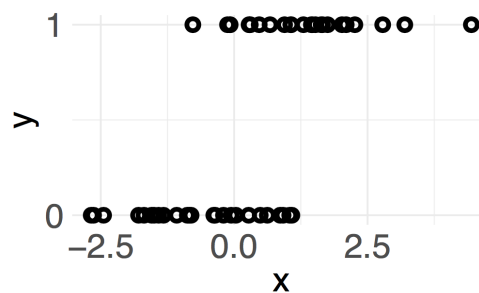


Discussion #11

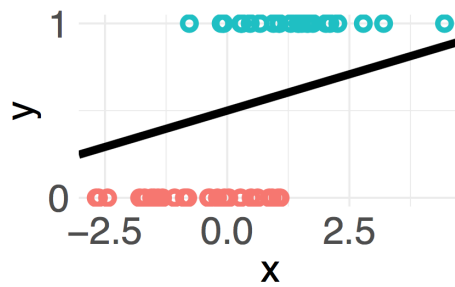
Name:

Logistic Regression

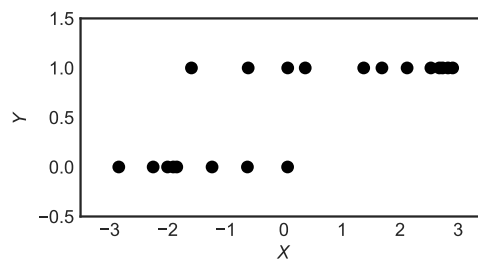
1. State whether the following claims are true or false. If false, provide a reason or correction.
 - (a) A binary or multi-class classification technique should be used whenever there are categorical features.
 - (b) A classifier that always predicts 0 has a test accuracy of 50% on all binary prediction tasks.
 - (c) For a logistic regression model, all features are continuous, with values from 0 to 1.
 - (d) In a setting with extreme class imbalance in which 95% of the training data have the same label, it is always possible to get at least 95% testing accuracy.
2. The next question refers to a binary classification problem with a single feature x . Based on the scatter plot of the data below, draw a reasonable approximation of the logistic regression probability estimates for $\mathbb{P}(Y = 1|x)$.



3. Your friend argues that the data are linearly separable by drawing the line on the following plot of the data. Argue whether or not your friend is correct.



4. Suppose you are given the following dataset $\{(x_i, y_i)\}_{i=1}^n$ consisting of x and y pairs where the covariate $x_i \in \mathbb{R}$ and the response $y_i \in \{0, 1\}$.



Given this data, the value $\mathbb{P}(Y = 1|x = -1)$ is likely closest to:

- ☐ 0.95 ☐ 0.50 ☐ 0.05 ☐ -0.95

5. You have a classification data set, where x is some value and y is the label for that value:

x	y
2	1
3	0
0	1
1	0

Suppose that we're using a logistic regression model to predict the probability that $Y = 1$ given x :

$$\mathbb{P}(Y = 1|x) = \sigma(\mathbf{X}\theta)$$

- (a) Suppose that $\mathbf{X} = [1 \ x \ x^2]^T$ and our model parameters are $\theta^* = [1 \ 0 \ -2]^T$. For the following parts, leave your answer as an expression (do not numerically evaluate log, e, π , etc).
- Compute $\hat{\mathbb{P}}(y = 1|x = 0)$.
 - What is the loss for this single prediction $\hat{\mathbb{P}}(y = 1|x = 0)$, assuming we are using Cross Entropy as our loss function (or equivalently that we are using the cross entropy as our loss function)?

6. Suppose we train a binary classifier on some dataset. Suppose y is the set of true labels, and \hat{y} is the set of predicted labels.

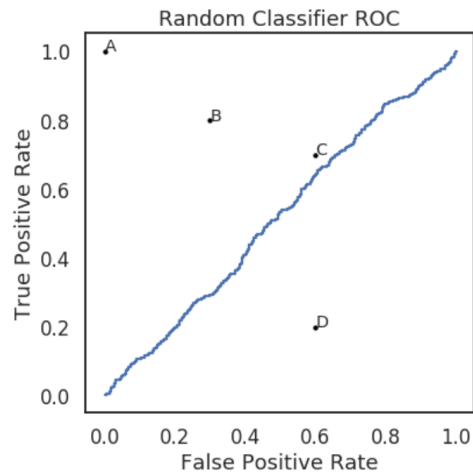
y	0	0	0	0	0	1	1	1	1	1
\hat{y}	0	1	1	1	1	1	1	0	0	0

Determine each of the following quantities.

- The number of true positives
- The number of false negatives
- The precision of our classifier. Write your answer as a simplified fraction.

ROC Curves

7. State whether the following claims are true or false. If false, provide a reason or correction.



- (a) Point A (0, 1) represents our ideal classifier.
- (b) Point C performs well compared to a classifier that guesses each class randomly.
- (c) The classifier at Point B performs better than the one at Point D.