

SUBJECT: MATHEMATICS

MAX. MARKS : 40

CLASS : IX

DURATION : 1½ hrs

**General Instructions:**

- All questions are compulsory.
- This question paper contains 20 questions divided into five Sections A, B, C, D and E.
- Section A comprises of 10 MCQs of 1 mark each. Section B comprises of 4 questions of 2 marks each. Section C comprises of 3 questions of 3 marks each. Section D comprises of 1 question of 5 marks each and Section E comprises of 2 Case Study Based Questions of 4 marks each.
- There is no overall choice.
- Use of Calculators is not permitted

**SECTION – A**

Questions 1 to 10 carry 1 mark each.

1. If  $\triangle ACB \cong \triangle EDF$ , then which of the following equations is/are true?

(I)  $AC = ED$ (II)  $\angle C = \angle F$ (III)  $AB = EF$ 

(a) Only (I)

(b) (I) and (III)

(c) (II) and (III)

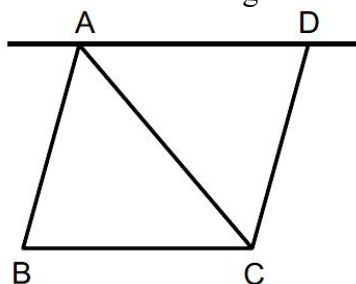
(d) All of these

Ans. (b) (I) and (III)

Since,  $\triangle ACB \cong \triangle EDF$ . $\therefore AC = ED$ ,  $CB = DF$  and  $AB = EF$ And  $\angle A = \angle E$ ,  $\angle C = \angle D$  and  $\angle B = \angle F$ 

Therefore, equations (I) and (III) are true.

2. In a triangle (as shown in fig).  $AB = CD$ ,  $AD = BC$  and  $AC$  is the angle bisector of  $\angle A$ , then which among the following conditions is true for congruence of  $\triangle ABC$  and  $\triangle CDA$  by SAS rule?

(a)  $\angle A = \angle D$ (b)  $\angle B = \angle A$ (c)  $\angle B = \angle D$ (d)  $\angle C = \angle A$ Ans. (c)  $\angle B = \angle D$ As In  $\triangle ABC$  and  $\triangle CDA$ ,  $AB = CD$  and  $AD = BC$ 

For SAS Rule, if two sides and the included angle of one triangle are equal to the two sides and the included angle of the other triangle, then triangles are congruent.

Therefore, For  $\triangle ABC \cong \triangle CDA$ by SAS,  $\angle B$  must be equal to  $\angle D$ 

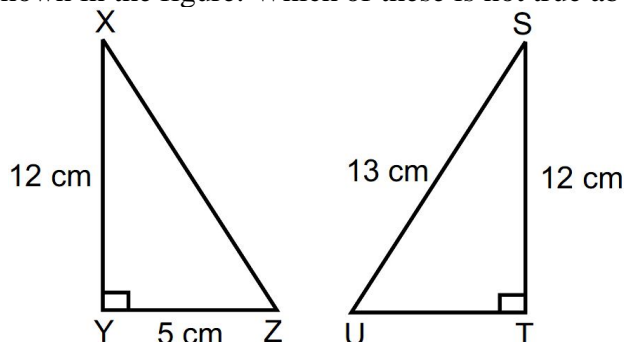
3. If  $AB = QR$ ,  $BC = PR$  and  $CA = PQ$  in  $\triangle ABC$  and  $\triangle PQR$ , then:

(a)  $\triangle ABC \cong \triangle PQR$ (b)  $\triangle CBA \cong \triangle PRQ$ (c)  $\triangle BAC \cong \triangle RPQ$ (d)  $\triangle BCA \cong \triangle PQR$ Ans. (b)  $\triangle CBA \cong \triangle PRQ$ According to the question,  $AB = QR$ ,  $BC = PR$  and  $CA = PQ$ Since,  $AB = QR$ ,  $BC = PR$  and  $CA = PQ$ 

We can say that, A corresponds to Q, B corresponds to R, C corresponds to P.

Hence,  $\triangle CBA \cong \triangle PRQ$

4. Consider the triangles shown in the figure. Which of these is not true about the given triangles?



- (a)  $\triangle XYZ \cong \triangle STU$  (by SSS congruence rule)  
 (b)  $\triangle XYZ \cong \triangle STU$  (by RHS congruence rule)  
 (c)  $\triangle XYZ \cong \triangle STU$  (by ASA congruence rule)  
 (d)  $\triangle XYZ \cong \triangle STU$  (by SAS congruence rule)

Ans. (c)  $\triangle XYZ \cong \triangle STU$  [By ASA congruence rule]

In  $\triangle XYZ$ ,  $XZ^2 = XY^2 + YZ^2$

$$\Rightarrow XZ^2 = (12)^2 + (5)^2$$

$$\Rightarrow XZ^2 = 144 + 25 \Rightarrow XZ^2 = 169 \Rightarrow XZ = 13 \text{ cm}$$

Therefore,  $\triangle XYZ \cong \triangle STU$  [By SSS congruence rule]

Now, In  $\triangle XYZ$  and  $\triangle STU$ ,

$$\angle Y = \angle T \text{ [Right angles]}$$

Hypotenuse  $XZ =$  Hypotenuse  $SU$

Hypotenuse  $XZ =$  Hypotenuse  $SU = 13 \text{ cm}$

$$XY = ST = 12 \text{ cm}$$

Therefore,  $\triangle XYZ \cong \triangle STU$  [By RHS congruence rule]

Then,  $YZ = UT = 5 \text{ cm}$  [By CPCT]

$$\therefore XY = ST, YZ = UT \text{ and } XZ = SU$$

And  $\angle Y = \angle T$

Here,  $\triangle XYZ \cong \triangle STU$

By SSS, RHS and SAS congruence rules, but as only one angle is known, ASA congruence rule is not applicable here.

5. If  $\triangle ABC \cong \triangle PQR$  and  $\triangle ABC$  is not congruent to  $\triangle RPQ$ , then which of the following is not true?

- (a)  $BC = PQ$                       (b)  $AC = PR$                       (c)  $QR = BC$                       (d)  $AB = PQ$

Ans. (a)  $BC = PQ$

Given,  $\triangle ABC \cong \triangle PQR$

Thus, the corresponding sides are equal

Hence,  $AB = PQ$ ,  $BC = QR$  and  $AC = PR$

Therefore,  $BC = PQ$  is not true for the triangles.

6.  $\triangle LMN$  is an isosceles triangle such the  $LM = LN$  and  $\angle N = 65^\circ$ . The value of  $\angle L$  is:

- (a)  $\angle L = 55^\circ$                       (b)  $\angle L = 45^\circ$                       (c)  $\angle L = 50^\circ$                       (d)  $\angle L = 65^\circ$

Ans. (c)  $\angle L = 50^\circ$

$\triangle LMN$  is an isosceles triangle.

$LM = LN$  [Given]

$\angle N = \angle M$  [ $\because$  Angles opposite to equal sides are equal]

$$\therefore \angle M = 65^\circ$$

$$\angle L + \angle M + \angle N = 180^\circ \text{ [}\because \text{ Angle sum property of a triangle]}$$

$$\Rightarrow \angle L + 65^\circ + 65^\circ = 180^\circ$$

$$\Rightarrow \angle L + 130^\circ = 180^\circ$$

$$\Rightarrow \angle L = 180^\circ - 130^\circ \Rightarrow \angle L = 50^\circ$$

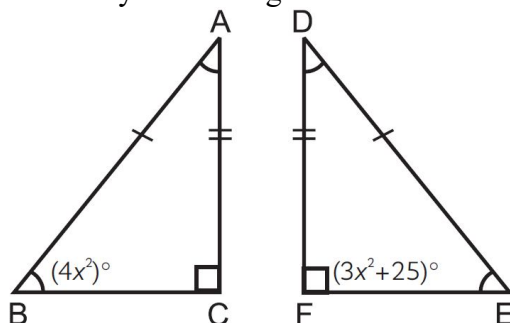
7. Ritish wants to prove that  $\triangle FGH \cong \triangle JKL$  using SAS rule. He knows that  $FG = JK$  and  $FH = JL$ . What additional piece of information does he need?

(a)  $\angle F = \angle J$                       (b)  $\angle H = \angle L$                       (c)  $\angle G = \angle K$                       (d)  $\angle F = \angle G$

Ans. (a)  $\angle F = \angle J$

We know for SAS, if two sides and the included angle of one triangle are equal to the two sides and the included angle of the other triangle, then the triangles are congruent. So,  $\angle F = \angle J$

8. In the given figure  $\triangle ABC \cong \triangle DEF$  by AAA congruence rule. The value of  $\angle x$  is:



(a)  $75^\circ$                       (b)  $105^\circ$                       (c)  $125^\circ$                       (d)  $5^\circ$

Ans. (d)  $5^\circ$

In  $\triangle ABC$  and  $\triangle DEF$ ,  $\angle C = \angle F$

$AB = DE$

$\therefore AC = DF$

$\triangle ABC \cong \triangle DEF$  [By RHS rule]

$\angle B = \angle E$  [By CPCT]

$\Rightarrow (4x^2)^\circ = (3x^2 + 25)^\circ$

$\Rightarrow x^2 = 25 \Rightarrow x = 5^\circ$

In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices.

- (a) Both A and R are true and R is the correct explanation of A.  
 (b) Both A and R are true but R is not the correct explanation of A.  
 (c) A is true but R is false.  
 (d) A is false but R is true.

9. **Assertion (A):** In  $\triangle ABC$  and  $\triangle PQR$ ,  $AB = PQ$ ,  $AC = PR$  and  $\angle BAC = \angle QPR$ ,  $\triangle ABC \cong \triangle PQR$ .

**Reason (R):** Both the triangles are congruent by SSS congruence.

Ans. (c) A is true but R is false.

In  $\triangle ABC$  and  $\triangle PQR$ ,

$AB = PQ$  (given)

$AC = PR$  (given)

$\angle BAC = \angle QPR$

$\therefore \triangle ABC \cong \triangle PQR$  (By SAS Rule)

$\therefore$  Assertion is true.

In case of reason (R): The reason is false as the triangles are congruent by SAS and not SSS.

10. **Assertion (A):** Each angle of an equilateral triangle is  $60^\circ$ .

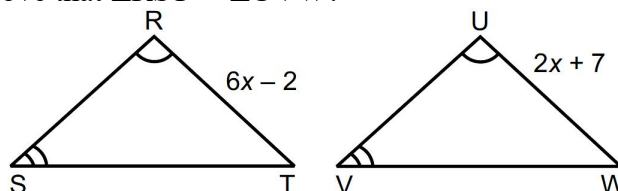
**Reason (R):** Angles opposite to equal sides of a triangle are equal.

Ans. (a) Both A and R are true and R is the correct explanation of A.

## SECTION – B

Questions 11 to 14 carry 2 marks each.

11. In  $\triangle RST$ ,  $RT = 6x - 2$ . In  $\triangle UVW$ ,  $UW = 2x + 7$ ,  $\angle R = \angle U$ , and  $\angle S = \angle V$ . What must be the value of  $x$  in order to prove that  $\triangle RST \cong \triangle UVW$ ?



Ans. Given that  $\angle S = \angle V$  and  $\angle R = \angle U$

$\angle T = \angle W$  (by Angle sum property of triangle)

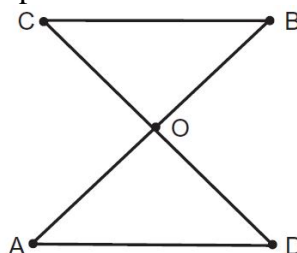
For  $\triangle RST \cong \triangle UVW$ ,  $RT = UW$  using either ASA or AAS congruence rule

$$\Rightarrow 6x - 2 = 2x + 7$$

$$\Rightarrow 6x - 2x = 9$$

$$\Rightarrow 4x = 9 \Rightarrow x = 9/4 \Rightarrow x = 2.25$$

12. In the given figure two lines AB and CD intersect each other at the point O such that  $BC \parallel AD$  and  $BC = DA$ . Show that O is the midpoint of both the line-segment AB and CD.



Ans.  $BC \parallel AD$  [Given]

Therefore  $\angle CBO = \angle DAO$  [Alternate interior angles]

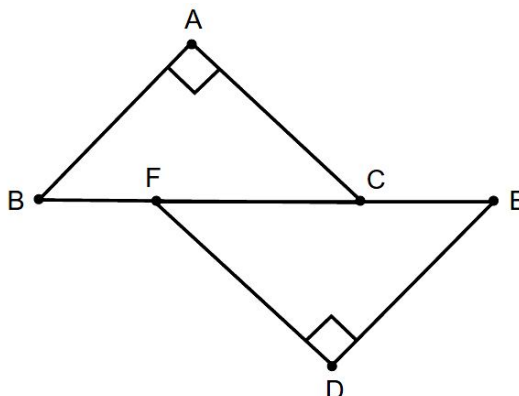
And  $\angle BCO = \angle ADO$  [Alternate interior angles]

Also,  $BC = DA$  [Given]

So,  $\triangle BOC \cong \triangle AOD$  [ASA congruence rule]

Therefore,  $OB = OA$  and  $OC = OD$ , i.e., O is the mid-point of both AB and CD.

13. In figure  $BA \perp AC$ ,  $DE \perp DF$ . Such that  $BA = DE$  and  $BF = EC$ . Show that  $\triangle ABC \cong \triangle DEF$ .



Ans. According to the question,  $BA \perp AC$ ,  $DE \perp DF$

Such that  $BA = DE$  and  $BF = EC$ .

In,  $\triangle ABC$  and  $\triangle DEF$

$BA = ED$  [Given]

$BF = EC$  [Given]

$\angle A = \angle D$  [Both  $90^\circ$ ]

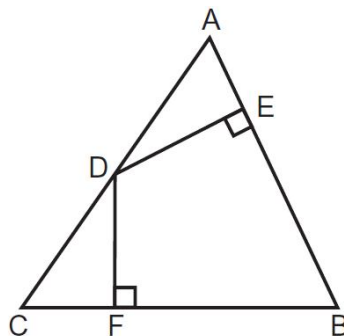
Now,  $BF = EC$  [Given]

$$\Rightarrow BF + FC = EC + FC$$

$$\Rightarrow BC = EF$$

$\therefore \triangle ABC \cong \triangle DEF$  [By RHS Congruence Rule]

14. In  $\triangle ABC$ , D is a point on side AC such that  $DE = DF$  and  $AD = CD$  and  $DE \perp AB$  at E and  $DF \perp CB$  at F, then prove that  $AB = BC$ .

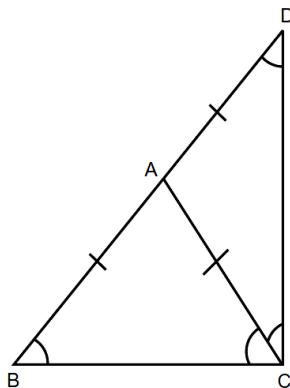


Ans. In  $\triangle AED$  and  $\triangle CFD$ ,  
 $AD = CD$   
 $DE = DF$   
 $\triangle AED \cong \triangle CFD$  [By RHS congruence rule]  
 $\angle A = \angle C$   
 $\therefore AB = BC$  [Sides opposite to equal angles are equal]

### SECTION – C

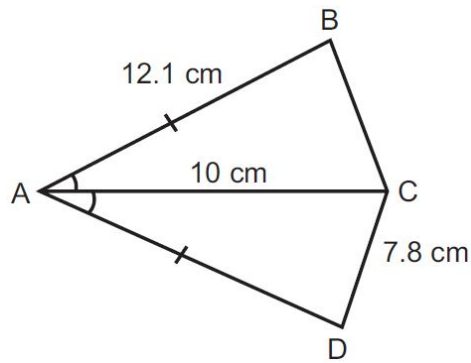
Questions 15 to 17 carry 3 marks each.

15.  $\triangle ABC$  is an isosceles triangle in which  $AB = AC$ . Side BA is produced to D such that  $AD = AB$ . Show that  $\angle BCD$  is a right angle.



Ans. In  $\triangle ABC$ ,  $AB = AC$   
 Also,  $AD = AB$   
 i.e.,  $AC = AB = AD$   
 In  $\triangle ABC$ ,  $AB = AC$   
 $\Rightarrow \angle ACB = \angle ABC = \angle 1 \dots$  (i) [Angles opposite to equal sides are equal]  
 In  $\triangle ACD$ ,  $AC = AD$  [As  $AC = AB$ ]  
 $\angle ADC = \angle ACD = \angle 2 \dots$  (ii) [Angle opposite to equal sides are equal]  
 In  $\triangle BCD$ ,  $\angle DBC + \angle BCD + \angle BDC = 180^\circ \dots$  (iii) [Angle sum property of triangle]  
 $\Rightarrow \angle 1 + \angle 1 + \angle 2 + \angle 2 = 180^\circ$   
 $\Rightarrow 2(\angle 1 + \angle 2) = 180^\circ$   
 $\Rightarrow \angle 1 + \angle 2 = 90^\circ \Rightarrow \angle BCD = 90^\circ$

16. Find the perimeter of the quadrilateral ABCD (as shown in the figure), if  $\angle CAB = \angle CAD$  and also  $AB = AD$ .



Ans. Since  $AB = AD$  [Given]

$\therefore AD = 12.1 \text{ cm}$  [ $AB = 12.1 \text{ cm}$ ]

Now, In  $\triangle ABC$  and  $\triangle ADC$

$AB = AD$  [Given]

$\angle BAC = \angle DAC$  [Given]

$AC = AC$  [Given]

$\therefore \triangle ABC \cong \triangle ADC$  [By SAS congruence rule]

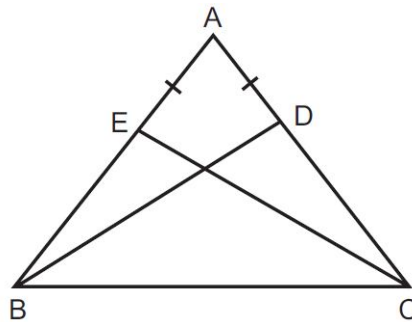
Hence  $BC = DC$  [By CPCT]

$BC = 7.8 \text{ cm}$

Now, we have to calculate the perimeter of quadrilateral.

Perimeter =  $AB + BC + CD + AD = 12.1 + 7.8 + 7.8 + 12.1 = 39.8 \text{ cm}$

17. ABC is an isosceles triangle with  $AB = AC$  and BD and CE are its two medians. Show that  $BD = CE$ .



Ans. Given:  $AB = AC$

Also, BD and CE are two medians

$\therefore E$  is the mid-point of AB

$D$  is the mid-point of AC

Hence  $\frac{1}{2} AB = \frac{1}{2} AC$

$\Rightarrow BE = CD$

In  $\triangle BEC$  and  $\triangle CDB$

$BE = CD$  [Given]

$\angle EBC = \angle DCB$  [Angles opposite to equal sides are equal]

$BC = BC$  [Common]

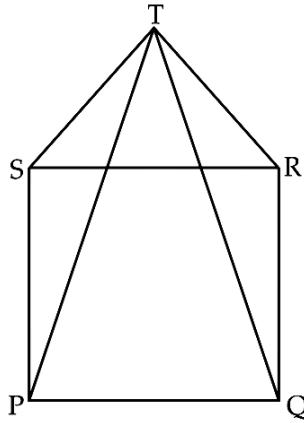
Hence,  $\triangle BEC \cong \triangle CDB$  [By SAS congruence rule]

$BD = CE$  [By CPCT]

## SECTION – D

Questions 18 carry 5 marks.

18. In figure, PQRS is a square and SRT is an equilateral triangle. Prove that :



(i)  $PT = QT$  (ii)  $\angle TQR = 15^\circ$

Ans. PQRS is a square. (Given)

(i) SRT is an equilateral triangle. (Given)

$\therefore \angle PSR = 90^\circ, \angle TSR = 60^\circ$

$\Rightarrow \angle PSR + \angle TSR = 150^\circ$ .

Similarly,  $\angle QRT = 150^\circ$

In  $\triangle PST$  and  $\triangle QRT$ , we have  $PS = QR$

$\angle PST = \angle QRT = 150^\circ$

and  $ST = RT$

By SAS,  $\triangle PST \cong \triangle QRT$

$\Rightarrow PT = QT$  (CPCT)

Hence Proved.

(ii) In  $\triangle TQR$ ,  $QR = RT$  (Square and equilateral triangle on same base)

or,  $\angle TQR = \angle QTR = x$

$\therefore x + x + \angle QRT = 180^\circ$

$\Rightarrow 2x + 150^\circ = 180^\circ$

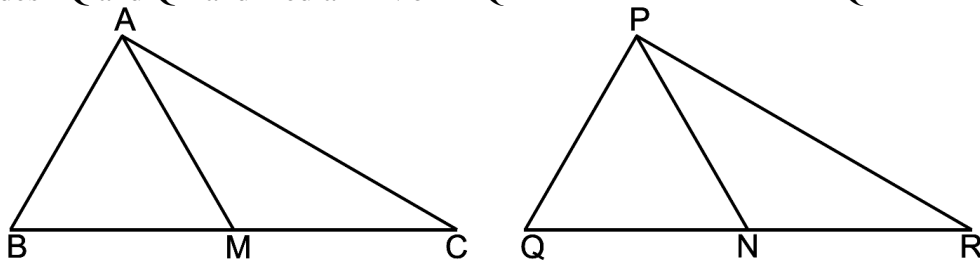
$\Rightarrow 2x = 30^\circ$

$\therefore x = 15^\circ$ .

$\Rightarrow \angle TQR = 15^\circ$ .

**OR**

In the below figure, two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of  $\triangle PQR$ . Show that  $\triangle ABC \cong \triangle PQR$ .



Ans. In  $\triangle ABC$  and  $\triangle PQR$ ,

$BC = QR$  (Given)

$\Rightarrow \frac{1}{2} BC = \frac{1}{2} QR$

$\Rightarrow BM = QN$

In triangles ABM and PQN, we have

$AB = PQ$  (Given)

$BM = QN$  (Proved above)

$AM = PN$  (Given)

$\therefore \triangle ABM \cong \triangle PQN$  (By SSS congruence criterion)

$\Rightarrow \angle B = \angle Q$  (By CPCT)

Now, in triangles ABC and PQR, we have

$AB = PQ$  (Given)

$\angle B = \angle Q$  (Proved above)

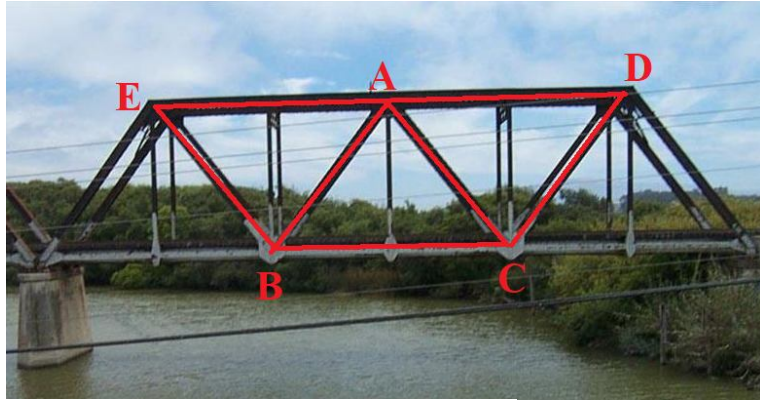
BC = QR (Given)

$\therefore \triangle ABC \cong \triangle PQR$  (By SAS congruence criterion)

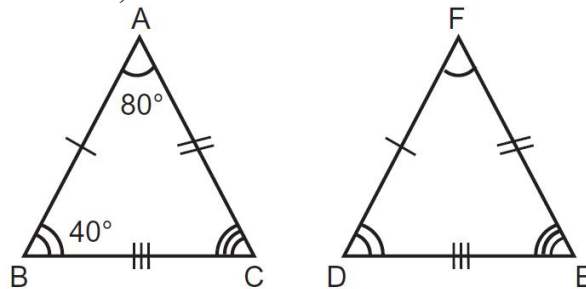
### **SECTION – E (Case Study Based Questions)**

**Questions 19 to 20 carry 4 marks each.**

- 19.** Truss bridges are formed with a structure of connected elements that form triangular structures to make up the bridge. Trusses are the triangles that connect to the top and bottom cord and two end posts. You can see that there are some triangular shapes are shown in the picture given alongside and these are represented as  $\triangle ABC$ ,  $\triangle CAD$ , and  $\triangle BEA$ .



- (a) If  $AB = CD$  and  $AD = CB$ , then prove  $\triangle ABC \cong \triangle CDA$   
(b) If  $AB = 7.5$  m,  $AC = 4.5$  m and  $BC = 5$  m. Find the perimeter of  $\triangle ACD$ , if  $\triangle ABC \cong \triangle CDA$  by SSS congruence rule.  
(c) If  $\triangle ABC \cong \triangle FDE$ ,  $AB = 5$  cm,  $\angle B = 40^\circ$  and  $\angle A = 80^\circ$ . Then find the length of  $DF$  and  $\angle E$ .



Ans. Ans. (a) In  $\triangle ABC$  and  $\triangle CDA$ ,

$AB = CD$  [Given]

$AD = CB$  [Given]

$AC = CA$  [common]

So by SSS congruence rule,  $\triangle ABC \cong \triangle CDA$

(b) Given that  $\triangle ABC \cong \triangle CDA$  [By SSS congruence rule]

So, Perimeter of  $\triangle ABC$  = Perimeter of  $\triangle CDA$

$(7.5 \text{ m} + 4.5 \text{ m} + 5 \text{ m}) = \text{Perimeter of } \triangle CDA$

The required perimeter of  $\triangle CDA = 17$  m.

(c) Given,  $\triangle ABC \cong \triangle FDE$  and  $AB = 5$  cm,

$\angle B = 40^\circ$

$\angle A = 80^\circ$

Since,  $\triangle FDE \cong \triangle ABC$

$DF = AB$  [By CPCT]

$DF = 5$  cm

and  $\angle E = \angle C$

$\Rightarrow \angle E = \angle C = 180^\circ - (\angle A + \angle B)$  [By Angle Sum Property of a DABC]

$\Rightarrow \angle E = 180^\circ - (80^\circ + 40^\circ) \Rightarrow \angle E = 60^\circ$

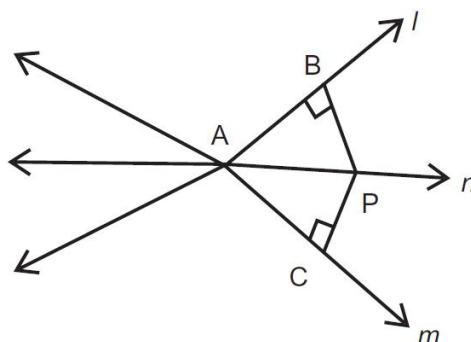
Hence,  $DF = 5$  cm,  $\angle E = 60^\circ$



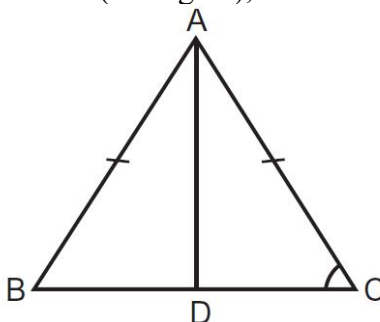
20. To check the understanding of the students of the class about IX the triangles, the Mathematics teacher write some questions on the blackboard and ask the students to read them carefully and answer the following question.



- (a) In figure, P is a point equidistant from the lines  $l$  and  $m$  intersecting at point A, then find  $\angle BAP$ .

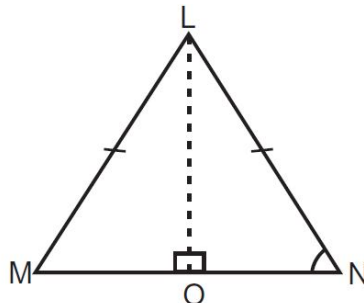


- (b) In  $\triangle ABC$ , if  $AB = AC$  and  $BD = DC$  (see figure), then find  $\angle ADC$ .



OR

- (b)  $\triangle LMN$  is an isosceles triangle, where  $LM = LN$  and LO, is an angle bisector of  $\angle MLN$ , Prove that point 'O' is the mid-point of side MN.



Ans. Ans. (a) Let us consider  $\triangle PAB$  and  $\triangle PAC$  (as shown in figure).

Here, we have  $PB = PC$  [Perpendicular distance]

$\angle PBA = \angle PCA$  [Each  $90^\circ$ ]

$PA = PA$  [Common]

$\triangle PAB \cong \triangle PAC$  [By RHS congruence rule]

So,  $\angle BAP = \angle CAP$  [By CPCT]

(b) We have,  $AB = AC$ ,  $BD = CD$  and  $AD = AD$

$\therefore \triangle ABD = \triangle ACD$  [By SSS congruence rule]

$$\angle ADB = \angle ADC \text{ [By CPCT]}$$

Since, BDC is a straight line.

$$\therefore \angle ADB + \angle ADC = 180^\circ \text{ [By SSS congruence rule]}$$

$$\Rightarrow 2\angle ADC = 180^\circ$$

$$\Rightarrow \angle ADC = 90^\circ$$

**OR**

(b) Given:  $LM = LN$  and  $\angle MLO = \angle NLO$

Since  $\triangle LMN$  is an isosceles triangle and  $LM = LN$

$$\therefore \angle M = \angle N \dots(i)$$

LO is an angle bisector of  $\angle MLN$

$$\angle MLO = \angle NLO \dots(ii)$$

In  $\triangle MLO$  and  $\triangle NLO$ ,  $\angle M = \angle N$

$$\text{i.e., } \angle OML = \angle ONL$$

$$LM = LN$$

$$\angle MLO = \angle NLO$$

$$\therefore \triangle MLO \cong \triangle NLO \text{ [By ASA congruence rule]}$$

$$\therefore OM = ON \text{ [By CPCT]}$$

.....