Topic: Describing a region in three dimensional space

**Question**: Describe the surface in three-dimensional space.

$$x + y = 1$$

### **Answer choices:**

- A horizontal plane that's parallel to the z-axis and intersects the xyplane in the line x + y = 1.
- B A horizontal plane that's perpendicular to the z-axis and intersects the xy-plane in the line x + y = 1.
- C A vertical plane that's perpendicular to the z-axis and intersects the xy-plane in the line x + y = 1.
- D A vertical plane that's parallel to the z-axis and intersects the xyplane in the line x + y = 1.



#### Solution: D

The first thing we can see with our region x + y = 1 is that there's no z element. This means that our region has no intersection with the z-axis which means that our region is a plane that's parallel to the z-axis. Next we can solve for the x- and y-intercepts.

The *x*-intercept occurs where y = 0.

$$x + (0) = 1$$

$$x = 1$$

The *x*-intercept occurs at the point (1,0,0).

The *y*-intercept occurs where x = 0.

$$(0) + y = 1$$

$$y = 1$$

The y-intercept occurs at the point (0,1,0).

These two points show that the xy-plane is intersected in  $\mathbb{R}^3$  along the line x+y=1.

Pulling together all of this information we can see that the surface in  $\mathbb{R}^3$  of x+y=1 is a vertical plane that's parallel to the z-axis and intersects the xy-plane in the line x+y=1.

Topic: Describing a region in three dimensional space

**Question**: Describe the surface in three-dimensional space.

$$x + z = 4$$

# **Answer choices:**

- A plane that's parallel to the y-axis and intersects the xz-plane in the line x + z = 4.
- B A plane that's parallel to the z-axis and intersects the xy-plane in the line x + z = 4.
- C A plane that's parallel to the *x*-axis and intersects the *xz*-plane in the line x + z = 4.
- D A plane that's parallel to the *x*-axis and intersects the *yz*-plane in the line x + z = 4.



## Solution: A

The first thing we can see with our region x + z = 4 is that there's no y element. This means that our region has no intersection with the y-axis which means that our region is a plane that's parallel to the y-axis. Next we can solve for the x- and z-intercepts.

The *x*-intercept occurs where z = 0.

$$x + (0) = 4$$

$$x = 4$$

The *x*-intercept occurs at the point (4,0,0).

The *z*-intercept occurs where x = 0.

$$(0) + z = 4$$

$$z = 4$$

The y-intercept occurs at the point (0,0,4).

These two points show that the xz-plane is intersected in  $\mathbb{R}^3$  along the line x+z=4.

Pulling together all of this information we can see that the surface in  $\mathbb{R}^3$  of x+z=4 is a plane that is parallel to the y-axis and intersects the xz-plane in the line x+z=4.

Topic: Describing a region in three dimensional space

Question: Describe the surface in three-dimensional space.

$$2y + z = -6$$

### **Answer choices:**

- A horizontal plane that's parallel to the z-axis and intersects the xyplane in the line 2y + z = -6.
- B A plane that's parallel to the *x*-axis and intersects the *yz*-plane in the line 2y + z = -6.
- C A vertical plane that's parallel to the *x*-axis and intersects the *xy*-plane in the line 2y + z = -6.
- D A plane that's parallel to the y-axis and intersects the xz-plane in the line 2y + z = -6.



### Solution: B

The first thing we can see with our region 2y + z = -6 is that there's no x element. This means that our region has no intersection with the x-axis which means that our region is a plane that's parallel to the x-axis. Next we can solve for the y- and z-intercepts.

The y-intercept occurs where z = 0.

$$2y + (0) = -6$$

$$y = -3$$

The *x*-intercept occurs at the point (0, -3,0).

The z-intercept occurs where y = 0.

$$2(0) + z = -6$$

$$z = -6$$

The y-intercept occurs at the point (0,0,-6).

These two points show that the yz-plane is intersected in  $R^3$  along the line 2y + z = -6.

Pulling together all of this information we can see that the surface in  $R^3$  of 2y + z = -6 is a plane that's parallel to the *x*-axis and intersects the *yz*-plane in the line 2y + z = -6.