Assignment 6

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Find Python Codes from below link

https://github.com/AnilMondedla/Python/ Assignment_6

and latex-tikz codes from

https://github.com/AnilMondedla/Python/ Assignment_6

1 Examples 1

1.1 Question 13

Prove that the points (2,-2),(8,4),(5,7), and (-1,1) are at the angular points of a rectangle.

1.2 Solution

$$\mathbf{A} = \begin{pmatrix} 2 \\ -2 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 8 \\ 4 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 5 \\ 7 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} -1 \\ 1 \end{pmatrix} \quad (1.2.1)$$

Direction vector of A and B

$$\mathbf{m_1} = \begin{pmatrix} 2 \\ -2 \end{pmatrix} - \begin{pmatrix} 8 \\ 4 \end{pmatrix} = \begin{pmatrix} -6 \\ -6 \end{pmatrix}$$
 (1.2.2)

Direction vector of B and C

$$\mathbf{m_2} = \begin{pmatrix} 8\\4 \end{pmatrix} - \begin{pmatrix} 5\\7 \end{pmatrix} = \begin{pmatrix} 3\\-3 \end{pmatrix} \tag{1.2.3}$$

Direction vector of C and D

$$\mathbf{m_3} = \begin{pmatrix} 5 \\ 7 \end{pmatrix} - \begin{pmatrix} -1 \\ 1 \end{pmatrix} = \begin{pmatrix} 6 \\ 6 \end{pmatrix} \tag{1.2.4}$$

Direction vector of D and A

$$\mathbf{m_4} = \begin{pmatrix} -1\\1 \end{pmatrix} - \begin{pmatrix} 2\\-2 \end{pmatrix} = \begin{pmatrix} -3\\3 \end{pmatrix} \tag{1.2.5}$$

Here,

These direction vectors are parallel

$$\mathbf{m_1} = k\mathbf{m_3} \qquad (1.2.6)$$

These direction vectors are parallel

$$\mathbf{m_2} = k\mathbf{m_4} \qquad (1.2.7)$$

For a rectangle

$$(\mathbf{m_1})^{\mathsf{T}}\mathbf{m_2} = 0 \tag{1.2.8}$$

$$\begin{pmatrix} -6 \\ -6 \end{pmatrix}^{\mathsf{T}} \begin{pmatrix} 3 \\ -3 \end{pmatrix} = 0 \tag{1.2.9}$$

$$(-6 -6)\begin{pmatrix} 3 \\ -3 \end{pmatrix} = 0$$
 (1.2.10)
-18 + 18 = 0
0 = 0

Hence, given points A,B,C and D are the Vector points of a rectangle.

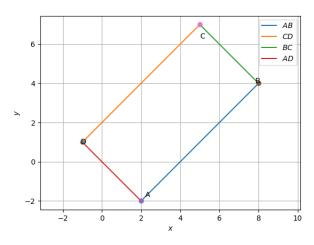


Fig. 0