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Assignment 3

Mondedla Anil

Download all python codes from

https://github.com/AnilMondedla/Python/ Assignment_3

and latex-tikz codes from

https://github.com/AnilMondedla/Python/ Assignment_3

1 Problem

2.5. Check whether

$$\begin{pmatrix} 5 \\ -2 \end{pmatrix}, \begin{pmatrix} 6 \\ 4 \end{pmatrix}, \begin{pmatrix} 7 \\ -2 \end{pmatrix}$$

are the vertices of an isosceles triangle.

2 Solution

Given vertices are

$$\mathbf{A} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 6 \\ 4 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 7 \\ -2 \end{pmatrix} \tag{2.0.1}$$

In an isosceles triangle length of two sides will be equal

The direction vectors of AB,BC and CA are

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} 1 \\ 6 \end{pmatrix} \tag{2.0.2}$$

$$\mathbf{C} - \mathbf{B} = \begin{pmatrix} 1 \\ -6 \end{pmatrix} \tag{2.0.3}$$

$$\mathbf{A} - \mathbf{C} = \begin{pmatrix} -2\\0 \end{pmatrix} \tag{2.0.4}$$

$$|AB| = \sqrt{(1)^2 + (6)^2}$$
 (2.0.5)

$$=\sqrt{37}$$
 (2.0.6)

$$|BC| = \sqrt{(1)^2 + (-6)^2}$$
 (2.0.7)

$$=\sqrt{37}$$
 (2.0.8)

$$|CA| = \sqrt{\left(-2\right)^2}$$
 (2.0.9)

$$= 2$$
 (2.0.10)

Sides AB and BC are equal. Hence the given points are the vertices of isosceles triangle.

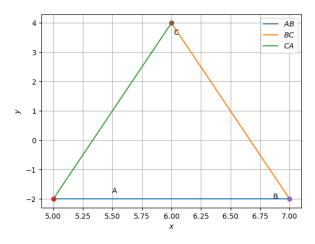


Fig. 0: triangle