

$$a) \quad AC \rightarrow BD \Rightarrow AC \rightarrow B \quad \left. \begin{array}{l} \\ B \rightarrow E \end{array} \right\} \Rightarrow AC \rightarrow E.$$

$$b). \quad (A)^+ = \{A\}, \quad (AC)^+ = \{A, AC, B, D, E\}.$$

$$c) \quad F \Rightarrow \{AC \rightarrow BD, B \rightarrow CE, C \rightarrow D\} \\ \Rightarrow \{AC \rightarrow B, B \rightarrow CE, C \rightarrow D\}$$

$$\therefore F_c = \{AC \rightarrow B, B \rightarrow CE, C \rightarrow D\}$$

$$d) \quad X = \{A\} \quad Y = \{B, C\}$$

$$X^+ \neq U, \quad (AB)^+ = \{A, B, C, D, E\} = U$$

$$(AC)^+ = \{A, B, C, D, E\} = U$$

$\therefore AB, AC$ are candidate keys.

because of FD $B \rightarrow E$, R is only in 1st normal form

~~AB~~

e) decompose into (ABL, BLE, CD) ~~AB~~

f)

	A	B	C	D	E
R_1	A	B	C	X_{14}	X_{15}
R_2	X_{21}	B	C	X_{24}	E
R_3	X_{31}	X_{32}	C	D	X_{35}

\Rightarrow

	A	B	C	D	E
R_1	A	B	C	D	E
R_2	X_{21}	B	C	D	E
R_3	X_{31}	X_{32}	C	D	X_{35}

so it is
lossless-join.
Since it's in
3rd NF,
it's also dependency
preserving