
product is negative.

Eg: 1)  $-5 \times -3 = 15$   
2)  $-15 \times 10 = -150$   
3)  $100 \times 5 = 500$   
4)  $6 \times -2 = -12$

a	b	$a \times b$
+	+	+
-	+	-
-	-	+
+	-	-

## Division of two integers

- \* When the dividend and divisor are of unlike signs: quotient is negative
- \* When the dividend and divisor are of

like signs: Quotient is Positive

e.g. 1.  $\frac{-100}{5} = -20$   
2.  $\frac{25}{-5} = -5$   
3.  $\frac{-625}{-25} = 25$   
4.  $\frac{121}{11} = 11$

Ex 1.4

1. a.  $\frac{-30}{10} = -3$

b.  $\frac{50}{-5} = -10$

c.  $\frac{(-36)}{(-9)} = +4$

d.  $(-49) \div (49)$

$\frac{-49}{49} = -1$

e.  $13 \div [(-2) + 1]$   
 $13 \div -1$   
 $\frac{13}{-1} = -13$

f.  $0 \div (-12) = 0$

g.  $(-31) \div [(-30) + (-1)]$   
 $(-31) \div (-31)$   
 $\frac{-31}{-31} = 1$

h.  $[(-36) \div 12] \div 3$   
 $\left[ \frac{-36}{12} \right] \div 3$

$-3 \div 3 = 1$

i.  $[((-6) + 3) \div (-2) + 1]$   
 $3 \div \frac{-1}{-1} = 1$

2. a.  $a \div (b+c) + (a \div b) + (a \div c)$   
a)  $a=12, b=-4, c=2$

LHS	RHS
$a \div (b+c)$ $12 \div (-4+2)$ $12 \div -2$ $\frac{12}{-2} = -6$	$(a \div b) + (a \div c)$ $12 \div (-4) + 12 \div 2$ $-3 + 6$ $3$

HW

b.  $a = (-10), b = 1, c = 1$

LHS	RHS
$a \div (b+c)$ $-10 \div (1+1)$ $-10 \div 2$ $5$	$a \div b + a \div c$ $(-10 \div 1) + (-10)$ $-10 + (-10)$ $20$

LHS  $\neq$  RHS, Hence verified

3.

- a)  $369 \div 1 = 369$   
 b)  $(-75) \div 75 = -1$   
 c)  $(-206) \div (-206) = 1$   
 d)  $(-87) \div (-1) = 87$   
 e)  $(-87) \div 1 = -87$   
 f)  $(-48) \div 48 = -1$   
 g)  $20 \div (-10) = -2$   
 h)  ~~$(-12) \div 4 = -3$~~

4.

Given :-

$$\begin{aligned} a \div b &= -3 \\ (6, -2) &\rightarrow 6 \div (-2) = -3 \\ (9, -3) &\rightarrow 9 \div (-3) = -3 \\ (12, -4) &\rightarrow 12 \div (-4) = -3 \\ (-3, 1) &\rightarrow -3 \div 1 = -3 \\ (15, -5) &\rightarrow 15 \div -5 = -3 \\ (18, -6) &\rightarrow 18 \div -6 = -3 \end{aligned}$$

5.

Given :-

$$\text{Temperature at } 12 \text{ noon} = 10^\circ \text{ above } 0 \\ = +10^\circ$$

For every hour, the temperature decreases by  $2^\circ\text{C} = -2^\circ\text{C}$

Time	Temperature
12 noon	$10^\circ$
1 o'clock	$8^\circ$
2 o'clock	$6^\circ$
3 o'clock	$4^\circ$
4 o'clock	$2^\circ$
5 o'clock	$0^\circ$
6 o'clock	$-2^\circ$
7 o'clock	$-4^\circ$
8 o'clock	$-6^\circ$
9 o'clock	$-8^\circ$
10 o'clock	$-10^\circ$
11 o'clock	$-12^\circ$
12 o'clock	$-14^\circ$

$\therefore$  At 12 o'clock, the temperature will be  $8^\circ\text{C}$  below zero ie,  $-8^\circ\text{C}$

The temperature at midnight  
=  $14^\circ$  below zero  
=  $-14^\circ\text{C}$

6. Given :-

Every correct answer: + 3 marks  
every incorrect answer: - 2 marks

(i) Radhika scored 20 marks

Correct answer = 20

Marks scored for correct answers =  $12 \times 3$ 

$$\Delta 36 - 20 = 16 \text{ marks}$$

= 36 marks

$$\frac{16}{2} = 8 \text{ were wrong answers.}$$

 $\therefore$  Radhika got 8 wrong answers.

(ii)

Score of Mahini = -5 marks

Correct answers = 7

Marks scored for correct answers =  $7 \times 3$ 

= 21 marks

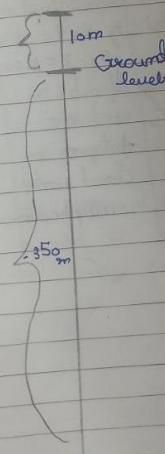
$$21 - (-5) = 21 + 5 = 26$$

$$\frac{26}{2} = 13 \text{ were wrong answers.}$$

 $\therefore$  Mahini got 13 wrong answers.

7. Given

An elevator descends into a mine shaft at the rate of 6 m/min.  
Descent starts from 10 m above the ground level.  
Distance travelled by an elevator = 10 m  
350 m  
= 360 m



Diagram

## PROPERTIES OF INTEGERS

### Closure Property of Integers

\* For every integers  $a, b \in \mathbb{Z}$   
(Where  $\in$  belongs to,  $\mathbb{Z}$  for all the  $a, b \in \mathbb{Z}$ )

Addition	Subtraction	Multiplication	Division
Eg: $-2 + 2 = 0 \in \mathbb{Z}$	Eg: $4 - (4) = 0 \in \mathbb{Z}$	Eg: $-4 \times 4 = -16 \in \mathbb{Z}$	Eg: $4 \div 2 = 2 \in \mathbb{Z}$
$2 - 8 + 8 = -16 \in \mathbb{Z}$	$5 - 5 = 0 \in \mathbb{Z}$	$-5 \times -3 = 15 \in \mathbb{Z}$	$2 \div 4 = \frac{1}{2} \notin \mathbb{Z}$
If $a, b \in \mathbb{Z}$ ,	If $a, b \in \mathbb{Z}$	If $a, b \in \mathbb{Z}$ ,	If $a, b \in \mathbb{Z}$ ,
$a + b \in \mathbb{Z}$	$a - b \in \mathbb{Z}$	$a \times b \in \mathbb{Z}$	$a \div b \notin \mathbb{Z}$
Integers are closed under addition	Integers are closed under subtraction	Integers are closed under multiplication	Integers are not closed under multiplication

✓ ✓ ✓ X

### Observation:-

\* The sum of any two integers, will always be an integer, ie if  $a, b$  are any integers,  $a+b$  will be an integer.

\* The difference of any two integers, will always be an integer, ie if  $a$  and  $b$  are any integers,  $a-b$  will also be an integer.

\* Any two integers product will be an integer, ie if  $a, b$  are integers,  $a \times b$  is an integer

\* Division doesn't follow closure property as if  $a$  and  $b$  are any integers,  $a \div b$  may or may not be an integer

### Commutative Property of Integers

#### Observations

\* Commutative property is only applicable for two arithmetic operations :- Addition and multiplication

\* Commutative property of addition:  
 $a + b = b + a$

\* Commutative property of multiplication:  
 $a \times b = b \times a$

### Associative Property of Integers

Addition	Subtraction	Multiplication	Division
Eg: $2, 3, 5 \in \mathbb{Z}$ $2+(3+5) = (2+3)+5$ $5+5 = 2+8$ $10 = 10$ $LHS = RHS$	Eg: $9, 5, 2 \in \mathbb{Z}$ $(9-5)-2 = 9-(5-2)$ $4-2 \neq 9-8$ $2 \neq 6$ $LHS \neq RHS$	Eg: $3, -2, 5 \in \mathbb{Z}$ $(3 \times 2) \times 5 = 3 \times (2 \times 5)$ $-6 \times 5 = 3 \times -10$ $-30 \neq -30$ $LHS \neq RHS$	Eg: $10, 5, 2 \in \mathbb{Z}$ $(10 \div 5) \div 2 = 2$ $10 \div (5 \div 2) = 10$ $LHS = RHS$

Eg: $-7, 3, 2 \in \mathbb{Z}$ $(-7+3)+2 = -7+(3+2)$ $-5+3 = -7+5$ $-2 = -2$ $LHS = RHS$	Eg: $-6, 2, 4 \in \mathbb{Z}$ $(-6-2)-4 = -6-(2-4)$ $-8-4 \neq -6-(2)$ $-12 \neq -6+2$ $LHS \neq RHS$	Eg: $-8, -4, 2 \in \mathbb{Z}$ $(-8 \div -4) \div 2 = -8 \div (-4 \div 2)$ $-8 \div (-4 \div 2) = 8 \div 2$ $72 = 72$ $LHS = RHS$
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$$a + (b+c) = (a+b)+c \quad a \cdot (b \cdot c) = (a \cdot b) \cdot c$$

$$(a-b)-c = a-(b+c) \quad a \cdot (b \cdot c) = a \cdot (b \cdot c)$$

### Observation

- \* The placement of parenthesis doesn't matter when it comes to adding or multiplication.

$$* a + (b+c) = (a+b)+c$$

$$* a \times (b \times c) = (a \times b) \times c$$

### Identity Property

- \* 0 is called the additive identity element.
- \* Eg:-  $0 + (-9) = (-9) + 0$

### Multiplicative Identity

- \* 1 is called the multiplicative Identity.
- \* Eg:-  $1 \times (-9) = (-9) \times 1$

### Distributive Property of Multiplication over Addition

\*  $a, b, c \in \mathbb{Z}$ , then

$$a \times (b+c) = (a \times b) + (a \times c)$$

Eg:- Verify distributive property of multiplication over addition of integers for  $a=5, b=-10, c=3$

LHS RHS

$$a \times (b+c)$$

$$5 \times (-10+3)$$

$$5 \times -7$$

$$-35$$

$$(a \times b) + (a \times c)$$

$$(5 \times -10) + (5 \times 3)$$

$$-50 + 15$$

$$-35$$

LHS = RHS

$$\therefore a \times (b+c) = (a \times b) + (a \times c)$$

Hence verified

### Distributive property of multiplication over subtraction

\*  $a, b, c \in \mathbb{Z}$ , then

$$[a \times (b-c) = (a \times b) - (a \times c)]$$

Eg Verify distributive property of multiplication over subtraction of integers for  $a=-8, b=5, c=-3$

LHS

$$a \times (b-c)$$

$$-8 \times 5 - (-3)$$

$$-8 \times 5 + 3$$

$$-8 \times 8$$

$$-64$$

RHS

$$(a \times b) - (a \times c)$$

$$-8 \times 5 - (-8 \times 3)$$

$$-40 - 24$$

$$64$$

LHS = RHS

$$\therefore a \times (b-c) = (a \times b) - (a \times c)$$

Hence Verified

### Problems :-

1) Verify the associative property over addition and multiplication when  $a=-7, b=-4, c=3$

=) Associative property over addition

LHS RHS

$$(a+b)+c$$

$$(-7+ -4)+3$$

$$-11 + 3$$

$$-8$$

$$a+(b+c)$$

$$-7+(-4+3)$$

$$-7+ -1$$

$$-8$$

$$\therefore (a \times b) \times c = a \times (b \times c)$$

=) Associative Property over Multiplication.

LHS

$$(a \times b) \times c$$

$$(-7 \times -4) \times 3$$

$$28 \times 3$$

RHS

$$a \times (b \times c)$$

$$-7 \times (-4 \times 3)$$

$$-7 \times (-12)$$

$$\begin{array}{ccc} 84 & = & 84 \\ \text{LHS} & = & \text{RHS} \end{array}$$

Let us understand this by an activity.

Aim: To verify Associative property under Addition for  $a = -3$ ,  $b = 2$ ,  $c = 5$

Procedure = Consider  
 $\square = -1$   
 $\blacksquare = +1$   
 $AS - L + (r) = 0$   
 $\blacksquare + \square = 0$

$$\begin{aligned} \text{LHS} &= a(b+c) \\ &= -3 + (2+5) \\ &= \square \square \square + (\blacksquare + \blacksquare \blacksquare \blacksquare) \\ &= \square \square \square + \blacksquare \blacksquare \blacksquare \blacksquare \blacksquare \blacksquare \\ &= \blacksquare \blacksquare \blacksquare = +4 \end{aligned}$$

$$\begin{aligned} \text{RHS} &: (a+b)+c \\ &= (-3+2)+5 \\ &= (\square \square \square + \square \square \square) + \blacksquare \blacksquare \blacksquare \blacksquare \blacksquare \blacksquare \\ &= \blacksquare \blacksquare \blacksquare = +4 \end{aligned}$$

$$= \square \square \square = +4$$

$$\text{LHS} = \text{RHS}$$

$$\therefore a + (b+c) = (a+b)+c$$

In a test (5) marks are given for every correct answer and (-2) marks for every incorrect answer. Radhika answered all the questions & scored 30 marks though she got 10 correct answers.

Ex 6

→ Jay also answered all the questions and scored (-12) marks though he got 4 correct answers.

How many incorrect answers had they attempted?

Sol \* Marks given for correct answers = 5  
 $\therefore$  Marks given for 10 correct answers =  $5 \times 10 = 50$

Radhika's score = 30  
 $\therefore$  Marks obtained for incorrect answers =  $30 - 50 = -20$

Marks given for 1 incorrect answer = (-2)  
 $\therefore$  No. of incorrect answers =  $(-20) \div (-2) = 10$

\* Marks given for 4 incorrect answers =  $5 \times 4 = 20$   
 $\therefore$  Jay's score = -12  
 $\therefore$  Marks obtained for incorrect answers =  $-12 - 20 = -32$   
 $\therefore$  Marks given for 1 incorrect answer = (-2)  
 $\therefore$  No. of incorrect answers =  $(-32) \div (-2) = 16$

Ex 7 A shopkeeper earns a profit of ₹1 by selling a pen and incurs a loss of 40 paise while selling pencils of her old stock.

→ In a particular month she incurs a loss of ₹3. In this period, she sold 48 pens. How many pencils did she sell in this period?

→ In the next month she neither earns a profit or loss. If she sold 70 pens, how many pencils did she sell?

Sol \* Profit earned by selling 1 pen = ₹1  
 $\therefore$  Profit earned by selling 48 pens = ₹48  
 $\therefore$  Total profit = ₹48

Total loss = ₹5, denoted as ₹-5

Profit earned + Loss incurred = Total loss

$\therefore$  Loss incurred = Total loss - Profit earned

= ₹(5 - 45) = ₹50 = -5000 paise

Loss incurred by selling one pencil = 40 paise

which we write as = -40 paise

$\therefore$  Number of pencils sold =  $(-5000) \div (-40) =$

125 pencils.

(ii) No profit or loss, Profit earned + Loss = 0  
 $\therefore$  Profit earned = - Loss, Profit = - Loss

Profit by selling 70 pens = ₹70

Loss = ₹70 or -7000 p

$\therefore$  Total pencils =  $(-7000) \div (-40) = 175$  pencils

Buy - Digg

$$1) -18 \times -10 \times 9$$

$$-18 \times -10 \times 9$$

$$180 \times 9$$

$$1620$$

$$-20 \times -2 \times -5 \times 7$$

$$40 \times -5 \times 7$$

$$-200 \times 7$$

$$-1400$$

$$(-1) \times (-5) \times -4 \times (-6)$$

$$[-1 \times -5] \times [-4 \times -6]$$

$$5 \times 24$$

$$120$$

Ex 1.2

$$1) a) \text{ Sum is } -7 \\ (-3) + (-4) = -7$$

$$b) \text{ Difference is } -10 \\ -3 - 7 = -10$$

$$c) \text{ Sum is } 0 \\ -10 + 10 = 0$$

$$2) a) \text{ Difference is } 8 \\ (-10) - (-18) = 8$$

$$b) \text{ Sum is } -5 \\ -10 + 5 = -5$$

$$c) \text{ Difference is } -3 \\ (-2) - (1) = -3$$

$$d) i) -5 + -8 = (8) + (5) \\ ii) -53 + 0 = -53$$

$$iii) 17 + (-17) = 0$$

$$iv) [13 + (-12)] + (-7) = 13 + (-12) + (-7)$$

$$(v) (-4) + [15 + (-3)] = [-4 + 15] + (-3)$$

Ex 1.3.

$$1) a. 3 \times (-1) = -3$$

$$j. (-3) \times (-6) \times (-2) \times (-1) = 36$$

$$2) a. 18 \times [7 + (-3)]$$

$$18 \times 7 - 3$$

$$18 \times 4$$

$$72$$

$$\text{LHS}$$

$$=$$

$$RHS$$

Hence Verified

b. HW

$$3) a) (-1) \times a = -a$$

$$b) -22$$

$$4) (-1) \times 5 = -5$$

$$(-1) \times 4 = -4$$

$$(-1) \times 3 = -3$$

$$(-1) \times 2 = -2$$

$$(-1) \times 1 = -1$$

$$(-1) \times 0 = 0$$

$$(-1) \times (-1) = 1$$

$$5) a) 26 \times (-68) + (-48) \times (-36) \\ b \times a + (a \times c) = a \times (b+c)$$

$$= (-48) \times [26 + (-36)]$$

$$= (-48) \times [26 - 36]$$

$$= (-48) \times (-10)$$

$$= 480$$

Distributive property of multiplication  
over addition

b.  $\underline{9 \times 53 \times [-125]}$

$\underline{-1000 \times 53}$

$\underline{-53000}$

c.  $15 \times (-25) \times (-4) \times 10$

$15 \times 10 \times [-25 \times -4]$

$15 \times (-10) \times 100$

$-150 \times 100$

$-150000$

d.  $(-41) \times 102$

$-41 \times (100+2)$

$-41 \times 100 + -41 \times 2$

$-4100 + 82$

$-4182$

Distributive Property of multiplication  
over addition

Ques

HW

$$(-21) \times [(-4) + (-6)] = [(-21) \times (-4)] + [(-21) \times (-6)]$$

RHS

LHS

$\underline{-21 \times [-4 + (-6)]}$

$\underline{-21 \times [-4 - 6]}$

$\underline{-21 \times -10}$

$\underline{210}$

$(-21 \times 4) + (-21 \times 6)$

$-84 + -126$

$-84 - 126$

$210$

LHS = RHS

Hence verified

Ex 1.3 1b.  $(-1) \times 225 = -225$

c.  $(-21) \times (-30) = 630$

d.  $(-316) \times (-1) = 316$

e.  $(-18) \times 0 \times (-18) = 0$

f.  $(-12) \times (-11) \times 10 = 1320$

g.  $9 \times (-3) \times (-6) = 162$

h.  $(-18) \times (-8) \times (-4) = (-360)$

i.  $(-1) \times (-2) \times (-3) \times 4 = (-24)$

HW

Ex 1.2

3. Given:-

$$\text{Scores of Team A} = -40, 10, 0$$

$$= (-40) + 10 + 0$$

$$= -30$$

$$\text{Score of Team B} = 10, 0, -40$$

$$= 10 + 0 + (-40)$$

$$= 10 - 40$$

$$= -30$$

$$30 = 30$$

$\therefore$  Both teams scored the same. Yes, we can add integers in any order.

21/6/23

HW

$$1. +30^\circ C - 38^\circ C = -8^\circ C \leftrightarrow B$$

$$2. \text{Additive inverse of } 5 = -5 \leftrightarrow E$$

$$3. -|-35| + |-36| = -35 + 36 = 1 = R$$

$$4. -|-7 - 4| + \text{Subtract } -45 \text{ from } -25$$

$$5. -21 + (-25 + 45) \Rightarrow -21 + 20 = -1 \leftrightarrow I$$

$$\text{Sum of exponents of } 5 \text{ and } 0 = 4 \leftrightarrow N$$

$$b - 6 \leftrightarrow D$$

$$6. (-25) + (-55) + 29 + 45$$

$$-25 + -55 + 29 + 45$$

$$-80 + 74$$

$$-6 \Rightarrow D$$

Finally we got "the kind"

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
-9	-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	

$$\begin{aligned} \text{P} & 625 \times (-35) = (-625) \times 35 \\ & (-625) \times (35) + (625) \times 35 \\ & \Rightarrow -625 \times 100 \end{aligned}$$

Distributive property of 'x' over '+'

$$\begin{aligned} \text{f} & 7 \times (50+2) \\ & \Rightarrow ax+b+c = axb - axc \\ & = (7 \times 50) - 7 \times 2 \\ & = 350 - 14 \\ & = 336 \end{aligned}$$

$$\begin{aligned} \text{g} & (-17) \times (-29) \\ & \Rightarrow 17 \times 29 \\ & = 17 \times (30-1) \\ & = 17 \times 30 - 17 \times 1 \\ & = 510 - 17 \\ & = 493 \\ & \text{DP of } \times \text{ over } + \end{aligned}$$

$$\begin{aligned} \text{h} & (-57) \times (-19) + 57 \\ & = 57 \times 19 + 57 \times 1 \\ & = 57 \times 19 + 1 \\ & = 57 \times 20 \\ & = 1140 \end{aligned}$$

Ans. 1140  
Method.

N

DP over of x over +

6. Given -

The room temperature will be dropped from  $40^{\circ}\text{C}$  at the rate of  $5^{\circ}\text{C}$  every hour. Temperatures after  $n$  hours =  $10 - 5n = -5^{\circ}\text{C}$

7. Total Questions = 10  
Correct =  $+5\text{ m}$   
Incorrect =  $-2\text{ m}$

i) Mohan

$$\begin{aligned} ca - 4 &= 4 \times 5 = 20 \\ ia - 6 &= 6 \times -2 = -12 \end{aligned}$$

ii) Rushma :-

$$\begin{aligned} ca - 5 &= 5 \times 5 = 25 \\ ia - 5 &= 5 \times -2 = -10 \\ -10 + 25 &= 15\text{ m} \end{aligned}$$

iii) Kusum :-

$$\begin{aligned} ca - 2 &= 2 \times 5 = 10 \\ ia - 5 &= 5 \times -2 = -10 \\ -10 + 10 &= 0 \end{aligned}$$

8. Given

Profit on white cement bag =  $\frac{8}{8}$   
Loss on grey cement =  $\frac{2}{3}$

(i) Profit on 3000 bags of white cement =  $8 \times 3000 = \text{₹}24000$

Loss on 5000 bags of grey cement =  $5 \times 5000 = \text{₹}25000$

Total loss =  $25000 - 24000 = \text{₹}1000$

(ii) No. of grey cement bags sold = 6400  
Loss on 6400 bags of grey cement =  $5 \times 6400 = 32000$

No. of white cement bags sold =  $\frac{32000}{8} = 4000$

$$\begin{array}{ll} \text{(Q. 9)} & -3x - 9 = 27 \\ \text{(H.W.)} & \begin{array}{l} b) 56 \\ c) -25 \\ d) 132 \end{array} \end{array}$$

### Simplification of Brackets

\* Order of Brackets =  $[ \{ ( ) \} ]$

\* B - Brackets  
O - Of  
D - Division  
M - Multiplication  
A - Addition  
S - Subtraction

HOTS

1. Find the value of.

$$(-1)^{100} \times (-1)^{100} + (-1)^{99}$$

$$\text{Ans. } \Rightarrow \frac{-1 \times 1 + 1}{1}$$

$$\Rightarrow \frac{-1 + 1}{1} = \frac{0}{1} = 0$$

Q. Evaluate:  $[\{(-15+5) \times 2 + 8\} - 32 \div 8] - 67$

$$\begin{aligned} &\Rightarrow [\{(-10) \times 2 + 8\} - 32 \div 8] + 7 \\ &\Rightarrow [(-20 + 8) - 32 \div 8] + 7 \\ &\Rightarrow [-12 - 32 \div 8] + 7 \\ &\Rightarrow [-12 - 4] + 7 \\ &\Rightarrow [-16] + 7 \\ &\Rightarrow -9 \end{aligned}$$

3. Find the side of a square whose area is  $10^{-3} \times (-2)^{29} \text{ cm}^2$

$$\begin{aligned} \text{Given. Area} &= (10 - 3 \times (-2)) \\ &= 10 + 6 \\ &= 16 \text{ cm}^2 \end{aligned}$$

$$\text{Side} = \sqrt{16} = \sqrt{4 \times 4} = 4$$

4. Find the perimeter of a sq whose side is  $-3 \times (1-3) \text{ cm}$

Ans. Given

$$\begin{aligned} \text{Side} &= -3 \times (1-3) \\ &= -3 \times -2 \end{aligned}$$

= 6 cm

$$\text{Perimeter} = 8 \times 4 \\ = 6 \times 4 \\ = 24$$

### 5. Simplify

a)  $14 - [3 + \{8 : (5-3) \cdot (2+3)\}]$   
 $14 - [3 + \{8 : (5-3 \times 6-5-6+3)\}]$   
 $14 - [3 + \{8 : (-2)\}]$   
 $14 - [3 + 4]$   
 $14 - 7$

36/4/23  
12/4/23

b)  $6 - [6 - \{6 - (6-5-3)\}]$   
 $6 - [6 - \{6 - (-2)\}]$   
 $6 - [6 - \{6 + 2\}]$   
 $6 - [6 - 8]$   
 $6 - (-2) = 6 + 2 = 8$

c)  $49 \div [49 + \{49 - (49 + 49 - 49)\}]$   
 $49 \div [49 + \{49 - (49)\}]$   
 $49 \div [49 + \{49 - 49\}]$   
 $49 \div [49 + \{0\}]$   
 $49 \div 49$   
1

6. At sunrise, the outside temperature was  $1^\circ$  below  $0^\circ$ . By lunch time, the temperature rose by  $17^\circ$  and then fell by  $4^\circ$  by night. What was the temperature by the end of the day?

[A7]  
↓  
7th question answer  
Let the 3 consecutive integers be  $x, x+1, x+2$   
 $x + x+1 + x+2 = 60$   
 $3x + 3 = 60$   
 $3x = 57$   
 $x = \frac{57}{3} = 19$

∴ The 3 consecutive integers are :-  
 $x, x+1, x+2 = 19, 19+1, 19+2$

$$\Rightarrow 19, 20, 21$$

A6  
(6th)  
question answer  
Temperature at sunrise =  $1^\circ$  below  
 $= -1^\circ$

Temperature at lunch time =  $+17^\circ$   
Temperature at the end of the day =  
 $-1^\circ + 17^\circ + -4^\circ$   
 $= 16^\circ - 4^\circ$   
 $= 12^\circ$

7  
(7th)  
question answer  
The sum of the least and the greatest of 3 consecutive integers is 60. What are values of the integers.  
(Answer at previous page)

8. Value using distributive property

a)  $-486 \times (-36) + (486) \times (-64)$   
 $-486 \times (\cancel{-36}) - 36 + 64$   
 $-486 \times -100$   
48600

b)  $23789 \times 99 - (23789)$   
 $23789 \times 99 + 23789 \times 1$   
 $23789 \times 99+1$   
 $23789 \times 100$   
2378900

c)  $9269 \times 999$   
 $9269 \times (1000-1)$   
 $9269 \times 1000 - 9269 \times 1$   
 $9269000 - 9269$   
9259731

d)  $6578 \times 105$   
 $6578 \times (100+5)$   
 $6578 \times 100 + 6578 \times 5$   
 $657800 + 32890$   
690690

8  
36/4/23