## A Comprehensive Note on Machine Learning $^{1}$

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## Preface

The primary purpose of this document is educational, specifically for the courses I teach (CSE 474/574 Introduction to Machine Learning, CSE 455/555 Pattern Recognition, and CSE 676 Deep Learning), as well as for my personal reference. A substantial portion of the material herein is directly referenced or adapted from established texts and sources, and is not claimed as original content. This document is intended as a supplementary teaching and learning resource and is not authorized for commercial use, redistribution, or sale without my explicit consent.

The majority of the material referenced comes from the following sources:

- [1] Zhang, Aston, et al. Dive into deep learning. Cambridge University Press, 2023.
- [2] Bishop, C. M., & Nasrabadi, N. M. (2006). Pattern recognition and machine learning (Vol. 4, No. 4, p. 738). New York: Springer.
- [3] Hart, P. E., Stork, D. G., & Duda, R. O. (2000). Pattern classification. Hoboken: Wiley.
- [4] Burkov, A. (2019). The hundred-page machine learning book (Vol. 1, p. 32). Quebec City, QC, Canada: Andriy Burkov.
- [5] Burkov, A. (2020). Machine learning engineering (Vol. 1). Montreal, QC, Canada: True Positive Incorporated.

All other referenced materials and sources are cited in the bibliography section of this document. This compilation is intended to provide a comprehensive overview and guide for students and practitioners of machine learning, drawing upon a wide range of foundational and contemporary sources in the field.

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# Part I

# **Basic Machine Learning**

## Chapter 1

#### Introduction

#### 1.1 What is Machine Learning

Machine learning is a subfield of computer science that is concerned with building algorithms which to be useful, rely on a collection of examples of some phenomenon.

• The examples come from nature, handcrafted by humans or generated by another algorithms.

Machine learning can also be defined as the process of solving a practical problem by

- 1. gathering a dataset
- 2. algorithmically building a statistical model based on the dataset.

The statistical model is assumed to be used somehow to solve the practical problem.

#### 1.2 Types of Learninig

Learning can be supervised, semi-supervised, unsupervised and reinforcement.

#### 1.2.1 Supervised Learning

In supervised learning, the dataset is the collection of labeled examples  $\{(\mathbf{x}_i, y_i)\}_{i=1}^N$ 

- Each element  $\mathbf{x}_i$  among N is called a **feature vector**. A feature vector is a vector in which each dimension j = 1, ..., D contains a value that describes the example somehow. That value is called a **feature** and is denoted as  $x^{(j)}$ .
- The label  $y_i$  can be either an element belonging to a finite set of classes 1, 2, ..., C, or a real number, or a more complex structure, like a vector, a matrix, a tree or a graph. Unless otherwise stated,  $y_i$  is either one of a finite set of classes or a real number.

The goal of a **supervised learning algorithm** is to use the dataset to produce a **model** that takes a feature vector  $\mathbf{x}$  as input and outputs information that allows deducing the label for this feature vector.

#### 1.2.2 Unsupervised Learning

In unsupervised learning, the dataset is a collection of unlabeled examples  $\{\mathbf{x}_i\}_{i=1}^N$ . The goal of an unsupervised learning algorithm is to create a model that takes a feature vector  $\mathbf{x}$  as input and

either transforms it into another vector or into a value that can be used to solve a practical problem. For example,

- in **clustering**, the model returns the id of the cluster for each feature vector in the dataset.
- in **dimensionality reduction**, the output of the model is a feature vector that has fewer features than the input **x**;
- in **outlier detection**, the output is a real number that indicates how  $\mathbf{x}$  is different from a "typical" example in the dataset.

#### 1.2.3 Semi-Supervised Learning

In semi-supervised learning, the dataset contains both labeled and unlabeled examples.

• Usually the quantity of unlabeled examples is much higher than the number of labeled examples.

The goal of **semi-supervised learning algorithm** is the same as the goal of the supervised learning algorithm.

• The hope here is that using many unlabeled examples can help the learning algorithm to find a better model.

How does the learning benefit from adding more unlabeled examples?

• By adding unlabeled examples, you add more information about your problem: a larger sample reflects better the probability distribution the data we labeled came from.

#### 1.2.4 Reinforcement Learning

**Reinforcement learning** is a subfield of machine learning where the machine "lives" in an environment and is capable of perceiving the *state* of that environment as vector of features.

• The machine can execute *actions* in every state. Different actions bring different *rewards* and could also move the machine to another state of the environment.

The goal of a reinforcement learning algorithm is to learn a *policy*. A policy is a function (similar to the model in supervised learning) that takes the feature vector of a state as input and outputs an optimal action to execute in that state. The action is optimal if it maximizes the *expected average reward*.

#### 1.3 How Supervised Learning Works

Supervised learning is the type of machine learning most frequently used in practice. The supervised learning process starts with gathering the data. The data for supervised learning is a collection of pairs (input,output).

- Inputs could be anything, for example, email messages, pictures, or sensor measurements.
- Outputs are usually real numbers, or labels (e.g. "spam", "not\_spam", etc). In some cases, outputs are vectors (e.g., four coordinates of the rectangle around a person on the picture), sequences (e.g. ["adjective", "adjective", "noun"] for the input "big beautiful car") or have some other structure.

You want to solve spam detection using supervised learning. First, you gather the data of 10,000 email messages and you have your label "spam" or "not\_spam" for each message. With the data at hand, you have to represent each message using a feature vector.

A common approach it to use **bag of words**, is to take a dictionary of English words (e.g. 20,000 alphabetically sorted words) and stipulate that in our feature vector:

- the first feature is equal to 1 if the email message contains the word "a"; other wise, this feature is 0:
- the second feature is equal to 1 if the email message contains the word "aaron"; otherwise, this feature equals 0;
- ...
- the feature at position 20,000 is equal to 1 if the email message contains the word "zulu"; otherwise, this feature is equal to 0.

You repeat the above procedure for every email message in our collection, which gives us 10,000 feature vectors (each vector having the dimensionality of 20,000) and a label ("spam"/"not\_spam").

We successfully converted input data into machine-readable type, but the output labels are still in the form of human-readable text. Some learning algorithms require transforming labels into numbers. For demonstration purpose, we will use a supervised learning algorithm called **Support Vector Machine** (SVM). This algorithm requires the positive label (in our case it's "spam") has the numeric value of +1 (one), and the negative label ("not\_spam") has the value of -1 (minus one).

You now have a **dataset** and a **learning algorithm**, you will need to apply the learning algorithm to the dataset to get the **model**.

SVM sees every feature vector as a point in a high-dimensional space (in our case, space is 20,000 – dimensional). The algorithm puts all feature vectors on an imaginary 20,000-dimensional plot and draws an imaginary 19,999 – dimensional line (a *hyperplane*) that separates examples with positive labels from examples with negative labels. In machine learning, the boundary separating the examples of different classes is called the **decision boundary**.

Hyperplane is denoted by two parameters

$$\mathbf{w}\mathbf{x} - b = 0$$
,

- a real-valued vector  $\mathbf{w}$  of the same dimensionality as our input vector  $\mathbf{x}$ , and a real number b
- $\mathbf{w}\mathbf{x} = w^{(1)}x^{(1)} + w^{(2)}x^{(2)} + \ldots + w^{(D)}x^{(D)}$ , and D is the number of dimensions of the feature vector  $\mathbf{x}$ .

The predicted label for some input feature vector  $\mathbf{x}$  is given like this:

$$y = \operatorname{sign}(\mathbf{wx} - b),$$

where sign is a mathematical operator that takes any value as input and returns +1 if the input is a positive number or -1 if the input is a negative number.

The goal of the learning algorithm, SVM in this case, is to leverage the dataset and find the optimal values  $\mathbf{w}^*$  and  $b^*$  for parameters  $\mathbf{w}$  and b. Once the learning algorithm identifies these optimal values, the **model**  $f(\mathbf{x})$  is then defined as:

$$f(\mathbf{x}) = \operatorname{sign}\left(\mathbf{w}^*\mathbf{x} - b^*\right)$$

How do we find these optima values? It turns out it is an optimization problem. Machines are good at optimizing functions <u>under constraints</u>.

$$\mathbf{w}\mathbf{x}_i - b \ge +1$$
 if  $y_i = +1$   
 $\mathbf{w}\mathbf{x}_i - b \le -1$  if  $y_i = -1$ 

It will also be ideal if the hyperplane separates positive examples from negative ones with the largest **margin**. The margin is the distance between the closestt examples of two classes, as defined by the decision boundary. A large margin contributes to a better **generalization**, that is how well the model will classify new examples in the future.

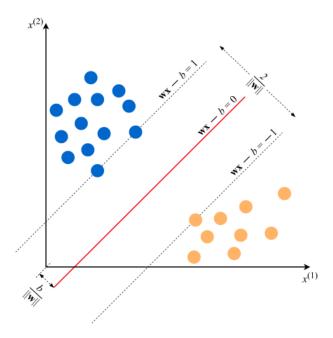


Figure 1.1: An example of an SVM model for two-dimensional feature vectors.

Let's do some quick refreshment

#### Distance Formulas in Euclidean Space

#### Distance Between Two Points

In two-dimensional space, for points  $P_1(x_1, y_1)$  and  $P_2(x_2, y_2)$ , the distance is calculated as:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

#### Distance From a Point to a Line

In two-dimensional space, for a line defined by ax + by + c = 0 and a point  $P(x_0, y_0)$ , the distance is:

$$d = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

#### Distance Between Two Parallel Lines

For two parallel lines with equations  $ax + by + c_1 = 0$  and  $ax + by + c_2 = 0$ , the distance is:

$$D = \frac{|c_2 - c_1|}{\sqrt{a^2 + b^2}}$$

So, the optimization problem that we want the machine to solve looks like this:

**Minimize**  $\|\mathbf{w}\|$  subject to  $y_i(\mathbf{w}\mathbf{x}_i - b) \ge 1$  for i = 1, ..., N. The expression  $y_i(\mathbf{w}\mathbf{x}_i - b) \ge 1$  is just a compact way to write the above two constraints.

More on SVMs later. This simple example should give you an idea how supervised learning works.

#### 1.4 Why the Model Works on New Data

Let's refer to Figure 1.1. If two classes are separable from one another by a decision boundary, then, obviously, examples that belong to each class are located in two different subspaces which the decision boundary creates.

If the examples used for training were selected randomly, independently of one another, and following the same procedure, then statistically, it is *more likely* that the new negative example will be located on the plot somewhere not too far from other negative examples. The idea goes with the positive examples as well.

## Chapter 2

#### Notation and Definition

#### 2.1 Notation

We will review all the necessary notation and mathematics for us to continue the journey of Machine Learning.

#### 2.1.1 Data Structure

A scalar is simple numerical value, like 15 or -3.25, denoted by an italic letter, like x or a. A vector is an ordered list of scalar values, called attributes. Vector is denoted by bold character  $\mathbf{x}$  or  $\mathbf{w}$ . A matrix is a rectangular array of numbers arranged in rows and columns.

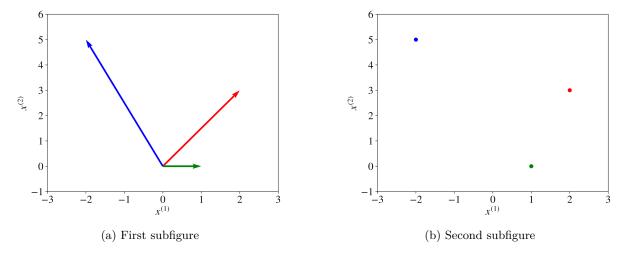


Figure 2.1: Three vectors visualized as directions and as points.

A matrix is a rectangular array of numbers arranged in rows and columns, which are denoted with bold capital letters, such as **A** or **W**. A **set** is an unordered collection of unique elements. We denote a set as a calligraphic capital character, for example,  $\mathcal{S}$ . When an element belongs to a set  $\mathcal{S}$ , we write  $x \in \mathcal{S}$ . We can obtain a new set  $\mathcal{S}_3$  as an **intersection** of two set  $\mathcal{S}_1$  and  $\mathcal{S}_2$ , written as  $\mathcal{S} \leftarrow \mathcal{S}_1 \cap \mathcal{S}_2$ . Also we can obtain a new set by **union**,  $\mathcal{S}_3 \leftarrow \mathcal{S}_1 \cup \mathcal{S}_2$ .

#### 2.1.2 Capital Sigma Notation

The summation over a collection  $\mathcal{X} = \{x_1, x_2, \dots, x_{n-1}, x_n\}$  or over the attributes of a vector  $\mathbf{x} = [x^{(1)}, x^{(2)}, \dots, x^{(m-1)}, x^{(m)}]$  is denoted like this:

$$\sum_{i=1}^{n} x_i \stackrel{\text{def}}{=} x_1 + x_2 + \ldots + x_{n-1} + x_n, \text{ or else: } \sum_{j=1}^{m} x^{(j)} \stackrel{\text{def}}{=} x^{(1)} + x^{(2)} + \ldots + x^{(m-1)} + x^{(m)}$$

The notation  $\stackrel{\text{def}}{=}$  means "is defined as".

#### 2.1.3 Capital Pi Notation

$$\prod_{i=1}^{n} x_i \stackrel{\text{def}}{=} x_1 \cdot x_2 \cdot \ldots \cdot x_{n-1} \cdot x_n$$

• A product of elements in a collection or attributes of a vector.

#### 2.1.4 Operations on Sets

Given the expression:

$$\mathcal{S}' \leftarrow \left\{ x^2 \mid x \in \mathcal{S}, x > 3 \right\}$$

This notation is used to define a derived set creation operator. It means that we create a new set S' by including the square of each element x from the set S, under the condition that x is greater than 3. In other words, S' is comprised of the squares of all elements in S which are greater than 3.

Additionally, the cardinality operator  $|\mathcal{S}|$  is used to denote the number of elements in the set  $\mathcal{S}$ . For example, if  $\mathcal{S} = \{1, 2, 4, 5\}$ , then  $\mathcal{S}' = \{16, 25\}$  as only 4 and 5 from  $\mathcal{S}$  satisfy the condition x > 3. The **cardinality**  $|\mathcal{S}|$  in this case would be 4.

#### 2.1.5 Operations on Vectors

**Vector Addition and Subtraction:** The sum and difference of two vectors  $\mathbf{x}$  and  $\mathbf{z}$  are defined component-wise as:

$$\mathbf{x} + \mathbf{z} = \left[ x^{(1)} + z^{(1)}, \dots, x^{(m)} + z^{(m)} \right]$$

$$\mathbf{x} - \mathbf{z} = \left[ x^{(1)} - z^{(1)}, \dots, x^{(m)} - z^{(m)} \right]$$

Example: For  $\mathbf{x} = [1, 2]$  and  $\mathbf{z} = [3, 4]$ ,

$$\mathbf{x} + \mathbf{z} = [1+3, 2+4] = [4, 6]$$

Scalar Multiplication: A vector multiplied by a scalar c results in a scaled vector:

$$\mathbf{x}c = \left[cx^{(1)}, \dots, cx^{(m)}\right]$$

Example: For  $\mathbf{x} = [1, 2]$  and c = 3,

$$\mathbf{x}c = [3 \times 1, 3 \times 2] = [3, 6]$$

**Dot Product:** The dot product of two vectors  $\mathbf{w}$  and  $\mathbf{x}$  is a scalar:

$$\mathbf{w}\mathbf{x} = \sum_{i=1}^{m} w^{(i)} x^{(i)}$$

2.1. NOTATION

Example: For  $\mathbf{w} = [1, 2]$  and  $\mathbf{x} = [3, 4]$ ,

$$\mathbf{wx} = 1 \times 3 + 2 \times 4 = 3 + 8 = 11$$

Matrix-Vector Multiplication: Multiplying a matrix  $\mathbf{W}$  by a vector  $\mathbf{x}$  yields another vector. For example:

$$\mathbf{W}\mathbf{x} = \begin{bmatrix} w^{(1,1)} & w^{(1,2)} & w^{(1,3)} \\ w^{(2,1)} & w^{(2,2)} & w^{(2,3)} \end{bmatrix} \begin{bmatrix} x^{(1)} \\ x^{(2)} \\ x^{(3)} \end{bmatrix}$$

$$\stackrel{\text{def}}{=} \begin{bmatrix} w^{(1,1)}x^{(1)} + w^{(1,2)}x^{(2)} + w^{(1,3)}x^{(3)} \\ w^{(2,1)}x^{(1)} + w^{(2,2)}x^{(2)} + w^{(2,3)}x^{(3)} \end{bmatrix}$$

$$= \begin{bmatrix} \mathbf{w}^{(1)}\mathbf{x} \\ \mathbf{w}^{(2)}\mathbf{x} \end{bmatrix}$$

Example: For

$$\mathbf{W} = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \text{ and } \mathbf{x} = \begin{bmatrix} 5 \\ 6 \end{bmatrix},$$

$$\mathbf{W}\mathbf{x} = \begin{bmatrix} 1 \times 5 + 2 \times 6 \\ 3 \times 5 + 4 \times 6 \end{bmatrix} = \begin{bmatrix} 17 \\ 39 \end{bmatrix}$$

**Transpose and Multiplication:** For the transpose of a vector  $\mathbf{x}$  denoted  $\mathbf{x}^{\top}$ , and a matrix  $\mathbf{W}$ , the multiplication  $\mathbf{x}^{\top}\mathbf{W}$  is given by:

$$\mathbf{x}^{\top}\mathbf{W} = \begin{bmatrix} x^{(1)} & x^{(2)} \end{bmatrix} \begin{bmatrix} w^{(1,1)} & w^{(1,2)} & w^{(1,3)} \\ w^{(2,1)} & w^{(2,2)} & w^{(2,3)} \end{bmatrix}$$

$$\stackrel{\text{def}}{=} \begin{bmatrix} w^{(1,1)}x^{(1)} + w^{(2,1)}x^{(2)}, w^{(1,2)}x^{(1)} + w^{(2,2)}x^{(2)}, w^{(1,3)}x^{(1)} + w^{(2,3)}x^{(2)} \end{bmatrix}$$

Example: For

$$\mathbf{x} = \begin{bmatrix} 7 \\ 8 \end{bmatrix} \text{ and } \mathbf{W} = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix},$$

$$\mathbf{x}^{\top} \mathbf{W} = \begin{bmatrix} 7 \times 1 + 8 \times 4, 7 \times 2 + 8 \times 5, 7 \times 3 + 8 \times 6 \end{bmatrix} = \begin{bmatrix} 39, 54, 69 \end{bmatrix}$$

#### 2.1.6 Functions

#### Definition of a Function

A function is a relation that associates each element x of a set  $\mathcal{X}$ , known as the domain, to a single element y of another set  $\mathcal{Y}$ , known as the codomain. This relation is denoted as y = f(x), where f is the name of the function, x is the input or argument, and y is the output. The input variable is also referred to as the variable of the function.

Example: Consider the function  $f(x) = x^2$  defined on the domain  $\mathcal{X} = \mathbb{R}$ . For x = 2, the output is  $f(2) = 2^2 = 4$ .

#### Local and Global Minima

The function f(x) has a local minimum at x = c if  $f(x) \ge f(c)$  for every x in an open interval around c. An open interval, such as (0,1), includes all numbers between its endpoints but not the endpoints themselves. The smallest value among all local minima is known as the global minimum.

Example: In the function  $f(x) = (x-1)^2$ , the local (and global) minimum occurs at x=1 since  $f(x) \ge f(1) = 0$  for all x.

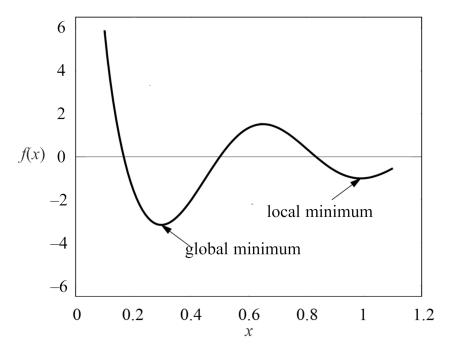


Figure 2.2: A local and a global minima of a function.

#### **Vector Functions**

A vector function, denoted  $\mathbf{y} = \mathbf{f}(x)$ , is a function that returns a vector  $\mathbf{y}$ . Its argument can be either a vector or a scalar.

Example: For the vector function  $\mathbf{f}(x) = [x, x^2]$ , with x = 2, the output is  $\mathbf{f}(2) = [2, 2^2] = [2, 4]$ .

#### 2.1.7 Max and Arg Max

Given a set of values  $\mathcal{A} = \{a_1, a_2, \dots, a_n\}$ , the operator  $\max_{a \in \mathcal{A}} f(a)$  returns the highest value of f(a) for all elements in the set  $\mathcal{A}$ . Conversely, the operator  $\max_{a \in \mathcal{A}} f(a)$  identifies the specific element a in the set  $\mathcal{A}$  that maximizes the function f(a).

In cases where the set is implicit or infinite, we can use the notation  $\max_a f(a)$  or  $\max_a f(a)$  respectively. Similarly, the operators min and arg min function in a comparable way, determining the lowest value of a function and the

#### 2.1.8 Assignment Operator

# Part II Advance Machine Learning

# Part III Convolution Neural Networks

## Part IV

# Adversarial Attacks and Training

### Chapter 3

## **Intriguing Properties of Neural Network**

Deep neural networks, known for their exceptional performance in speech and visual recognition tasks, exhibit two notable characteristics (Szegedy et al., 2013). First, the semantic information in their higher layers is embedded not in individual units but in the collective space they form. This insights shifts the focus from analyzing single neurons to considering the entire unit group to understand network processing. Second, these networks display a surprisingly sensitivity to minute, yet percisely tailored alternations (or perturbation). Such small changes can lead to incorrect outcomes. This vulnerability is not due to random noise; the same modifications can deceive different networks trained on a different subset of the dataset, to misclassify the same input.

#### 3.1 Introduction

Deep neural networks are powerful learning models that achieve excellent performance on visual and speech recognition problems because they can express arbitrary computation that consists of a modest number of massively parallel nonlinear steps. As the resulting computation is automatically discovered by backpropagation via supervised learning, it can be difficult to interpret and can have counter-intuitive properties.

The **first** property is concerned with the semantic meaning of individual units. It seems that the entire space of activation, rather than the individual units, that contains the bulk of the semantic information contrary to prior belief and the **second** property is concerned with the stability of neural networks with respect to small perturbation to their inputs. Apply an *imperceptible* non-random perturbation to a test image, it is possible to arbitrarily change the network's prediction. These perturbation are found by optimizing the input to maximize the prediction error. The perturbed examples are often called "adversarial examples"

#### 3.2 Framework

**Notation**  $x \in \mathbb{R}$  denotes an input image,  $\phi(x)$  is an activation values of some layer. (Szegedy et al., 2013) first examine properties of the image of  $\phi(x)$ , and then search for its blind spots.

# $\mathbf{Part}\ \mathbf{V}$

# Recurrent Neural Networks

## Part VI

# Transformers

## Part VII

# Artificial General Intelligence

## Chapter 4

## Continual Learning

#### 4.1 Introduction

Continual Learning is motivated by the fact that human and other organisms has the ability to adapt, accumulate and exploit knowledge. A common setting for continual learning is to learn a sequence of contents one by one and behave as if they were observed simultaneously (Wang et al., 2023). Each task learned throughout the life time can be new skills, new examples of old skills, different environments, etc. This attribute of continual learning makes it also referred to as incremental learning or lifelong learning.

Unlike conventional pipeline, where joint training is applied, continual learning is characterized by learning from dynamic data distributions. A major challenge is known as **catastrophic forgetting**, where adaptation to a new distribution generally results in a largely reduced ability to capture the old ones. This dilemma is a facet of the trade-off between **learning plasticity** and **memory stability**: an excess of the former interferes with the latter, and vice versa. A good continual learning algorithm should obtain a strong **generalizability** to accommodate distribution differences within and between tasks. As a naive baseline, retraining all old training samples (if allowed) makes it easy to address the above challenges, but creates huge computational and storage overheads (as well as potential privacy issues). In fact, continual learning is primarily intended to ensure **resource efficiency** of model updates, preferably close to learning only new training samples.

## Bibliography

Christian Szegedy, Wojciech Zaremba, Ilya Sutskever, Joan Bruna, Dumitru Erhan, Ian Goodfellow, and Rob Fergus. Intriguing properties of neural networks. arXiv preprint arXiv:1312.6199, 2013.

Liyuan Wang, Xingxing Zhang, Hang Su, and Jun Zhu. A comprehensive survey of continual learning: Theory, method and application.  $arXiv\ preprint\ arXiv:2302.00487$ , 2023.