PC2232 Physics for Electrical Engineers: Tutorial 4

Question 1: Photoelectric effect

A 2.50 W beam of light of wavelength 124 nm falls on a metal surface. You observe that the maximum kinetic energy of the ejected electrons is 4.16 eV. You may assume that each photon in the beam ejects a photoelectron.

- (a) What is the work function (in eV) of this metal?
- (b) How many photoelectrons are ejected each second from the metal?
- (c) If the power of the light beam, but not its wavelength were reduced by half, what would be the answer to part (b)?
- (d) If the wavelength of the beam, but not its power, were reduced by half, what would be the answer to part (b)?
- (e) Explain whether the maximum kinetic energy of the photoelectrons is changed in parts (c) and (d).

Question 2: Compton Effect

- (a) Derive an expression for the total shift in photon wavelength after two successive Compton scatterings from electrons at rest. The photon is scattered by an angle θ_1 in the first scattering and θ_2 in the second.
- (b) In general, is the total shift in wavelength produced by two successive scatterings of angle $\theta/2$ the same as by a single scattering of θ ? If not, are there any specific values of θ , other than $\theta = 0$ for which the total shifts are the same?
- (c) Use the result of part (a) to calculate the total wavelength shift produced by two successive Compton scatterings of 30.0° each. Express your answer in terms of h/mc.
- (d) What is the wavelength shift produced by a single Compton scattering of 60.0°? Compare to the answer in part (c).

Question 3: Atomic Spectra

What is the radius of the first Bohr orbit and ionization energy in each of the following:

- (a) He⁺ ion,
- (b) Li^{2+} ion, and
- (c) Be^{3+} ion?

Question 4: Atomic Spectra

A non-relativistic particle with mass m is held in circular orbit around the origin by an attractive force F(r) = -Dr, where D is a positive constant. Use the Bohr model idea that only certain values of the angular momentum are allowed to answer the following questions.

- (a) What are the allowed values of the orbital radius?
- (b) What are the allowed energies? (Let the potential energy be zero at r=0)
- (c) If the particle is excited, it will decay back down to the ground state by emitting one or more photons. What are the possible photon energies?
- (d) Describe a possible physical situation in which this problem corresponds.

Question 5: Atomic Spectra (Optional)

- (a) Show that in the Bohr model, the frequency of revolution of an electron in its circular orbit around a stationary hydrogen nucleus is $f = me^4/4\epsilon_0^2 n^3 h^3$.
- (b) In classical physics, the frequency of revolution of the electron is equal to the frequency of the radiation it emits. Show that when n is very large, the frequency of revolution does indeed equal the radiation frequency calculated for a transition from $n_1 = n + 1$ to $n_2 = n$.

(This illustrates Bohr's correspondence principle, which is often used as a check on quantum calculations. When n is small, quantum physics gives results that are very different from those of classical physics. When n is large, the differences are not significant, and the two methods then "correspond". In fact, when Bohr first tackled the hydrogen atom problem, he sought to determine f as a function of n such that it would correspond to classical results for large n.)