Deep Dive into Neural Networks

Agenda

Discussion about ANN and it's components

Feedforward neural network

Loss function

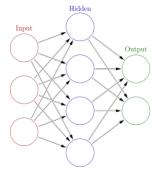
Gradient Descent and Backpropagation

Hyperparameter discussion

Write our first ANN

Neural Network

https://www.youtube.com/watch?v=aircAruvnKk&list=PLZHQ0b0WTQDNU6R1_67000Dx_ZCJB-3pi



This is the basic structure of a neural network

Each circle represents a node

Each arrow represents a connection called weights which gives an idea how strong the connection is

Input nodes pass the input data

So if a dataset has n input features it will have n input nodes

```
In [138]:
```

```
df = pd.read_csv('../../data/training_dataset_500.csv')
df[df['House']==1]
```

Out[138]:

| | ID | Label | House | Year | Month | Temperature | Daylight | EnergyProduction | |
|----|----|-------|-------|------|-------|-------------|----------|------------------|--|
| 0 | 0 | 0 | 1 | 2011 | 7 | 26.2 | 178.9 | 740 | |
| 1 | 1 | 1 | 1 | 2011 | 8 | 25.8 | 169.7 | 731 | |
| 2 | 2 | 2 | 1 | 2011 | 9 | 22.8 | 170.2 | 694 | |
| 3 | 3 | 3 | 1 | 2011 | 10 | 16.4 | 169.1 | 688 | |
| 4 | 4 | 4 | 1 | 2011 | 11 | 11.4 | 169.1 | 650 | |
| 5 | 5 | 5 | 1 | 2011 | 12 | 4.2 | 199.5 | 763 | |
| 6 | 6 | 6 | 1 | 2012 | 1 | 1.8 | 203.1 | 765 | |
| 7 | 7 | 7 | 1 | 2012 | 2 | 2.8 | 178.2 | 706 | |
| 8 | 8 | 8 | 1 | 2012 | 3 | 6.7 | 172.7 | 788 | |
| 9 | 9 | 9 | 1 | 2012 | 4 | 12.6 | 182.2 | 831 | |
| 10 | 10 | 10 | 1 | 2012 | 5 | 17.6 | 214.2 | 955 | |
| 11 | 11 | 11 | 1 | 2012 | 6 | 20.8 | 143.0 | 837 | |
| | | | | | | | 1 | | |

F1, F2, F3, F4, F5 -> F6

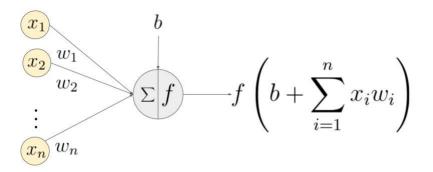
So in case of a dataframe like this we will have 3 input nodes

Output nodes represent the number of values a target node can take $% \left(1\right) =\left(1\right) \left(1\right)$

So it it's a iris classification problem we can have 4 outputs since there are 4 categories of iris

Input nodes and output nodes are fixed but the number of hidden layers and hidden nodes is a hyperparam

Weights and bias



An example of a neuron showing the input ($x_1 - x_n$), their corresponding weights (w₁ - w_n), a bias (b) and the activation function f applied to the weighted sum of the inputs.

Multi-layered neural network Input layer Hidden layers Output layer Input 1 Output 1 Input 2 Output n Input n

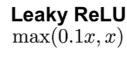
Used to introduce non-linearity

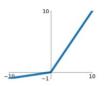
Activation Functions

Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$







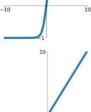
tanh

tanh(x)



ReLU

 $\max(0, x)$



Maxout

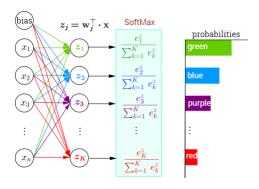
 $\max(w_1^T x + b_1, w_2^T x + b_2)$

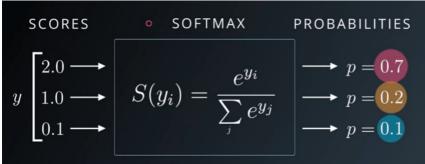
ELU

$$\begin{cases} x & x \ge 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

Activation function does two things :-

Softmax function





 $S(2) = e^2/(e^2+e^1+e^0.1)$

S(1) = e^1/(e^2+e^1+e^0.1)

 $S(0.1) = e^0.1/(e^2+e^1+e^0.1)$

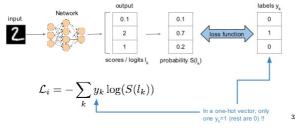
S(2) + S(1) + S(0.1) = 1

Linear -> MSE

Logistic -> Cross-Entropy

Cross-entropy loss

Cross-entropy loss (2)



L = - ((0 * log(0.1)) + (1 * log(0.7) + (0 * log(0.2)))

Why cross-entropy and not mean square loss

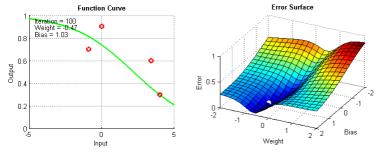
Gradient Descent

Neural network does forward propagation to give a certain output

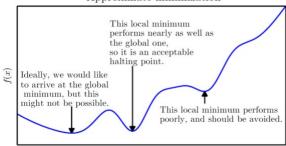
We then see how much the output differs from expect output using the cost/loss function $% \left(1\right) =\left(1\right) \left(1\right)$

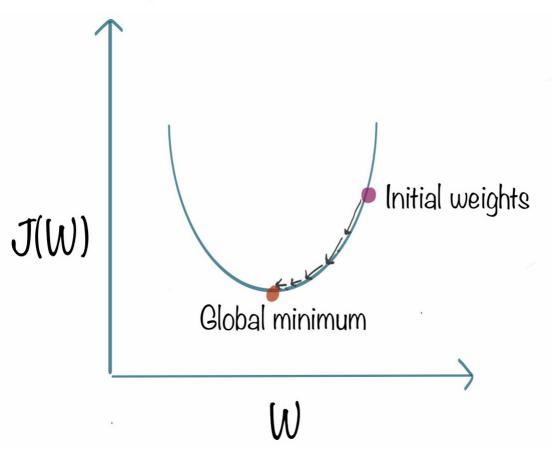
Our goal is to reduce the loss function and get the global minima using the weights and biases $\frac{1}{2}$

To do this start with random set of weights and gradually nudge them to reach the local minima $\,$



Approximate minimization





https://www.youtube.com/watch?v=IHZwWFHWa-w&list=PLZHQ0b0WTQDNU6R1_67000Dx_ZCJB-3pi&index=2

Gradient Descent

Remember that the general form of gradient descent is:

Repeat {
$$\theta_{j} := \theta_{j} - \alpha \frac{\partial}{\partial \theta_{j}} J(\theta)$$
}

We can work out the derivative part using calculus to get:

Repeat {
$$\theta_j := \theta_j - \frac{\alpha}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$
}

Backpropagation

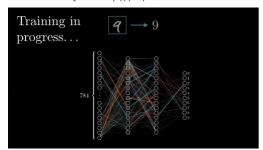
This is the output we want

To achieve this we need to push up the activation at 2 to 1 and push the rest down to 0

3 ways to change to output

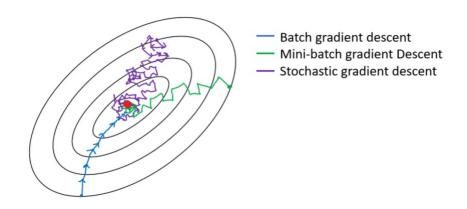
- Change bias
 Change weights
 Change activations

Cumulative sum of changes. Recursively apply the process and move backwards and hence backpropagation



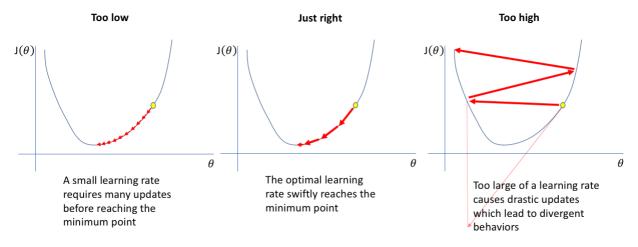
Training concepts

Batch is a set of data points



Learning rate

Pace at which you would want to train



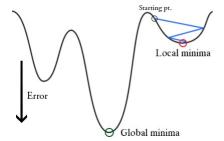
Batch size is number of data points present in a single training step i.e iteration

An epoch is when all the examples in the training dataset is visited once

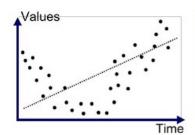
Difference between neural networks and other things you saw until now

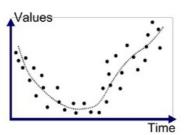
Neural networks global minima might look like below, so you need to train more to reach global minima

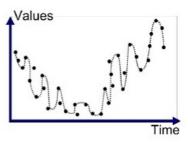
If batch gd is used can get stuck in local minima hence mini batch gd is used



Underfitting and overfitting







Underfitted

Good Fit/Robust

Overfitted

Underfitting is battled by increasing the capacity of network

Overfitting is battled by adding regularisation techniques

28x28

Input normalization

Keep pixel values between 0-1

Divide every pixel value by 255

Training and Test dataset

We divide the dataset into train and test to validate if the model is not overfitting

