



Calculus 3 Workbook

Approximating triple integrals

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MATH

MIDPOINT RULE FOR TRIPLE INTEGRALS

- 1. Use the midpoint rule to approximate the value of the triple integral, using boxes with sides $2 \times 2 \times \pi$.

$$\int_{-2}^2 \int_0^4 \int_{-2\pi}^{2\pi} x^2 y \cos z \, dz \, dy \, dx$$

- 2. Use the midpoint rule to approximate the value of the triple integral, where D is the cube with opposite corners $(0, 1, -1)$ and $(4, 5, 3)$. Use cubes with side length 2.

$$\iiint_D \log_2((x+1)^5 y^2 (z+2)) \, dV$$

- 3. Use the midpoint rule to approximate the value of the improper triple integral. Use cubes with side length 1.

$$\int_0^1 \int_0^1 \int_0^\infty \log_4(x) \frac{(y-1)^3}{z^2} \, dz \, dy \, dx$$



