

Day_2: DSA

Day-2 Leetcode 1358

given: a string s - only characters a, b and c
 → Return the number of substrings containing at least one occurrence of all these characters a, b and c

$s = b b a c b a$ → 3rd substring are possible. Total → 9

1st 2nd 3rd

Try all substrings
 $cnt = 0$
 for ($i = 0 \rightarrow n$)
 {
 $hash[i] = \{0\}$
 for ($j = i \rightarrow n$)
 {
 $hash[s[j]] = 1$;
 if ($hash[0] + hash[1] + hash[2] == 3$)
 $cnt = cnt + 1$;
 }
 }
 print (cnt);

Brute force
 $T.C = O(N^2)$
 $S.C = O(1)$

↓ optimization
 $cnt = cnt + (n - j)$; break;

Sliding window.
 $s = b b a c b a$
 → minimum window with every character there is a substring that ends.

fun(s)
 {
 $lastseen[3] = \{-1, -1, -1\}$;
 $cnt = 0$
 for ($i = 0 \rightarrow n$)
 {
 $lastseen[s[i] - 'a'] = i$;
 if ($lastseen[0] != -1 \& \& lastseen[1] != -1 \& \& lastseen[2] != -1$)
 $cnt = cnt + (1 + \min(lastseen[0], lastseen[1], lastseen[2]))$;
 }
 }
 return cnt ;

$T.C \rightarrow O(N)$
 $S.C \rightarrow O(1)$

• Frog Jump with K -distance

- In this frog can jump K steps at each time.
- pseudocode for simple frog jump

```

f(ind, height[]) {
    if (ind == 0) return 0
    jumpOne = f(ind-1, height) + abs(height[ind] - height[ind-1])
    if (ind > 1)
        jumpTwo = f(ind-2, height) + abs(height[ind] - height[ind-2])
    return min(jumpOne, jumpTwo)
}
    
```

- In this we are taking single step or two step at a time

• Now we need to try K -option in order to try out all possible ways.

Final pseudocode.

```

f(ind, height[]) {
    if (ind == 0) return 0
    mmSteps = INT_MAX
    for (j = 1; j <= K; j++) {
        if (ind - j >= 0) {
            jump = f(ind - j, height) + abs(height[ind] - height[ind - j])
            mmSteps = min(jump, mmSteps)
        }
    }
    return mmSteps
}
    
```

This is recursive solution.

Now convert into dp sol.

- Create a $dp[n]$ array initialized to -1
- whenever we want to find the answer of a particular value (say n) we first check whether the answer is already calculated using the dp array (i.e. $dp[n] != -1$)
If yes simply return the value from the dp array
- If not, we are finding the answer for the given value for the first time, we will use the recursive solution as usual but before returning the function, we will set $dp[n]$ to the solution we got.

code: ^{solveUtil}

```

def solution (end, height, dp, k):
    # Base case: If we are at the beginning (index 0), no cost is needed
    if end == 0:
        return 0
    # If the result is already calculated
    if dp[end] != -1:
        return dp[end]
    # Loop to try all possible jump from '1' to 'k'
    for j in range(1, k+1):
        # Ensure that we do not jump beyond the beginning of the array
        if end - j >= 0:
            jump = solveUtil(end - j, height, dp, k) + abs(height[end] - height[end - j])
            mmsteps = min(jump, mmsteps)
    # Third step
    dp[end] = mmsteps
    return dp[end]

```

TC: $O(N * K)$
 \approx
 $O(N)$

mmsteps = sys.maxsize

Tabulation Approach

```

input sys
def solve_util(n, height, dp, k):
    dp[0] = 0
    for i in range(1, n):
        mmsteps = sys.maxsize
        for j in range(1, k+1):
            if i - j >= 0:
                # calculate the no. of steps to reach current position from previous position
                jump = dp[i - j] + abs(height[i] - height[i - j])
                mmsteps = min(jump, mmsteps)
        dp[i] = mmsteps
    # Return the mini steps needed to reach the last position
    return dp[n-1]

```


Problem: Maximum Sum of Non-adjacent Element

ex 1 2 3 9 \rightarrow sum = 11

(Let's try out all subsequence with the given constraint)
 \rightarrow pick the subsequence with maximum

```
f(ind) {
    dp[ind] = -1
    if (ind == 0) return a[ind];
    if (ind < 0) return 0;
    if (dp[ind] != -1) return dp[ind];
    pick = a[ind] + f(ind-2);
    not pick = 0 + f(ind-1);
    dp[ind] = max(pick, not pick);
    return dp[ind];
}
```

Recursion
Sol.

$$T.C = O(2^n)$$

\rightarrow This is dp solution

$$T.C \rightarrow O(N)$$

$$S.C \rightarrow O(N) + O(N)$$

Stack space Array space

Tabulation: \rightarrow Bottom-Up

```
dp[0] = 0
dp[1] = a[0]; // Base case
int neg = 0; // Base case
```

```
for (i = 1; i < n; i++) {
    take = a[i] + dp[i-2];
    not take = 0 + dp[i-1];
    dp[i] = max(take, not take);
}
```

if (i > 1) take += dp[i-2];
 \rightarrow It can reach to negative index

$$T.C = O(N)$$

$$S.C = O(N)$$

Space Optimisation

```
prev = a[0];
prev2 = 0;
for (i = 1; i < n; i++) {
    take = a[i] + prev2;
    not take = 0 + prev;
    cur = max(take, not take);
    prev2 = prev;
    prev = cur;
}
```

$$T.C = O(N)$$

$$S.C = O(1)$$