DS 100/200: Principles and Techniques of Data Science Date: August 12, 2019

Exam Review Solutions

Name:

EDA & Visualization

- 1. For each of the following scenarios, determine which plot type is *most* appropriate to reveal the distribution of and/or the relationships between the following variable(s). For each scenario, select only one plot type. Some plot types may be used multiple times.
 - A. histogram B. pie chart C. bar plot D. line plot
 - E. side-by-side boxplots F. scatter plot G. stacked bar plot H. overlaid line plots
 - (a) Sale price and number of bedrooms for houses sold in Berkeley in 2010.

Solution: E. Side-by-side Boxplots. We might imagine using a scatter plot since we are plotting the relationship between two numeric quantities. However because the number of bedrooms is an integer and most houses will only have a small number, we are likely to encounter *over-plotting* in the scatter plot. Therefore side-by-side boxplots are likely to be most informative.

(b) Sale price and date of sale for houses sold in Berkeley between 1995 and 2015.

Solution: F. Scatter Plot. Here we are plotting two numeric quantities with sufficient spread on each axis.

(c) Infant birth weight (grams) for babies born at Alta Bates hospital in 2016.

Solution: A. Histogram. Here we are plotting the distribution of a likely large number of observations and therefore a histogram would be most appropriate.

(d) Mother's education-level (highest degree held) for students admitted to UC Berkeley in 2016.

Solution: C. Bar Plot. Here we want to visualize counts of a categorical variable.

(e) SAT score and HS GPA of students admitted to UC Berkeley in 2016.

Solution: F. Scatter Plot. Here we are visualizing the relationship between two continuous quantities.

(f) The percentage of female student admitted to UC Berkeley each year from 1950 to 2000.

Solution: D. Line plot. This allows us to see the trends over time.

(g) SAT score for males and females of students admitted to UCB from 1950 to 2000

Solution: E. side-by-side boxplots. This allows us to see the distributions of SAT scores per gender and year.

Optimization

2. Fix the following buggy Python implementation of gradient descent:

```
def grad_descent(X, Y, theta0, grad_function, max_iter = 1000):
    """X: A 2D array, the feature matrix.
    Y: A 1D array, the response vector.
    theta0: A 1D array, the initial parameter vector.
    grad_function: Maps a parameter vector, a feature matrix, and a
        response vector to the gradient of some loss function at the
        given parameter value. The return value is a 1D array."""
    theta = theta0
    for t in range(1, max_iter+1):
        grad = grad_function(theta, X, Y)
        theta = theta0 + t * grad
    return grad
```

```
Solution: The last two lines need to change:

def grad_descent(X, Y, theta0, grad_function, max_iter = 1000):
    """X: A 2D array, the feature matrix.
    Y: A 1D array, the response vector.
    theta0: A 1D array, the initial parameter vector.
    grad_function: Maps a parameter vector, a feature matrix, and
    a response vector to the gradient of some loss function at the given parameter value. The return value is a 1D
    array."""
    theta = theta0
    for t in range(1, max_iter+1):
        grad = grad_function(theta, X, Y)
        theta = theta - (1/t) * grad
    return theta
```

3. Suppose you are given a dataset $\{(x_i, y_i)\}_{i=1}^n$ where $x_i \in \mathbb{R}$ is a one dimensional feature and $y_i \in \mathbb{R}$ is a real-valued response. You use f_θ to model the data where θ is the model parameter. You choose to use the following regularized loss:

$$L(\theta) = \frac{1}{n} \sum_{i=1}^{n} (y_i - f_{\theta}(x_i))^2 + \lambda \theta^2$$

(a) This regularized loss is best described as:

- (a) Average absolute loss with L^2 regularization.
- (b) Average squared loss with L^1 regularization.
- (c) Average squared loss with L^2 regularization.
- (d) Average Huber loss with λ regularization.
- (b) Suppose you choose the model $f_{\theta}(x_i) = \theta x_i^3$. Using the above objective derive the loss minimizing estimate for θ .

Solution:

Step 1: Take the derivative of the loss function.

$$\frac{\partial}{\partial \theta} L(\theta) = \frac{1}{n} \sum_{i=1}^{n} \frac{\partial}{\partial \theta} \left(y_i - \theta x_i^3 \right)^2 + \frac{\partial}{\partial \theta} \lambda \theta^2 \tag{1}$$

$$= -\frac{2}{n} \sum_{i=1}^{n} \left(y_i - \theta x_i^3 \right) x_i^3 + 2\lambda \theta \tag{2}$$

Step 2: Set derivative equal to zero and solve for θ .

$$0 = -\frac{2}{n} \sum_{i=1}^{n} (y_i - \theta x_i^3) x_i^3 + 2\lambda \theta$$
 (3)

$$\theta = \frac{1}{n\lambda} \sum_{i=1}^{n} \left(y_i - \theta x_i^3 \right) x_i^3 \tag{4}$$

$$\theta = \frac{1}{n\lambda} \sum_{i=1}^{n} y_i x_i^3 - \theta \frac{1}{n\lambda} \sum_{i=1}^{n} x_i^6$$
 (5)

$$\theta\left(1 + \frac{1}{n\lambda} \sum_{i=1}^{n} x_i^6\right) = \frac{1}{n\lambda} \sum_{i=1}^{n} y_i x_i^3$$
 (6)

(7)

Thus we obtain the final answer:

$$\hat{\theta} = \frac{\frac{1}{n} \sum_{i=1}^{n} y_i x_i^3}{\left(\lambda + \frac{1}{n} \sum_{i=1}^{n} x_i^6\right)}$$
 (8)

Inference

4. **True or False.** Determine whether the following statements are true or false.

(a) Suppose we have 100 samples drawn independently from a population. If we construct a 95% confidence interval for each sample, we expect 95 of them to include the **sample** mean.

Solution: False. All of them should include the sample mean.

(b) We often prefer a pseudo-random number generator because our simulations results can be exactly reproduced by controlling the seed.

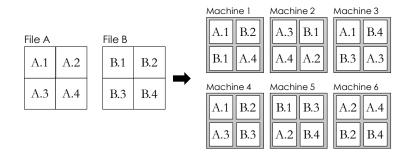
Solution: True. This is an essential aspect of reproducible data analyses and simulation studies.

5. Suppose we have a Pandas Series called **thePop** which contains a census of **25000** subjects. We also have a simple random sample of **400** individuals saved in the Series **theSample**. We are interested in studying the behavior of the bootstrap procedure on the simple random sample. Fill in the blanks in the code below to construct **10000** bootstrapped estimates for the median.

```
Solution:
boot_stats = [
    theSample
```

```
.sample(n = 400, replace = True)
.median()
for j in range(10000)
]
```

6. Consider the following layout of the files A and B onto a distributed file-system of 6 machines.



Assume that all blocks have the same file size and computation takes the same amount of time.

- (a) (1 point) If we wanted to load file A in parallel which of the following sets of machines would give the best load performance:
 - A. M1, M2 B. M1, M2, M3 C. M2, M4, M5, M6

Solution: While all choices would be able to load the file, only M2, M4, M5, M6 could load the file in parallel.

- (b) (1 point) If we were to lose machines M1, M2, and M3 which of the following file or files would we lose (select all that apply).
 - A. File A B. File B C. We would still be able to load both files.
- (c) (1 point) If each of the six machines fail with probability p, what is the probability that we will lose block B.1 of file B.?
 - A. 3p B. p^3 C. $(1-p)^3$ D. $1-p^3$