

## Flow-Velocity function from IDM at equilibrium:

Setting up the equations and constants.

$$\text{In[1]:= } s_{e_{v_0, s_0, T}}[v_-] = \frac{s_0 + v \cdot T}{\left(1 - \left(\frac{v}{v_0}\right)^4\right)^{0.5}}$$

$$\text{Out[1]:= } \frac{s_0 + T v}{\left(1 - \frac{v^4}{v_0^4}\right)^{0.5}}$$

$$\text{In[2]:= } 1 = 5$$

$$\text{Out[2]:= } 5$$

$$\text{In[5]:= } Q_{s_0, v_0, T}[v_-] = \frac{v}{\frac{s_0 + v \cdot T}{\left(1 - \left(\frac{v}{v_0}\right)^4\right)^{0.5}} + 1}$$

Set: Tag Times in  $Q_{s_0, v_0, T}[v_-]$  is Protected.

$$\text{Out[5]:= } \frac{v}{5 + \frac{s_0 + T v}{\left(1 - \frac{v^4}{v_0^4}\right)^{0.5}}}$$

Calculating the derivatives:

$$dQ_{ds_0, v_0, s_0, T}[v_-] = \text{Simplify}\left[\partial_{s_0} \frac{v}{5 + \frac{s_0 + T v}{\left(1 - \frac{v^4}{v_0^4}\right)^{0.5}}}\right]$$

$$\text{Out[12]:= } -\frac{v \left(1 - \frac{v^4}{v_0^4}\right)^{0.5}}{\left(s_0 + T v + 5 \left(1 - \frac{v^4}{v_0^4}\right)^{0.5}\right)^2}$$

$$\text{In[10]:= } dQ_{dv_0} = \text{Simplify}\left[\partial_{v_0} \frac{v}{5 + \frac{s_0 + T v}{\left(1 - \frac{v^4}{v_0^4}\right)^{0.5}}}\right]$$

$$\text{Out[10]:= } \left(2 \cdot v^5 (s_0 + T v)\right) / \left(\left(s_0 + T v + 5 \cdot \left(1 - \frac{v^4}{v_0^4}\right)^{0.5}\right)^2 \left(1 - \frac{v^4}{v_0^4}\right)^{0.5} v_0^5\right)$$

$$\text{In[11]:= } dQ_{dT} = \text{Simplify}\left[\partial_T \frac{v}{5 + \frac{s_0 + T v}{\left(1 - \frac{v^4}{v_0^4}\right)^{0.5}}}\right]$$

$$\text{Out[11]:= } -\frac{v^2 \left(1 - \frac{v^4}{v_0^4}\right)^{0.5}}{\left(s_0 + T v + 5 \left(1 - \frac{v^4}{v_0^4}\right)^{0.5}\right)^2}$$

Plotting the graphs for the partial derivative of Q wrt to  $s_0$ .

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In[13]:= Plot[  
  Evaluate@Table[dQds0v0,s0,T[v], {v0, 3, 30, 3}, {s0, 0, 5, 0.5}, {T, 1, 3, 0.5}], {v, 0, 30}]
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