```python
class Node:
    """A Huffman Tree Node"""

    def __init__(self, freq_, symbol_, left_=None, right_=None):
        # frequency of symbol
        self.freq = freq_

        # symbol name (character)
        self.symbol = symbol_

        # node left of current node
        self.left = left_

        # node right of current node
        self.right = right_

        # tree direction (0/1)
        self.huff = ""


def print_nodes(node, val=""):
    """Utility function to print huffman codes for all symbols in the newly created Huffman tree"""
    # huffman code for current node
    new_val = val + str(node.huff)

    # if node is not an edge node then traverse inside it
    if node.left:
        print_nodes(node.left, new_val)
    if node.right:
        print_nodes(node.right, new_val)

    # if node is edge node then display its huffman code
    if not node.left and not node.right:
        print(f"{node.symbol} -> {new_val}")


# characters for huffman tree
chars = ["a", "b", "c", "d", "e", "f"]

# frequency of characters
freq = [5, 9, 12, 13, 16, 45]

# list containing huffman tree nodes of characters and frequencies
nodes = [Node(freq[x], chars[x]) for x in range(len(chars))]

while len(nodes) > 1:
    # sort all the nodes in ascending order based on their frequency
    nodes = sorted(nodes, key=lambda x: x.freq)

    # pick 2 smallest nodes
    left = nodes[0]
    right = nodes[1]

    # assign directional value to these nodes
```

```
    left.huff = 0
    right.huff = 1

    # combine the 2 smallest nodes to create new node as their parent
    newNode = Node(left.freq + right.freq, left.symbol + right.symbol, left, right)

    # remove the 2 nodes and add their parent as new node among others
    nodes.remove(left)
    nodes.remove(right)
    nodes.append(newNode)


print("Characters :", f'[{", ".join(chars)}]')
print("Frequency  :", freq, "\n\nHuffman Encoding:")
print_nodes(nodes[0])

"""
OUTPUT:

Characters : [a, b, c, d, e, f]
Frequency  : [5, 9, 12, 13, 16, 45]

Huffman Encoding:
f → 0
c → 100
d → 101
a → 1100
b → 1101
e → 111
"""

```