

**Name:****LumiNUS Account:****Email:****NRIC / Passport / NUS Matriculation No.:**

(Choose and provide one applicable)

Institute of Systems Science  
National University of Singapore

## GRADUATE CERTIFICATE INTELLIGENT REASONING SYSTEMS

### Assessment

Subject: Machine Reasoning

### SECTION A

Question	Marks
1	/1.0
TOTAL	/1.0

### Instructions for Paper

Duration: Five minutes reading  
Duration: Fifteen minutes exam

**This is an OPEN BOOK examination. This examination paper consists of one Section and one Question. You are to answer ALL questions. There are a total of 1.0 Mark for this paper.**

1. The first **5** minutes are for reading and understanding the questions in this examination paper. You must **NOT** answer any questions using any writing instrument during this time.
2. Read **ALL** instructions before answering any of the examination questions.
3. Write your Student ID number on the **front page** of this examination paper in the box provided.
4. This is an **Open Book** examination. If you wish, you may use reference materials to answer a question. Reference materials can be *books, manuals, handouts* or *notes*.
5. Answers are to be written **only** in this **examination paper** and any **attachments** provided and will be considered for credit. Answers written in any appendices will **NOT** be marked.
6. Use a pen for writing your answers. Pencil may only be used for drawing diagrams and writing program code.
7. Non-programmable calculators may be used if required. **However, computers of any form (laptops, tablets, smart watches etc.) are not permitted to be brought into the examination hall.**
8. State clearly any assumptions you make in answering any question where you feel the requirement is not sufficiently clear.
9. At the end of the examination:
  - a) Hand-in the examination paper for **each** section **separately**, any appendices and attachments.
  - b) You are **not** allowed to remove the examination paper, appendices or attachments from the examination hall.

**REMEMBER:**

- ***This is an OPEN BOOK exam.***
- ***There are a total of **1.0** Mark for this paper.***
- ***You are required to answer ALL questions.***
- ***State clearly any assumptions you make in answering any question where you feel the requirement is not sufficiently clear.***

**SECTION A****Question 1**

(Total: 1.0 Mark)

With the current low interest rate for loans, **ABC Bank** is receiving many housing loan applications every day. The following regulations have been used by the Bank for housing loan approval since 2008:

- (1) The loan will be rejected if the applicant currently has another housing loan with more than 50% of the loan amount unpaid.
- (2) The loan will be rejected if the applicant has a bad credit history within the last three years.
- (3) The loan will be approved if the applicant currently does not have an unpaid housing loan and does not have a bad credit history within the last three years.
- (4) The loan will be partially approved if the applicant currently has another housing loan with less than 25% of the loan amount unpaid, and does not have a bad credit history within the last three years.

Based on these regulations, for  $x \in X$ , where  $X$  is the group of applicants to be assessed, the following **binary (true or false)** predicates have been defined:

<b>unpaid_big(<math>x</math>)</b>	the person $x$ has a loan with > 50% unpaid amount.
<b>unpaid_small(<math>x</math>)</b>	the person $x$ has a loan with < 25% unpaid amount.
<b>bad_credit(<math>x</math>)</b>	the person $x$ has a bad credit history within the last three years.
<b>no_loan(<math>x</math>)</b>	the person $x$ does not have an unpaid housing loan at the moment.
<b>reject(<math>x</math>)</b>	the housing loan application from person $x$ is rejected.
<b>approval(<math>x</math>)</b>	the housing loan application from person $x$ is approved.
<b>partial(<math>x</math>)</b>	the housing loan application from person $x$ is partially approved.

(Note: For all these predicates, no details of the loan amount are needed.)

**Answer the following questions:**

**1.1** Translate the regulations into WHEN/THEN rules.

*For example: WHEN unpaid\_big(x) THEN reject(x)*

(0.5 Mark)

[Answer]

- (1) WHEN unpaid\_big(x) THEN reject(x)
- (2) WHEN bad\_credit(x) THEN reject(x)
- (3) WHEN no\_loan(x) AND  $\neg$ bad\_credit(x) THEN approval(x)
- (4) WHEN unpaid\_small(x) AND  $\neg$ bad\_credit(x) THEN partial(x)

**1.2** Mr A is currently applying for a housing loan with ABC Bank. Given that *Mr A has a current loan with 20% of the loan amount unpaid, and had a bad credit history ten years ago*, prove that *the housing loan application for Mr A will be partially approved* is true. Show your reasoning steps: rule firing sequences based on matching conditions.

(0.5 Mark)

[Answer]

Hypothesis: Housing loan application for Mr A will be partially approved.

**1) Forward Chaining**

Fact1: 20% of loan amount unpaid  $\rightarrow$  unpaid\_small(Mr A)

Fact2: Bad credit history ten years ago  $\rightarrow$  bad\_credit(Mr A) is false  $\rightarrow \neg$  bad\_credit(Mr A)

Pattern Matching: unpaid\_small(MrA) and  $\neg$  bad\_credit(Mr A)  $\rightarrow$  partial (Mr A)

The above facts will fire rule 4 and the loan for Mr A will be partially approved.

Hypothesis is TRUE.

**2) Backward Chaining**

Facts:

- (a) unpaid\_small(Mr A) – since Mr A has loan of <25% unpaid amount
- (b)  $\neg$ bad\_credit(Mr A)

Rules:

- (1) WHEN unpaid\_big(x) THEN reject(x)
- (2) WHEN bad\_credit(x) THEN reject(x)
- (3) WHEN no\_loan(x) AND  $\neg$ bad\_credit(x) THEN approval(x)
- (4) WHEN unpaid\_small(x) AND  $\neg$ bad\_credit(x) THEN partial(x)

Based on matching conditions of facts (a) and (b), only conditions for rule (4) matches. Hence resulting in partial(Mr A)  $\Rightarrow$  housing loan application from person Mr A is partially approved.

Rules:

- (1) unpaid\_big(x)  $\rightarrow$  reject(x)
- (2) bad\_credit(x)  $\rightarrow$  reject(x)
- (3) no\_loan(x)  $\wedge$   $\neg$ bad\_credit(x)  $\rightarrow$  approval(x)
- (4) unpaid\_small(x)  $\wedge$   $\neg$ bad\_credit(x)  $\rightarrow$  partial(x)

Converted rules:

- (1)  $\neg$ unpaid\_big(x)  $\vee$  reject(x)
- (2)  $\neg$ bad\_credit(x)  $\vee$  reject(x)
- (3)  $\neg$ (no\_loan(x)  $\wedge$   $\neg$ bad\_credit(x))  $\vee$  approval(x)  $\Rightarrow$   $\neg$ no\_loan(x)  $\vee$  bad\_credit(x)  $\vee$  approval(x)
- (4)  $\neg$ (unpaid\_small(x)  $\wedge$   $\neg$ bad\_credit(x))  $\vee$  partial(x)  $\Rightarrow$   $\neg$ unpaid\_small(x)  $\vee$  bad\_credit(x)  $\vee$  partial(x)

Prove hypothesis a:  $\text{partial}(\text{Mr A})$

Prove refutation  $\neg a: \neg \text{partial}(\text{Mr A})$

$\text{KB} \wedge \neg a:$

- (1)  $\neg \text{unpaid\_big}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (2)  $\neg \text{bad\_credit}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (3)  $\neg \text{no\_loan}(\text{Mr A}) \vee \text{bad\_credit}(\text{Mr A}) \vee \text{approval}(\text{Mr A})$
- (4)  $\neg \text{unpaid\_small}(\text{Mr A}) \vee \text{bad\_credit}(\text{Mr A}) \vee \text{partial}(\text{Mr A}) \wedge \neg \text{partial}(\text{Mr A})$

- (1)  $\neg \text{unpaid\_big}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (2)  $\neg \text{bad\_credit}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (3)  $\neg \text{no\_loan}(\text{Mr A}) \vee \text{bad\_credit}(\text{Mr A}) \vee \text{approval}(\text{Mr A})$
- (4)  $\neg \text{unpaid\_small}(\text{Mr A}) \vee \text{bad\_credit}(\text{Mr A}) \wedge \neg \text{bad\_credit}(\text{Mr A})$

- (1)  $\neg \text{unpaid\_big}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (2)  $\neg \text{bad\_credit}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (3)  $\neg \text{no\_loan}(\text{Mr A}) \vee \text{bad\_credit}(\text{Mr A}) \vee \text{approval}(\text{Mr A})$
- (4)  $\neg \text{unpaid\_small}(\text{Mr A}) \wedge \text{unpaid\_small}(\text{Mr A})$

- (1)  $\neg \text{unpaid\_big}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (2)  $\neg \text{bad\_credit}(\text{Mr A}) \vee \text{reject}(\text{Mr A})$
- (3)  $\neg \text{no\_loan}(\text{Mr A}) \vee \text{bad\_credit}(\text{Mr A}) \vee \text{approval}(\text{Mr A})$
- (4)  $\{\}$

**Refutation is unsatisfiable**

**Proof that hypothesis is true**

- $\text{Partial}(\text{Mr A})$

## **END OF ASSESSMENT PAPER**