

Social Networks: Assignment #1

Due on Monday, December 15, 2025

Dr. Masoud Asadpour 15:00am

Ali Dashtbozorg 810104302

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Question 1

Distances and Neighbors

(a) Consider the below network.

For each of the following scenarios, indicate which node would be the best choice, giving reasons:

1. The mayor wants to install a radio broadcast station so that, in a crisis, a single nationwide message can reach all areas. The goal is that every node's distance to the station (independently of other nodes) is as small as possible –in other words, the maximum distance from any node to the station should be minimized.

To determine the optimal node for placing the broadcast station, we use **closeness centrality**, which measures how close a node is on average to all other nodes in the graph. By choosing the node with the highest closeness centrality, we ensure that the station can reach all other nodes as quickly as possible on average.

The formula for closeness centrality of a node v is:

$$C(v) = \frac{n - 1}{\sum_{u \in V} d(v, u)}$$

where $d(v, u)$ is the shortest-path distance between nodes v and u , and n is the total number of nodes.

For our 15-node graph, the closeness centrality values are:

$$\begin{bmatrix} 0.4667 & 0.4667 & 0.4667 & 0.4 & 0.4516 \\ 0.4516 & 0.4667 & 0.4242 & 0.4516 & 0.4375 \\ 0.4118 & 0.4 & 0.5185 & 0.3684 & 0.2745 \end{bmatrix}$$

Node $i = 13$ (value 0.5185) has the highest closeness centrality, so we choose it as the location for the broadcast station to ensure efficient nationwide coverage.

2. Two stores have decided to open new branches in the city. Each person (node) buys from the nearest store. If a person is at equal distance from both stores, their purchases are split equally between them. First, select the best node to open store A, then determine the best location for store B given that choice.

From the closeness centrality analysis, we know that node 13 has the highest value, so it is the best choice for opening store A. Given store A at node 13, the nodes that would maximize the number of customers for store B are those with the highest customer counts. In this case, nodes 1, 3, 7, and 8 each attract 7.0 customers, making them all equally good candidates for store B.

The number of customers each node would get if store A is at node 13 is shown

below, with the best candidates for store B highlighted in bold:

1	7.0
2	6.0
3	7.0
4	6.5
5	6.5
6	5.5
7	7.0
8	7.0
9	6.5
10	5.0
11	5.5
12	6.5
14	2.0
15	1.5

Therefore, the recommended locations are: store A at node 13, and store B at any of nodes 1, 3, 7, or 8.