Assignment 3

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Download all python codes from

https://github.com/AnilMondedla/Python/ Assignment_3

and latex-tikz codes from

https://github.com/AnilMondedla/Python/ Assignment_3

1 Problem

2.5. Check whether

$$\begin{pmatrix} 5 \\ -2 \end{pmatrix}, \begin{pmatrix} 6 \\ 4 \end{pmatrix}, \begin{pmatrix} 7 \\ -2 \end{pmatrix}$$

are the vertices of an isosceles triangle.

2 Solution

Given vertices are

$$\mathbf{A} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 6 \\ 4 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 7 \\ -2 \end{pmatrix} \tag{2.0.1}$$

In an isosceles triangle length of two sides will be equal

OA vector =
$$(5i - 2j)$$
 vector $(2.0.2)$

OB vector =
$$(6i + 4j)$$
 vector $(2.0.3)$

OC vector =
$$(7i - 2j)$$
 vector $(2.0.4)$

$$AB \text{ vector} = OB - OA$$
 (2.0.5)

$$= (6i + 4j) - (5i - 2j)$$
 (2.0.6)

$$= (i + 6j)$$
 vector (2.0.7)

$$|AB| = \sqrt{(1)^2 + (6)^2}$$
 (2.0.8)

$$=\sqrt{37}$$
 (2.0.9)

$$BC \text{ vector} = OC - OB$$
 (2.0.10)

$$= (7i - 2j) - (6i + 4j) \tag{2.0.11}$$

$$= (i - 6j)$$
 vector (2.0.12)

$$|BC| = \sqrt{(1)^2 + (-6)^2}$$
 (2.0.13)

$$=\sqrt{37}$$
 (2.0.14)

$$CA \ vector = OA - OC$$
 (2.0.15)

$$= (5i - 2j) - (7i - 2j) \tag{2.0.16}$$

$$= (-2i)$$
 vector (2.0.17)

$$|CA| = \sqrt{\left(-2\right)^2}$$
 (2.0.18)

$$= 2$$
 (2.0.19)

Sides AB and BC are equal. Hence the given points are the vertices of isosceles triangle.

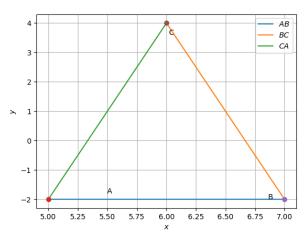


Fig. 0: triangle