



Advanced Control System

Term Project

Submitted by:

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Question 1:

Design a Compensator for unity feedback system with open loop transfer function $G(s) = K / (K/(s(s+1)(0.5s + 1)))$ to satisfy the following specifications:

- (i) Velocity error constant $K_v=5$
- (ii) Phase margin =40 degrees.
- (iii) Gain Margin = 10dB

Code:

```
%% Advanced Control System
% Submitted by
% Aniket Kumar
% 200108068
% Group 16
% Question 1
%% Design of Lag Compensator
% Design a Compensator for a unity feedback system with
% open loop transfer function  $G(s)= 1/(s(s+1)(0.5s + 1))$  to satisfy
the
% following specifications:
% (i) velocity error constant  $K_v=5$ ,
% (ii) Phase margin =40 degrees.
% (iii)Gain Margin = 10dB
close all
clear all
clc
% Adjusting the open loop transfer function of  $K_V = 5$ 
% So ,  $G1 = k*G$ 
%  $K_v = \lim(s \rightarrow 0) sG1(s)H(s) = 5$ 
%  $K_v = \lim(s \rightarrow 0) s*K/(s(s+1)(0.5s + 1))*1 = 5$ 
% Therefore  $K_v = K = 5$ 
% Uncompensated Sys =  $5/(s(s+1)(0.5s + 1))$ 
```

```

num1 = [5];
den1 = [0.5 1.5 1 0] ;
disp(['Uncompensated system Transfer function']);
G1 = tf(num1 , den1 ) ;
% printing to console the uncompensated Tf with adjusted Kv
G1
%Extracting the Gm , Pm of G1
figure
grid
[Gm, Pm, w_gm, w_pm] = margin(G1);
margin(G1)
title({"Uncompensated system with gain adjusted Kv=5sec^-
1",sprintf('Phase Margin = %0.4f deg, Gain Margin = %0.4fdB',Pm,
Gm)}))
%% Lag Compensator
phie_req = 40 ;
tolerance = 5;
phie_req = 40 +tolerance ;
% Noting down the W value at 180 - phir_req i.e 180 -45 = 135 from
the
% Bode Plot of G1
w_at_135 = 0.554;
% Noting Down the Gain at W = 0.554 from bode plot of G1
% Gain = 17.5
g_un_w = 17.5;
% We then design a lag compensator and we know that lag compensator
brings down
% the magintude plot by beta such that the phase crossover
frequency
% becomes wc/10.

```

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% Lag Compensator = (sT +1) / (sBT +1 ) where B>1
% we know ,  $20 \log(B) = g_{un\_w}$ 
beta = 10 ^ (17.5/20);
wc_z = w_at_135/10 ;
T = 1/wc_z;
wcp = 1/(beta * T) ;

% Forming the Lag Compensator using the obtained Values
numc = [T 1];
denc = [beta*T 1] ;
GC = tf(numc , denc) ;
disp(['Compensator Transfer function']);
GC
figure
% Displaying the compensator thus obtained
margin(GC)
%% Final Compensated Transfer Function
Geq = G1 * GC;

figure
margin(Geq)

disp(['Compensator Transfer function']);
Geq

%% Ploting step response of compensated and uncompensated system
CloseLoopG1 = feedback(G1*1 ,1) ; %  $H(s) = 1$ 
CloseLoopGeq = feedback(Geq*1,1) ; %  $H(s) = 1$ 
figure

step(CloseLoopGeq)

```

```

title({"Step Response of  Compensated close loop system"})

figure
step(CloseLoopG1)
title({"Step Response of  Uncompensated close loop system"})
%% Ramp Response of Compensated and UnCompensated System

% Define the input signal as a ramp
t = 0:0.1:10;
alpha = 1;
ramp = alpha * t;
% Plotting for Compensated System
figure
plot(t, ramp)
hold on
lsim(CloseLoopGeq, ramp, t)
title({"Ramp Response of Compensated System"})
legend('Ramp signal','Compensated system')

hold off
% Plotting for Uncompensated System
figure
plot(t, ramp)
hold on
lsim(CloseLoopG1, ramp, t)
title({"Ramp Response of Uncompensated System"})
legend('Ramp signal','Uncompensated system')

hold off

```

Question 2:

Design a PID controller, obtain unit step response with MATLAB/ Simulink, and compare the responses of systems.

$$G(s) = 1 / (s) * (s+1) * (s+5)$$

Code:

```
%% Advanced Control System
% Submitted by
% Aniket Kumar
% 200108068
% Group 16
% Question 2 part b
%% Design a PID controller, obtain unit step response with
MATLAB/ Simulink, and compare the responses of systems
%  $G(s) = 1 / (s)(s+1)(s+5)$ 
close all
clear all
clc

num1 = [1];
den1 = [1 6 5 0] ;

G1 = tf(num1 , den1 ) ;
%plotting root locus to calculate the gain and frequency at
which the closed-loop system becomes marginally stable
% (i.e., the gain and frequency at the point where the root
locus intersects the imaginary axis)
```

```

figure(1)
rlocus(G1)

% k = 30;
% w = 2.24;
% Close Loop feedback without controller

k_u = 30; % ultimate gain
w_u = 2.24; %ultimate period
pu = 2* 3.14/w_u ;
%pu = 2pie / w_u

%% Using The Ziegler-Nichols Tuning Rule | Ultimate Gain &
Ultimate Period
kp = k_u/1.7;
ki = kp/(pu/2) ;
kd = kp * (pu/8);

%% pid controller without tuning

PID_CONT1 = pid(kp , ki, kd);
PID_CONT1
open_sys = series(PID_CONT1 , G1) ;
closeSys1 = feedback(open_sys,1) ;

%% pid controller with tuning
% Fix one quantity and change other
% General trend to better the following parameters are listed
below
%% Settling time : Kp -> Small Change, Ki -> Increase, Kd ->
Decrease
%% Rise Time : Kp -> Decrease, Ki -> Decrease, Kd -> Small
Change
%% Overshoot : Kp -> Increase, Ki -> Increase, Kd -> Decrease

```

```
%% SS error : Kp -> Decrease, Ki -> Estimate, Kd -> Small  
Change
```

```
delta1 = 2.8;  
delta2 = 3.1;  
delta3 = 1.5;  
kp = k_u/1.7 - delta3;  
ki = kp/(pu/2) - delta1 ;  
kd = kp * (pu/8) +delta2;  
PID_CONT2 = pid(kp , ki, kd);  
PID_CONT2  
open_sys = series(PID_CONT2 , G1) ;  
closeSys2 = feedback(open_sys,1) ;
```

```
%% Plotting the step response
```

```
figure(2)  
step(closeSys1)  
hold on  
step(closeSys2)  
hold on  
gcl = feedback(G1 , 1) ;  
step(gcl)  
legend('PID without tuning','PID with tuning','Without  
Controller')  
hold off  
%% Details of both the responses  
disp(['Step Response in PID'])  
S1= stepinfo(closeSys1)  
disp(['Step Response in PID further tuned'])  
S = stepinfo(closeSys2)  
%% Thank You %%%%
```