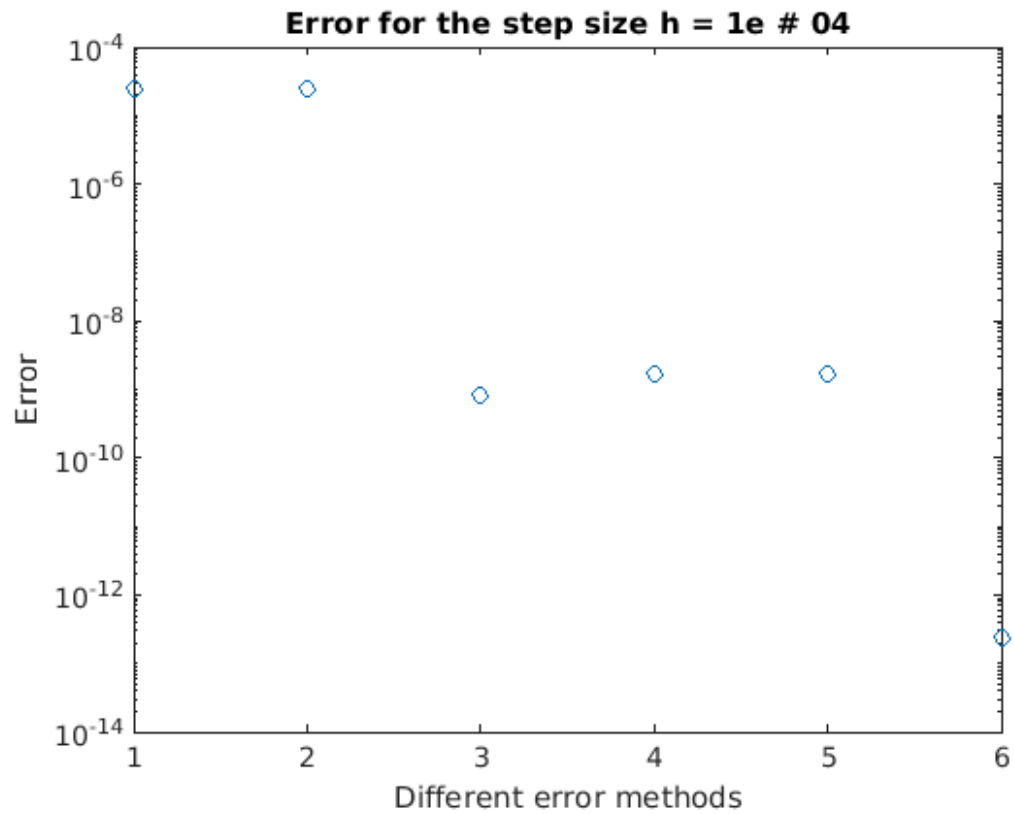


---

% Q1

```
% Matlab script to calculate numerical derivative of arctan(x)
a = 1;
trueVal = 1/(1 + a.^2);
h = 1e-4;
% Forward diff.
fwdDiff = (f(a + h) - f(a))/h;
errFwd = abs(trueVal - fwdDiff);
disp(['Error in forward diff: ', num2str(errFwd)]);
% Backward diff.
bckDiff = (f(a) - f(a - h))/h;
errBck = abs(trueVal - bckDiff);
disp(['Error in backward diff: ', num2str(errBck)]);
% Central diff.
cntrDiff = (f(a + h) - f(a - h))/(2*h);
errCntr = abs(trueVal - cntrDiff);
disp(['Error in central diff.: ', num2str(errCntr)]);
% Improved Forward diff.
iFwdDiff = (-f(a + 2*h) + 4*f(a + h) - 3*f(a))/(2*h);
errIFwd = abs(trueVal - iFwdDiff);
disp(['Error in improved forward diff.: ', num2str(errIFwd)]);
% Improved Backward diff.
iBckDiff = (3*f(a) - 4*f(a - h) + f(a - 2*h))/(2*h);
errIBck = abs(trueVal - iBckDiff);
disp(['Error in improved backward diff.: ', num2str(errIBck)]);
% Improved Central diff.
iCntrDiff = (8*f(a + h) - 8*f(a - h) - f(a + 2*h) + f(a - 2*h))/(12*h);
errICntr = abs(trueVal - iCntrDiff);
disp(['Error in improved central diff.: ', num2str(errICntr)]);
% Plotting graph for different method
semilogy([errFwd, errBck, errCntr, errIFwd, errIBck, errICntr], 'o')
title('Error for the step size h = 1e # 04')
ylabel('Error')
xlabel('Different error methods')
% Defining function for arctan(x)
function fx = f(x)
    fx = atan(x);
end
```

```
Error in forward diff: 2.4999e-05
Error in backward diff: 2.5001e-05
Error in central diff.: 8.3317e-10
Error in improved forward diff.: 1.6665e-09
Error in improved backward diff.: 1.6682e-09
Error in improved central diff.: 2.4014e-13
```



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