

StatisticalInference-Project

Miguel Baquero

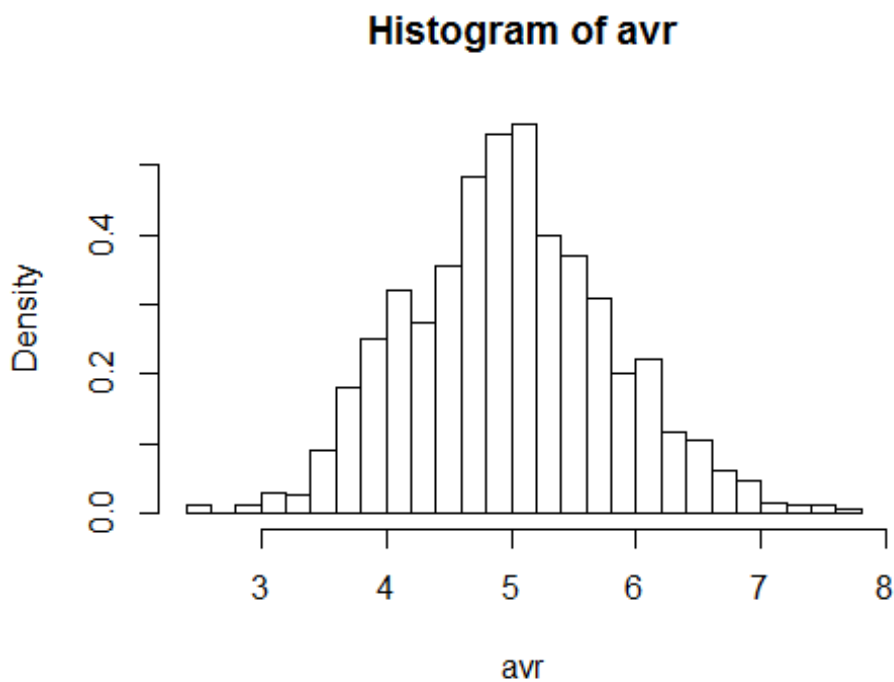
Sunday, September 21, 2014

Project for Statistical Inference in Coursera

Part 1

First we simulate the 1000 means of 40 exponentials, and plot and histogram to observe the center:

```
avr<-replicate(1000,mean(rexp(40,0.2)))  
hist(avr,30,freq=F)
```



Theoretically it should be 5 ($1/\lambda$), the center of the distribution is actually:

```
mean(avr)  
## [1] 4.988  
  
## Then if we normalize by applying  $X-5/(5/\sqrt{40})$   
avr_norm<-(avr-5)/(5/sqrt(40))  
## We can see that the simulation mean is  
mean(avr_norm)  
## [1] -0.01532
```

```
## Standard deviations less than the population mean
```

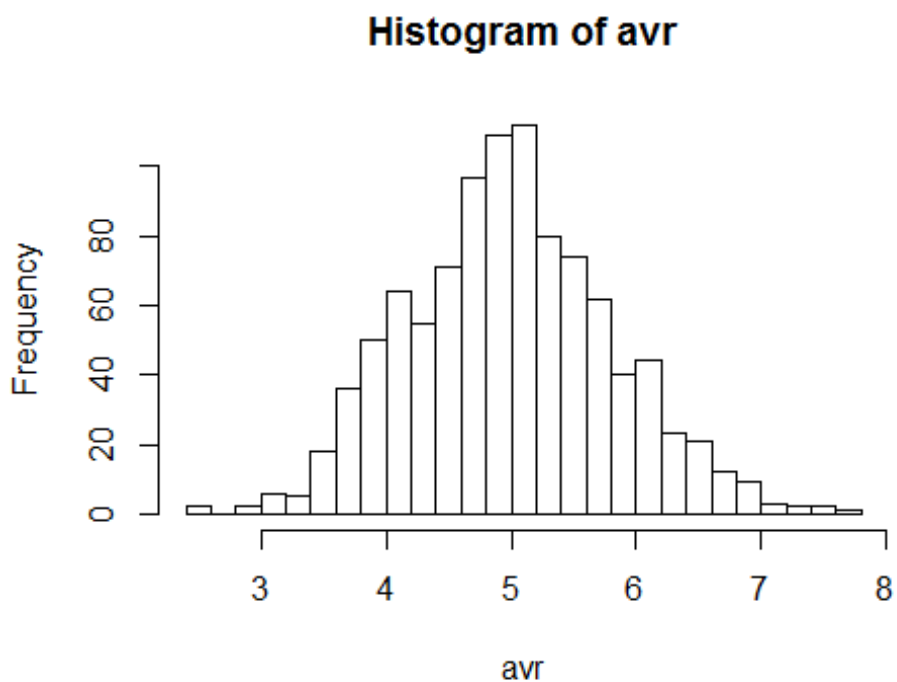
For the variance, theoretically it should be 0.625 (25/40) but the real value is presented now:

```
var(avr)
```

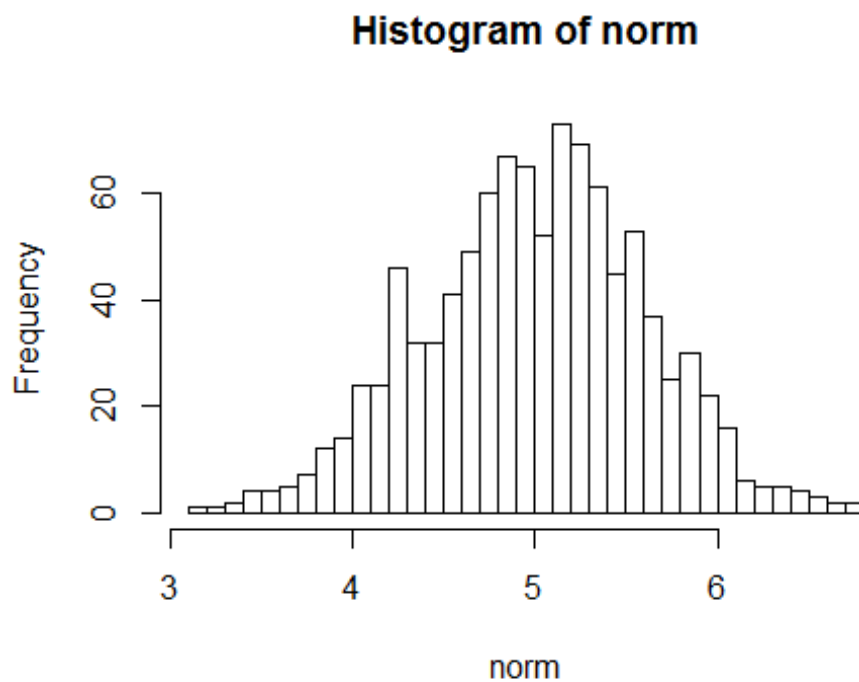
```
## [1] 0.6554
```

To show that is approximately normal, we can plot the theoretical normal $N(5, 0.625)$ and the histogram of the actual distribution:

```
norm<-rnorm(n = 1000, mean = 5, sd=0.625)  
hist(avr, breaks=30)
```



```
hist(x=norm, breaks=30)
```



#They are fairly similar

The coverage of the confidence interval is:

```
## High end of the interval is:  
mean(avr)+1.96*var(avr)/sqrt(40)
```

```
## [1] 5.191
```

```
## and the low end:
```

```
mean(avr)-1.96*var(avr)/sqrt(40)
```

```
## [1] 4.785
```

```
## With 95% confidence interval
```