

Suppose super-concept *TastyFood* (D) contains 4 subsumed concepts with confidence score:

1. Ice-Cream 0.9 ( $C_1$ )
2. Brownie 0.7 ( $C_2$ )
3. Ramen 0.7 ( $C_3$ )
4. Pizza 0.7 ( $C_4$ )

C	O	$\hat{r}_O$	P <sub>1</sub>	$\hat{r}_{P1}$	b <sub>1</sub>	P <sub>2</sub>	$\hat{r}_{P2}$	b <sub>2</sub>
C <sub>1</sub>	4	0.9	4	0.6	0	4	0.7	0
C <sub>2</sub>	3	0.7	3	0.4	0	4	0.7	1
C <sub>3</sub>	3	0.7	3	0.4	0	3	0.4	0
C <sub>4</sub>	3	0.7	4	0.6	1	3	0.4	0
	$\Sigma=13$		$\Sigma=14$			$\Sigma=14$		

**nDCG** is inapplicable in cases where the sum of original rank prediction (13) is less than predicted rank sum. It gives a score greater than 1 which is not correct as it ranges [0,1].

So we use **hDMA** which is explained below.

C- sub-concepts of superconcept D.

O- original rank of subconcepts based on decreasing confidence scores  $\hat{r}_O$ .

$\hat{r}_O$ - original confidence score of relatedness to D.  $P_i$ - predicted ranking based on predicted confidence score  $\hat{r}_{P_i}$ .

$b_i$ - bit vector of XOR operation between O and  $P_i$ .

$$O \oplus P_1 = (0001)_2 = (1)_{10}$$

$$hDMA(O, P_1) = \frac{1}{1+1}$$

$$O \oplus P_2 = (0100)_2 = (4)_{10}$$

$$hDMA(O, P_2) = \frac{4}{4+1}$$

The hDMA method appropriately assigns a higher score to the more deviant rank distribution,  $P_2$ . This is because  $P_2$  exhibits a deviation in the 2nd position, whereas  $P_1$  deviates in the 4th position. Since higher-ranked positions in the ranking table indicate greater importance, the deviation in  $P_2$  is considered more significant.