



Data Structures

Topics Covered:

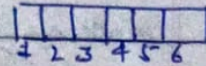
Arrays

Linked-List

Double-Linked list

Stack

Arrays: Contiguous area of memory consisting of equal-size element indexed by contiguous integers

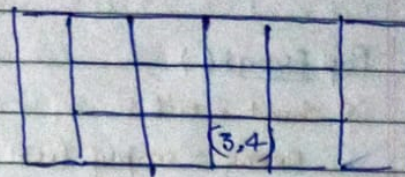


What's Special About Arrays? Constant time access

$$\text{array_addr} + \text{element_size} \times (i - \text{first})$$
 Multi-Dimensional Arrays: - Index

array_addr +

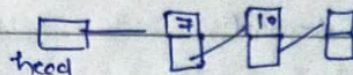
$$\text{elem_size} \times ((3-1) \times 6 + (4-1))$$



Time for Common Operations

	Add	Remove	
Beginning	$O(n)$	$O(n)$	Linear
** End	$O(1)$	$O(1)$	constant
Middle	$O(n)$	$O(n)$	Linear

* Linked List:



Node contains:

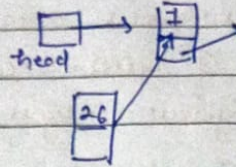
- key
- Pointer: #

- ⇒ PushFront(key) → add to front $O(1)$
- KeyTopFront() → return front item $O(1)$
- PopFront() → remove front item $O(1)$
- PushBack(key) → add to back → $O(n)$ with tail $O(1)$
- KeyTopBack() → return back item → $O(n)$ with tail $O(1)$
- PopBack() → remove back item → $O(n)$
- Boolean find(key) → is key in list? → $O(n)$
- erase(key) → remove key from list → $O(1)$
- AddBefore(Node, key) → add key before → $O(n)$
- AddAfter(Node, key) → add key after → $O(1)$

Pseudo code PushFront (key)

```

node ← new node
node.key ← key
node.next ← head
head ← node
if tail = nil:
    tail ← head
    
```



Pop Front()

```

if head = nil:
    ERROR: empty list
head ← head.next
if head = nil:
    tail ← nil
    
```

Push Back()

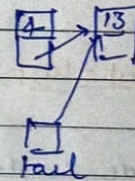
```

node ← new node
node.key ← key
node.next = nil
if tail = nil:
    head ← tail ← node
else:
    tail.next ← node
    tail ← node
    
```

• Pop Back()

```

if head = nil: ERROR: empty list
if head = tail:
    head ← tail ← nil
else:
    p ← head
    while p.next.next ≠ nil:
        p ← p.next
    
```

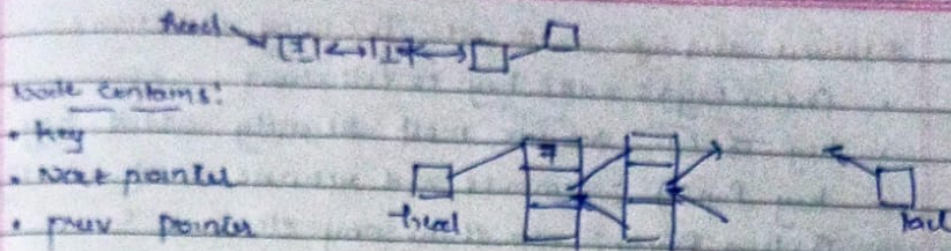


Add After (node, key)

```

node2 ← new node
node2.key ← key
node2.next = node.next
node.next = node2
if tail = node:
    tail ← node2
    
```


Double-linked list:



popback $\rightarrow O(1)$

Push Back (key)

node \leftarrow new node
 node.key \leftarrow key; node.next = nil
 if tail = nil:

head \leftarrow tail \leftarrow node
 node.prev \leftarrow nil

else:

tail.next \leftarrow node
 node.prev \leftarrow tail
 tail \leftarrow node

* Add After (node, key)

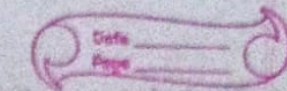
node2 \leftarrow new node
 node2.key \leftarrow key
 node2.next \leftarrow node.next
 node2.prev \leftarrow node
 node.next \leftarrow node2
 if node2.next \neq nil:
 node2.next.prev \leftarrow node2
 if tail = node:
 tail \leftarrow node2

* In Doubly-linked list

PopBack $\rightarrow O(1)$

Add Before (node, key) $\rightarrow O(1)$

Improvement - Pushing single linked list



PopBack()

if head = nil: Error: empty list
 if head = tail:

head \leftarrow tail \leftarrow nil

else:

tail \leftarrow tail.prev
 tail.next \leftarrow nil

Add Before (node, key)

node2 \leftarrow new node
 node2.key \leftarrow key
 node2.next \leftarrow node
 node2.prev \leftarrow node.prev
 node.prev \leftarrow node2

if node2.prev \neq nil:

node2.prev.next \leftarrow node2

if head = node:

head \leftarrow node2

#1 Stacks:

Abstract data type with the following operations

- Push(key): adds key to collection
- key Top(): returns most recently-added key
- key Pop(): removes and returns most recently-added
- Boolean Empty: are there any elements?

Balanced Brackets:

input: A string str consisting of '(', ')', '[', ']', '{', '}' characters
output: Return whether or not the strings parenthesis and square brackets are balanced.

IsBalanced(str)

Stack stack

for char in str:

if char in ['(', '[', '{']:

stack.Push(char)

else:

if stack.Empty(): return false

top ← stack.Pop()

if (top == '[' and char != ']') or
(top == '(' and char != ')'):

return False

return stack.Empty()

Stack Implementation with Array

num Elements: 2 → 3 → 2

a b c | |

push(c)

pop() → c

push(d)

push(e)

some operations: