

P1

Calculation Table for single variable Linear Regression

x	y	xy	x^2	\bar{x}	\bar{y}	\overline{xy}	$(\bar{x})^2$	$\overline{x^2}$
2	35	70	4	$\bar{x} = \frac{\text{sum of all } x}{n}$ $= \frac{32}{7}$ $= 4.57$	$\bar{y} = \frac{\text{sum of } y}{n}$ $= \frac{155}{7}$ $= 22.14$	$\overline{xy} = \frac{\text{sum of } xy}{n}$ $= \frac{1555}{7}$ $= 222.14$	$(\bar{x})^2 = (4.57)^2$ $= 20.885$	$\overline{x^2} = \frac{\text{sum of } x^2}{n}$ $= \frac{164}{7}$ $= 23.43$
4	60	240	16					
5	20	100	25					
3	50	150	9					
6	50	300	36					
5	55	275	25					
7	60	420	49					
$\sum = 32$		1555						
$\bar{y} = 47.14$								
$\bar{x} = 4.57$								

Task 01

$$Y = MX + C$$

$$C = \bar{Y} - M\bar{X}$$

$$M = \frac{\bar{X} \cdot \bar{Y} - \overline{XY}}{(\bar{X})^2 - \overline{X^2}}$$

$$= \frac{215.4298 - 222.14}{20.885 - 23.43}$$

$$= \frac{-6.7102}{-2.545}$$

$$M = 2.6366$$

$$M = 2.6366$$

$$C = \bar{Y} - M\bar{X}$$

$$= 47.14 - (2.6366 \times 4.57)$$

$$= +35.091$$

$$\approx 35.0907$$

$\bar{Y} =$	47.14
$\bar{X} =$	4.57
$\bar{X} \cdot \bar{Y} =$	$(47.14) \times (4.57)$
	215.4298
$\overline{XY} =$	222.14
$(\bar{X})^2 =$	20.885
$\overline{X^2} =$	23.43

Prediction

$$Y = MX + C$$

$$Y = (2.6266 \times 6) + 35.0907$$

$$Y = 50.9103$$

Observed Value	Price (Y)	Weight (X)
35	6	1
40	7	2
45	8	3
50	9	4
55	10	5
60	11	6
65	12	7

MAE = 20

96698

Task 02

p4

$$Y_p = MX + C$$

$$M = 2.6366, C = 35.0907$$

Weight (x)	Price (y) Observed value	Y_p Predicted value	$Y - Y_p$ Residual
2	35	$Y_p = 2.6366 \times 2 + 35.0907$ $= 40.3639$	$35 - 40.3639$ $= -5.3639$
4	60	$Y_p = 2.6366 \times 4 + 35.0907$ $= 45.6371$	14.3629
5	20	$Y_p = 48.2737$	-28.2737
3	50	$Y_p = 42.0005$	6.9995
6	50	$Y_p = 50.9103$	-0.9103
5	55	$Y_p = 48.2737$	6.7263
7	60	$Y_p = 53.5469$	6.4531

TASK 03

Mean Squared Error (MSE)

$$MSE = \frac{1}{n} \sum (Y - Y_p)^2$$

$$n = 7$$

$$\begin{aligned} \sum (Y_i - Y_{pi})^2 &= (-5.3639)^2 \\ &+ (14.3629)^2 + (-28.2737)^2 \\ &+ (6.9995)^2 + (-0.9103)^2 \\ &+ (6.7263)^2 + (6.4531)^2 \end{aligned}$$

$$\begin{aligned} &= 28.77 + 206.29 \\ &+ 799.40 + 48.93 + 0.8286 \\ &+ 45.24 + 41.64 \end{aligned}$$

$$= 1171.0986$$

$$MSE = \frac{1171.0986}{7}$$

$$= 167.2998$$

Mean Absolute Error (MAE)

$$MAE = \frac{1}{n} \sum_{i=1}^n |Y_i - Y_{pi}|$$

$$n = 7$$

$$\sum_{i=1}^n |Y_i - Y_{pi}| = 5.3639$$

$$\begin{aligned} &+ 14.3629 + 28.2737 \\ &+ 6.9995 + 0.9103 \\ &+ 6.7263 + 6.4531 \end{aligned}$$

$$= 69.0897$$

$$MAE = \frac{69.0897}{7}$$

$$= 9.86996$$