



Calculus 3 Workbook

Cross products

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MATH

CROSS PRODUCT OF TWO VECTORS

- 1. Find the vector \vec{a} given that $\vec{a} \times \vec{b} = \vec{c}$, where $\vec{a} = \langle 1, a_2, a_3 \rangle$, $\vec{b} = \langle 3, 1, 1 \rangle$, and $\vec{c} = \langle 1, 2, -5 \rangle$.

- 2. Find the cross product $\vec{a} \times \vec{a}$ for an arbitrary vector \vec{a} .

- 3. Find the cross product $\vec{a} \times \text{proj}_{xy} \vec{a}$, where $\vec{a} = \langle 4, 5, -3 \rangle$ and $\text{proj}_{xy} \vec{a}$ is the vector projection of the vector \vec{a} onto the xy -plane.



VECTOR ORTHOGONAL TO THE PLANE

- 1. Find the vector orthogonal to the plane which passes through the point $A(2,3,1)$ and the z -axis.

- 2. Find the equation of the plane that passes through the point D and is parallel to the plane ABC , if $A(1,2,-2)$, $B(1,4,3)$, $C(-5,3,-1)$, and $D(2,-4,7)$.

- 3. Find the equation of the line that passes through the point $A(-2,3,4)$ and is orthogonal to the plane that includes the vectors $\vec{a} = \langle 2,4,0 \rangle$ and $\vec{b} = \langle -1,1,2 \rangle$.



VOLUME OF THE PARALLELEPIPED FROM VECTORS

- 1. Find the height of the parallelepiped given that its volume is 670, and that the vectors $\vec{a} = \langle 1, 0, -1 \rangle$ and $\vec{b} = \langle 2, 3, 5 \rangle$ are the adjacent edges of its base.

- 2. Find the volume of the tetrahedron whose adjacent edges are the vectors $\vec{a} = \langle 0, 0, 3 \rangle$, $\vec{b} = \langle 2, 1, 4 \rangle$, and $\vec{c} = \langle -1, -2, 1 \rangle$.

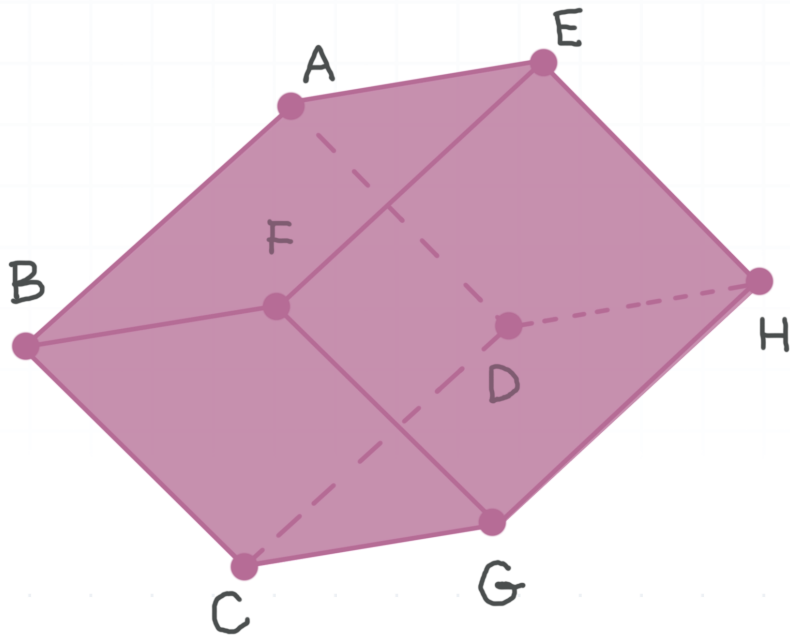
- 3. Find the value of p such that the volume of the parallelepiped with adjacent edges $\vec{a} = \langle 0, 2, 3 \rangle$, $\vec{b} = \langle 1, -2, 1 \rangle$, and $\vec{c} = \langle p, p, p \rangle$ is equal to 63.



VOLUME OF THE PARALLELEPIPED FROM ADJACENT EDGES

■ 1. Find the volume of tetrahedron $ABCD$, given $A(2,0,3)$, $B(-1,1,3)$, $C(4,5,-2)$, and $D(2,2,3)$.

■ 2. Find the volume of parallelepiped $ABCDEFGH$, given $A(1,2,2)$, $B(-1,-2,0)$, $F(4,3,-1)$, and $G(5,6,-4)$.



■ 3. Find the volume of the parallelepiped with base $ABCD$ and height 5, if $A(3,3,3)$, $B(0,-2,-2)$, and $C(-3,1,0)$.



SCALAR TRIPLE PRODUCT TO PROVE VECTORS ARE COPLANAR

- 1. Find the value of the parameter p such that the vectors $\vec{a} = \langle 1, 3, -1 \rangle$, $\vec{b} = \langle 2, 2, 2 \rangle$, and $\vec{c} = \langle 0, -1, p \rangle$ are coplanar.

- 2. Check if the vectors $\vec{a} = \langle 1, 1, 0 \rangle$, $\vec{b} = \langle 0, 1, 1 \rangle$, and $\vec{c} = \langle 1, 0, -1 \rangle$ are coplanar. If they are, find the equation of the plane, assuming that the initial point of the vectors is the origin.

- 3. Check if the points $A(0, 0, 1)$, $B(2, 0, 3)$, $C(2, 3, 0)$, and $D(3, 2, 2)$ lie in the same plane.



