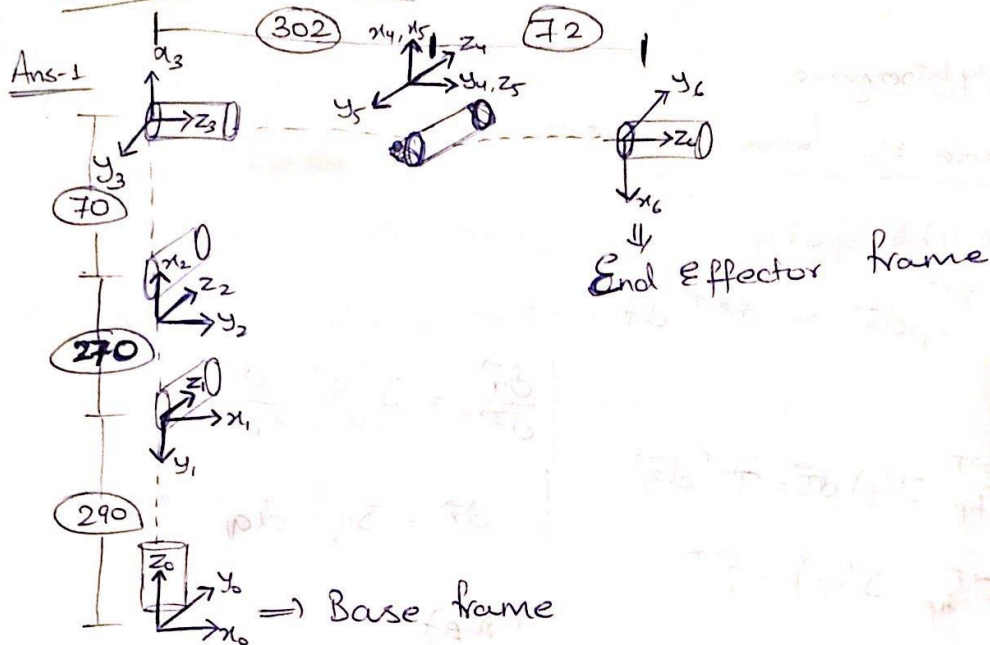


Dynamics homework-2



Ans-2 D-H parameters

n	θ (degree)	α (degree)	d (mm)	a (mm)
1	θ_1	-90°	290mm	0mm
2	$(\theta_2 - 90)^\circ$	0°	0mm	270mm
3	$(\theta_3)^\circ$	-90°	0mm	70mm
4	$(\theta_4)^\circ$	90°	302mm	0mm
5	$(\theta_5)^\circ$	-90°	0mm	0mm
6	$(\theta_6 + 180)^\circ$	0°	72mm	0mm

θ = Rotation about z_{n-1} axis

α = Rotation about x_n axis

d = Translation about z_{n-1} axis

a = Translation about x_n axis.

PRIMARY CODE (ALL CODES PROVIDED IN A SEPARATE FILE)

```
clc,clear;
```

```
syms q1 q2 q3 q4 q5 q6
```

%ANSWER-2

```
theta = deg2rad([q1, q2-90, q3, q4, q5, q6+180]);  
alpha = deg2rad([-90, 0, -90, 90, -90, 0]);  
d = [290, 0, 0, 302, 0, 72];  
a = [0, 270, 70, 0, 0, 0];
```

ANSWER-3 (The entire code for function is mentioned later)

```
T_M = dhparam2matrix(theta, alpha, d, a)
```

```
T_total = T_M(:,:,1)*T_M(:,:,2)*T_M(:,:,3)*T_M(:,:,4)*T_M(:,:,5)*T_M(:,:,6)  
T_simplified= simplify(T_total)  
  
T_0_6_Q5 = subs(T_simplified, [q1,q2,q3,q4,q5,q6], [0,0,0,0,0,0]);  
T_0_6_Q5 = round(T_0_6_Q5)  
  
T_0_6_Q6 = subs(T_simplified, [q1,q2,q3,q4,q5,q6], [-45,30,-30,-30,-45,180]);  
T_0_6_Q6 = round(T_0_6_Q6)  
%T1 = plotarm(-50,40,-30,-30,-50,180)  
T_0_6_Q8_1 = subs(T_simplified, [q1,q2,q3,q4,q5,q6], [-50,40,-30,-30,-50,180]);  
T_0_6_Q8_1 = round(T_0_6_Q8_1)  
%T2 = plotarm(-11,-4,26,-9,-27,-16)  
T_0_6_Q8_2 = subs(T_simplified, [q1,q2,q3,q4,q5,q6], [-11,-4,26,-9,-27,-16]);  
T_0_6_Q8_2 = round(T_0_6_Q8_2)  
%T3 = plotarm(-5,50,-36,-24,-36,0)  
T_0_6_Q8_3 = subs(T_simplified, [q1,q2,q3,q4,q5,q6], [-5,50,-36,-24,-36,0]);  
T_0_6_Q8_3 = round(T_0_6_Q8_3)  
%T4 = plotarm(-45,35,-35,-35,-40,0)  
T_0_6_Q8_4 = subs(T_simplified, [q1,q2,q3,q4,q5,q6], [-45,35,-35,-35,-40,0]);  
T_0_6_Q8_4 = round(T_0_6_Q8_4)  
%T5 = plotarm(-10,-5,-20,-20,-10,0);  
T_0_6_Q8_5 = subs(T_simplified, [q1,q2,q3,q4,q5,q6], [-10,-5,-20,-20,-10,0]);  
T_0_6_Q8_5 = round(T_0_6_Q8_5)
```

ANS 3 - CODE - dhparam2matrix function

```
function T_M = dhparam2matrix(theta, alpha, d, a)  
old = digits(2);  
for i= 1:6  
    T_M(:,:,i)= vpa([cos(theta(i)) (-sin(theta(i))*cos(alpha(i)))  
    (sin(theta(i))*sin(alpha(i))) (a(i)*cos(theta(i)))  
    sin(theta(i)) cos(theta(i))*cos(alpha(i)) (-cos(theta(i))*sin(alpha(i)))  
    a(i)*sin(theta(i));  
    0 (sin(alpha(i))) cos(alpha(i)) d(i);  
    0 0 0 1]);  
  
end  
end
```

ANS-3-c - SYMBOLIC TRANSFORMATION MATRICES

$$T_M(:, :, 1) = T^0_1$$

$$\begin{bmatrix} \cos(0.017*q_1) & -6.1e-17*\sin(0.017*q_1) & -1.0*\sin(0.017*q_1) & 0 \end{bmatrix}$$

$$\begin{bmatrix} \sin(0.017*q_1) & 6.1e-17*\cos(0.017*q_1) & \cos(0.017*q_1) & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & -1.0 & 6.1e-17 & 299.0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 1.0 \end{bmatrix}$$

$$T_M(:, :, 2) = T^1_2$$

$$\begin{bmatrix} \cos(0.017*q_2 - 1.6) & -1.0*\sin(0.017*q_2 - 1.6) & 0 & 277.0*\cos(0.017*q_2 - 1.6) \end{bmatrix}$$

$$\begin{bmatrix} \sin(0.017*q_2 - 1.6) & \cos(0.017*q_2 - 1.6) & 0 & 277.0*\sin(0.017*q_2 - 1.6) \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 1.0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 1.0 \end{bmatrix}$$

$$T_M(:, :, 3) = T^2_3$$

$$\begin{bmatrix} \cos(0.017*q_3) & -6.1e-17*\sin(0.017*q_3) & -1.0*\sin(0.017*q_3) & 70.0*\cos(0.017*q_3) \end{bmatrix}$$

$$\begin{bmatrix} \sin(0.017*q_3) & 6.1e-17*\cos(0.017*q_3) & \cos(0.017*q_3) & 70.0*\sin(0.017*q_3) \end{bmatrix}$$

$$\begin{bmatrix} 0 & -1.0 & 6.1e-17 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 1.0 \end{bmatrix}$$

$$T_M(:, :, 4) = T^3_4$$

$$\begin{bmatrix} \cos(0.017*q_4) & -6.1e-17*\sin(0.017*q_4) & \sin(0.017*q_4) & 0 \end{bmatrix}$$

$$\begin{bmatrix} \sin(0.017*q_4) & 6.1e-17*\cos(0.017*q_4) & -1.0*\cos(0.017*q_4) & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1.0 & 6.1e-17 & 300.0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & 1.0 \end{bmatrix}$$

$$T_M(:, :, 5) = T^4_5$$

```
[ cos(0.017*q5), -6.1e-17*sin(0.017*q5), -1.0*sin(0.017*q5), 0]
```

```
[ sin(0.017*q5), 6.1e-17*cos(0.017*q5), cos(0.017*q5), 0]
```

```
[ 0, -1.0, 6.1e-17, 0]
```

```
[ 0, 0, 0, 1.0]
```

$$T_M(:, :, 6) = T^5_6$$

```
[ cos(0.017*q6 + 3.1), -1.0*sin(0.017*q6 + 3.1), 0, 0]
```

```
[ sin(0.017*q6 + 3.1), cos(0.017*q6 + 3.1), 0, 0]
```

```
[ 0, 0, 1.0, 72.0]
```

```
[ 0, 0, 0, 1.0]
```

ANSWER 4 - $T_simplified = T^0_6$ (THE CODE IS BIG DUE TO MATLAB

CONSIDERING SMALL TERMS THAT CAN BE NEGLIGIBLE - SIMPLIFIED MATRIX IS ALSO SHOWN BELOW THIS GENERATED MATRIX.)

```
[ sin(0.018*q6 + 3.1)*(3.7e-33*sin(0.018*q1)
+ 6.1e-17*sin(0.018*q5)*(cos(0.018*q4)*(sin(0.018*q3)*(6.1e-17*cos(0.018*q2 -
1.6)*sin(0.018*q1) + cos(0.018*q1)*sin(0.018*q2 - 1.6)) -
cos(0.018*q3)*(cos(0.018*q2 - 1.6)*cos(0.018*q1) - 6.1e-17*sin(0.018*q2 -
1.6)*sin(0.018*q1))) + sin(0.018*q4)*(6.1e-17*cos(0.018*q3)*(6.1e-17*cos(0.018*q2 -
1.6)*sin(0.018*q1) + cos(0.018*q1)*sin(0.018*q2 - 1.6)) - 1.0*sin(0.018*q1) + 6.1e-
17*sin(0.018*q3)*(cos(0.018*q2 - 1.6)*cos(0.018*q1) - 6.1e-17*sin(0.018*q2 -
1.6)*sin(0.018*q1)))) + 6.1e-17*cos(0.018*q3)*(6.1e-17*cos(0.018*q2 -
1.6)*sin(0.018*q1) + cos(0.018*q1)*sin(0.018*q2 - 1.6)) - 6.1e-
17*cos(0.018*q5)*(6.1e-17*sin(0.018*q1) + cos(0.018*q3)*(6.1e-17*cos(0.018*q2 -
1.6)*sin(0.018*q1) + cos(0.018*q1)*sin(0.018*q2 - 1.6)) - 6.1e-
17*sin(0.018*q4)*(sin(0.018*q3)*(6.1e-17*cos(0.018*q2 - 1.6)*sin(0.018*q1) +
cos(0.018*q1)*sin(0.018*q2 - 1.6)) - cos(0.018*q3)*(cos(0.018*q2 -
1.6)*cos(0.018*q1) - 6.1e-17*sin(0.018*q2 - 1.6)*sin(0.018*q1))) + 6.1e-
17*cos(0.018*q4)*(6.1e-17*cos(0.018*q3)*(6.1e-17*cos(0.018*q2 - 1.6)*sin(0.018*q1)
+ cos(0.018*q1)*sin(0.018*q2 - 1.6)) - 1.0*sin(0.018*q1) + 6.1e-
17*sin(0.018*q3)*(cos(0.018*q2 - 1.6)*cos(0.018*q1) - 6.1e-17*sin(0.018*q2 -
1.6)*sin(0.018*q1))) + sin(0.018*q3)*(cos(0.018*q2 - 1.6)*cos(0.018*q1) - 6.1e-
17*sin(0.018*q2 - 1.6)*sin(0.018*q1))) + sin(0.018*q4)*(sin(0.018*q3)*(6.1e-
17*cos(0.018*q2 - 1.6)*sin(0.018*q1) + cos(0.018*q1)*sin(0.018*q2 - 1.6)) -
cos(0.018*q3)*(cos(0.018*q2 - 1.6)*cos(0.018*q1) - 6.1e-17*sin(0.018*q2 -
1.6)*sin(0.018*q1))) - 1.0*cos(0.018*q4)*(6.1e-17*cos(0.018*q3)*(6.1e-
17*cos(0.018*q2 - 1.6)*sin(0.018*q1) + cos(0.018*q1)*sin(0.018*q2 - 1.6)) -
1.0*sin(0.018*q1) + 6.1e-17*sin(0.018*q3)*(cos(0.018*q2 - 1.6)*cos(0.018*q1) -
6.1e-17*sin(0.018*q2 - 1.6)*sin(0.018*q1))) + 6.1e-17*sin(0.018*q3)*(cos(0.018*q2 -
1.6)*cos(0.018*q1) - 6.1e-17*sin(0.018*q2 - 1.6)*sin(0.018*q1))) - cos(0.018*q6 +
```

[illegible]

[illegible]


```

sin(0.018*q5)*(72.0*cos(0.018*q4)*sin(0.018*q2 + 0.018*q3 - 1.6) +
72.0*sin(0.018*q4)*(6.1e-17*cos(0.018*q2 + 0.018*q3 - 1.6) + 6.1e-17)) -
300.0*cos(0.018*q2 + 0.018*q3 - 1.6) - 70.0*sin(0.018*q2 + 0.018*q3 - 1.6) -
277.0*sin(0.018*q2 - 1.6) - cos(0.018*q5)*(72.0*cos(0.018*q2 + 0.018*q3 - 1.6) -
4.4e-15*sin(0.018*q4)*sin(0.018*q2 + 0.018*q3 - 1.6) + 72.0*cos(0.018*q4)*(3.7e-
33*cos(0.018*q2 + 0.018*q3 - 1.6) + 3.7e-33) - 2.7e-31) - 4.4e-
15*sin(0.018*q4)*sin(0.018*q2 + 0.018*q3 - 1.6) + cos(0.018*q4)*(2.7e-
31*cos(0.018*q2 + 0.018*q3 - 1.6) + 2.7e-31) + 299.0]

[
0,
0,
0,
1.0]

```

Basically, if we ignore the small terms, we obtain

$$= \begin{bmatrix} 72(-c\theta_{123}s\theta_1 + c\theta_{14}s\theta_{23} - s\theta_{14}s - c\theta_{123}s\theta_1 - c\theta_{123}s\theta_1) - 302(c\theta_{12}s\theta_1 + c\theta_{12}s\theta_1) + 70(c\theta_{123} - c\theta_{12}s\theta_{23}) + 270(c\theta_{12}) \\ 72(-c\theta_{234}s\theta_{15} + c\theta_{4}s\theta_{123} + c\theta_1s\theta_{45} - c\theta_{25}s\theta_{12} - c\theta_{25}s\theta_{12}) - 302(c\theta_2s\theta_{13} + c\theta_1s\theta_{12}) + 70(c\theta_{23}s\theta_1 - s\theta_{123}) + 270(c\theta_2s\theta_1) \\ 72(c\theta_{14}s\theta_{25} + c\theta_{24}s\theta_{15} + c\theta_2s\theta_{23} - c\theta_{23}) + 302(s\theta_{23} - c\theta_{23}) - 70(c\theta_1s\theta_2 + c\theta_2s\theta_1) - 270(s\theta_2) + 290 \\ 1 \end{bmatrix}$$

ANS-5

T_0_6_Q5 =

```

[ 0, 0, 1, 374]

[ 0, 1, 0, 0]

[-1, 0, 0, 630]

[ 0, 0, 0, 1]

```

ANS-6-a

T_0_6_Q6 =

```

[ 0, -1, 1, 363]

[ 1, -1, 0, -328]

[ 1, 0, 1, 637]

[ 0, 0, 0, 1]

```

ANS 6 -b = Cartesian position = [363 mm , -328mm, -637mm]^T

ANS 6 -c = Unit vector representing approach vector = [1, 0, 1]^T

ANS 7 - plotarm function code. THE IMAGES ARE SHOWN in answer-8

```
function T = plotarm(Q1,Q2,Q3,Q4,Q5,Q6);

syms q1 q2 q3 q4 q5 q6
theta = deg2rad([q1, q2-90, q3, q4, q5, q6+180]);
alpha = deg2rad([-90, 0, -90, 90, -90, 0]);
d = [290, 0, 0, 302, 0, 72];
a = [0, 270, 70, 0, 0, 0];
T_M = dhparam2matrix(theta, alpha, d, a);

X=[0];
Y=[0];
Z=[0];

for i=1:6
    T_M(:, :, i) = vpa(subs(T_M(:, :, i), [q1, q2, q3, q4, q5, q6], [Q1,Q2,Q3,Q4,Q5,Q6]));
end

T_0_1 = T_M(:, :, 1);
T_0_2 = T_M(:, :, 1)*T_M(:, :, 2);
T_0_3 = T_M(:, :, 1)*T_M(:, :, 2)*T_M(:, :, 3);
T_0_4 = T_M(:, :, 1)*T_M(:, :, 2)*T_M(:, :, 3)*T_M(:, :, 4);
T_0_5 = T_M(:, :, 1)*T_M(:, :, 2)*T_M(:, :, 3)*T_M(:, :, 4)*T_M(:, :, 5);
T_0_6 = T_M(:, :, 1)*T_M(:, :, 2)*T_M(:, :, 3)*T_M(:, :, 4)*T_M(:, :, 5)*T_M(:, :, 6);

X = round([X, T_0_1(1,4) , T_0_2(1,4), T_0_3(1,4), T_0_4(1,4), T_0_5(1,4), T_0_6(1,4)]);
Y = round([Y, T_0_1(2,4) , T_0_2(2,4), T_0_3(2,4), T_0_4(2,4), T_0_5(2,4), T_0_6(2,4)]);
Z = round([Z, T_0_1(3,4) , T_0_2(3,4), T_0_3(3,4), T_0_4(3,4), T_0_5(3,4), T_0_6(3,4)]);

figure
scatter3(X,Y,Z);
hold on
plot3(X,Y,Z);
xlabel('x')
ylabel('y')
zlabel('z')
hold off
```

ANS-8

As seen from the images, the computed values match the values from ROBOT STUDIO.

Any deviations are due to the rounding off in the program.

Images have been provided in a separate file as well to crosscheck the answers.

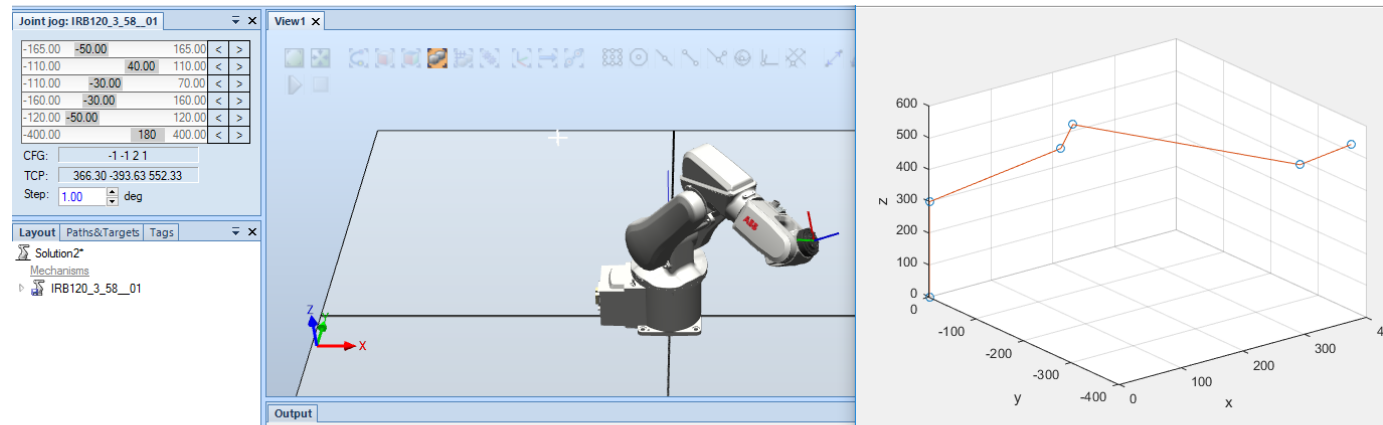
T_0_6_Q8_1 =

[0, -1, 1, 366] Tool Cartesian position w.r.t baseframe is[366mm, -395mm, 551mm]^T

[1, -1, 0, -395]

[1, 0, 1, 551]

[0, 0, 0, 1]



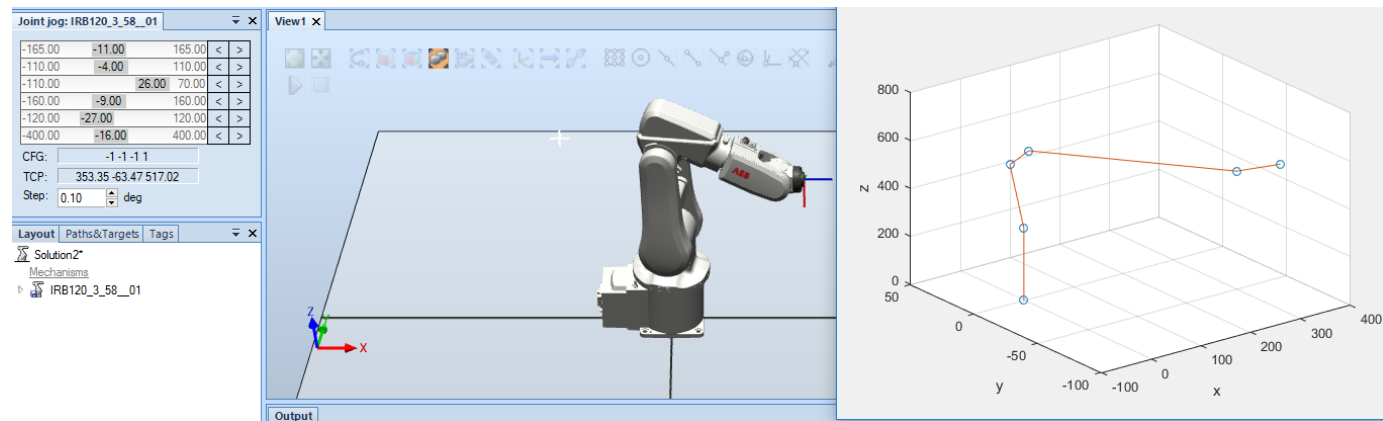
T_0_6_Q8_2 =

[0, 0, 1, 353] Tool Cartesian position w.r.t baseframe is[353mm, -64mm, 516mm]^T

[0, 1, 0, -64]

[-1, 0, 0, 516]

[0, 0, 0, 1]



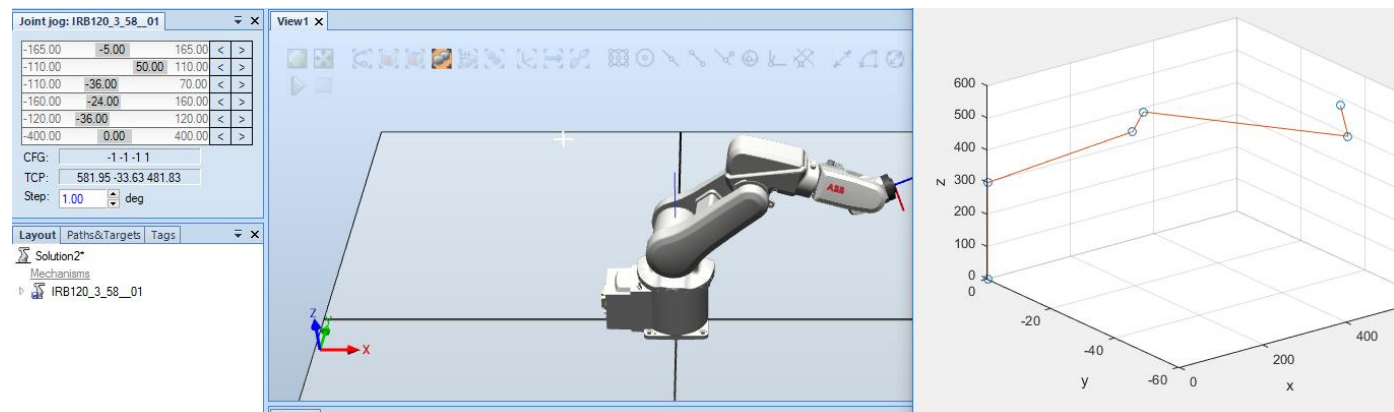
$T_{0_6_Q8_3} =$

$\begin{bmatrix} 0 & 0 & 1 & 582 \end{bmatrix}$ Tool Cartesian position w.r.t baseframe is $[582\text{mm}, -34\text{mm}, 481\text{mm}]^T$

$\begin{bmatrix} 0 & 1 & 0 & -34 \end{bmatrix}$

$\begin{bmatrix} -1 & 0 & 0 & 481 \end{bmatrix}$

$\begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix}$



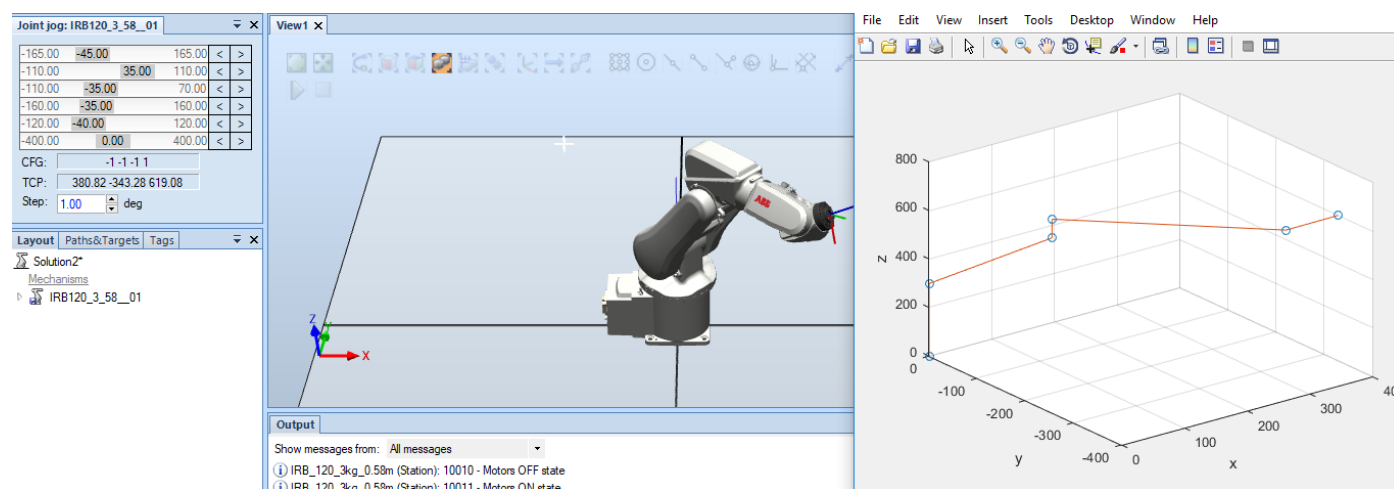
$T_{0_6_Q8_4} =$

$\begin{bmatrix} 0 & 1 & 1 & 381 \end{bmatrix}$ Tool Cartesian position w.r.t baseframe is $[381\text{mm}, -344\text{mm}, 618\text{mm}]^T$

$\begin{bmatrix} -1 & 1 & 0 & -344 \end{bmatrix}$

$\begin{bmatrix} -1 & -1 & 1 & 618 \end{bmatrix}$

$\begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix}$



$T_{0_6_Q8_5} =$

$\begin{bmatrix} 0 & 0 & 1 & 276 \end{bmatrix}$ Tool Cartesian position w.r.t baseframe is $[276\text{mm}, -45\text{mm}, 791\text{mm}]^T$

$\begin{bmatrix} 0 & 1 & 0 & -45 \end{bmatrix}$

$\begin{bmatrix} -1 & 0 & 1 & 791 \end{bmatrix}$

$\begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix}$

