EX 1 THREE-LAYER NEURAL NETWORK FROM SCRATCH

Problem Statement:

Design and implement a three-layer neural network from scratch using Python. Train the network using the backpropagation algorithm with appropriate activation and loss functions. Apply the model to recognize handwritten digits using the MNIST dataset.

Objectives:

- 1. Understand the structure and working of a basic feedforward neural network.
- 2. Implement forward propagation and backpropagation from scratch.
- 3. Use the sigmoid activation function and cross-entropy loss.
- 4. Train the model on the MNIST dataset and evaluate the loss over epochs.
- 5. Visualize training performance and perform predictions on sample images.

Scope:

This experiment demonstrates the core principles behind neural networks and training them using backpropagation. It is foundational for understanding deep learning and how more complex models (like CNNs or Transformers) build upon this architecture.

Tools and Libraries Used:

- 1. Python 3.x
- 2. NumPy
- 3. Matplotlib
- 4. TensorFlow (for dataset loading)
- scikit-learn (OneHotEncoder)

Implementation Steps:

Step 1: Import Necessary Libraries

import numpy as np import matplotlib.pyplot as plt from tensorflow.keras.datasets import mnist from sklearn.preprocessing import OneHotEncoder

Step 2: Load and Preprocess the Dataset

```
(X_train, y_train), (_, _) = mnist.load_data()

X_train = X_train.reshape(-1, 784) / 255.0

encoder = OneHotEncoder(sparse_output=False)

y_train = encoder.fit_transform(y_train.reshape(-1, 1))
```

Step 3: Initialize the Network

```
input_size, hidden_size, output_size = 784, 64, 10
W1 = np.random.randn(input_size, hidden_size) * 0.01
b1 = np.zeros((1, hidden_size))
W2 = np.random.randn(hidden_size, output_size) * 0.01
b2 = np.zeros((1, output_size))
```

Step 4: Define Activation and Loss Functions

```
sigmoid = lambda x: 1 / (1 + np.exp(-x))
sigmoid_deriv = lambda x: x * (1 - x)
loss_fn = lambda y, y_hat: -np.mean(y * np.log(y_hat + 1e-8))
```

Step 5: Train the Model

```
epochs, lr = 10, 0.1
losses = []
for epoch in range(epochs):
  total loss = 0
  for i in range(X_train.shape[o]):
    x = X train[i:i+1]
    y = y_train[i:i+1]
    z_1 = x @ W_1 + b_1
    a1 = sigmoid(z1)
    z2 = a1 @ W2 + b2
    a2 = sigmoid(z2)
    loss = loss_fn(y, a2)
    total loss += loss
    dz2 = a2 - y
    dW_2 = a_1.T @ dz_2
    db2 = dz2
    dz1 = (dz2 @ W2.T) * sigmoid_deriv(a1)
    dW1 = x.T @ dz1
    db1 = dz1
    W_2 = lr * dW_2
    b2 -= lr * db2
    W1 = lr * dW1
    b1 -= lr * db1
  losses.append(total_loss / X_train.shape[o])
  print(f"Epoch {epoch+1}, Loss: {losses[-1]:.4f}")
```

Step 6: Visualize Training Loss

```
plt.plot(losses)
```

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```
plt.title("Training Loss")
plt.xlabel("Epoch")
plt.ylabel("Loss")
plt.grid(True)
plt.show()
```

Step 7: Predict a Sample Digit

```
def predict(img):
    img = img.reshape(1, 784) / 255.0
    a1 = sigmoid(img @ W1 + b1)
    a2 = sigmoid(a1 @ W2 + b2)
    return np.argmax(a2)

idx = 100
plt.imshow(X_train[idx].reshape(28, 28), cmap='gray')
plt.title(f"Prediction: {predict(X_train[idx])}")
plt.axis('off')
plt.show()
```

Output:



