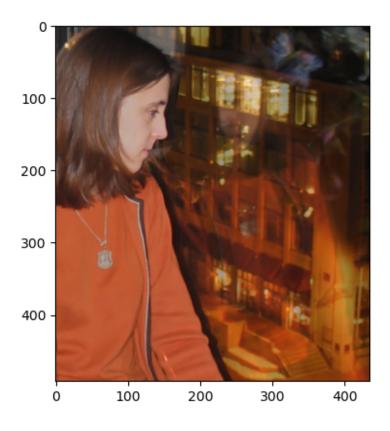
## bonus-flash-reflection-removal

October 26, 2022

```
[10]: import numpy as np
      import matplotlib.pyplot as plt
      import cv2
      from scipy.interpolate import interpn
      from scipy.signal import convolve2d
      from tqdm import tqdm
[11]: # load images
      museum_amb = './data/custom_bonus_1/paper_ambient.png'
      museum flash = './data/custom bonus 1/paper-reflection.png'
      # museum amb = './data/custom part1/DSC 1080.JPG'
      # museum flash = './data/custom part1/DSC 1081.JPG'
      museum amb = cv2.imread(museum amb,-1)[::skip,::skip,:3][:-50,:,::-1]
      museum_flash = cv2.imread(museum_flash,-1)[::skip,::skip,:3][:-50,:,::-1]
      # normalize to 0-1
      # museum_amb_norm = (museum_amb - np.min(museum_amb)) / (np.max(museum_amb) -__
       ⇔np.min(museum amb))
      # museum_flash_norm = (museum_flash - np.min(museum_flash)) / (np.
      →max(museum_flash) - np.min(museum_flash))
      museum_amb_norm = museum_amb / 255
      museum_flash_norm = museum_flash / 255
      # museum_flash_norm_shifted = np.zeros(museum_flash_norm.shape)
      # museum flash norm shifted[76//skip:] = museum flash norm[:-76//skip]
      # museum_flash_norm = museum_flash_norm_shifted
      H = museum_amb_norm*2/4 + museum_flash_norm*3/4
      plt.imshow(H)
```

Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).

[11]: <matplotlib.image.AxesImage at 0x7fcca44d2830>



```
[12]: def gradient(img):
          temp = img[:,:].copy()
          row = np.zeros((1,temp.shape[1]))
          col = np.zeros((temp.shape[0]+2,1))
          temp2 = np.vstack((row,np.vstack((temp, row))))
          temp2 = np.hstack((col,np.hstack((temp2, col))))
          img = temp2.copy()
          # we remove the last row and the last column corresponding to img_x at the_
       \hookrightarrowend
          # we remove the last col and the last column corresponding to img y at the
       \hookrightarrowend
          img_x = np.diff(img,n=1,axis=1) # change along row (i.e. diff bw columns)
          img_y = np.diff(img,n=1,axis=0) # change along column (i.e. diff bw rows)
            print(img_x.shape, img_y.shape)
            img_x, img_y = img_x[:-1,:], img_y[:,:-1]
            print(img_x.shape, img_y.shape)
          return img_x, img_y # vector field
      def divergence(u,v) :
```

```
u_x = np.diff(u,n=1,axis=1) # change along row (i.e. diff bw columns)
v_y = np.diff(v,n=1,axis=0) # change along column (i.e. diff bw rows)
u_x, v_y = u_x[1:-1,:], v_y[:,1:-1]

out = u_x + v_y
return out # scalar field

def laplacian(img) :
    kernel = np.array([[0,1,0],[1,-4,1],[0,1,0]])
    out = convolve2d(img, kernel, mode='same', boundary='fill', fillvalue=0)
    return out # scalar field
```

```
[13]: # Differentiate then re-integrate an image
      # Poisson Solver
      def conjugate_gradient_descent(I_init, B, I_star_boundary, eps, N, D) :
          I_star = B * I_init + (1-B) * I_star_boundary
          r = B * (D - laplacian(I_star))
          d = r.copy()
          delta_new = np.sum(r*r) # <r,r>
          n = 0
          while np.sqrt(np.sum(r*r)) > eps and n < N :
              if n \% 200 == 0 : print(n,np.sqrt(np.sum(r*r)))
              q = laplacian(d)
              eta = delta_new / np.sum(d*q) # n = delta_new / \langle d, q \rangle
              I_star = I_star + B * (eta * d)
              r = B * (r - eta * q)
              delta_old = delta_new.copy()
              delta_new = np.sum(r*r)
              beta = delta_new / delta_old
              d = r + beta * d
              n = n + 1
          return I_star
      def poisson_solver(lap_img, img, N = 1000, eps = 0.001) :
          I_init = np.zeros(img.shape)
```

```
boundary_size = 10
B = np.ones(img.shape)
B[0:boundary_size,:], B[-boundary_size:-1,:], B[:,0:boundary_size], B[:
-,-boundary_size:-1] = 0,0,0,0

I_star_boundary = np.zeros(img.shape)
I_star_boundary[0:boundary_size,:] = img[0:boundary_size,:].copy()
I_star_boundary[-boundary_size:-1,:] = img[-boundary_size:-1,:].copy()
I_star_boundary[:,0:boundary_size] = img[:,0:boundary_size].copy()
I_star_boundary[:,-boundary_size:-1] = img[:,-boundary_size:-1].copy()

I_star = conjugate_gradient_descent(I_init, B, I_star_boundary, eps, N,u
--lap_img)

return I_star
```

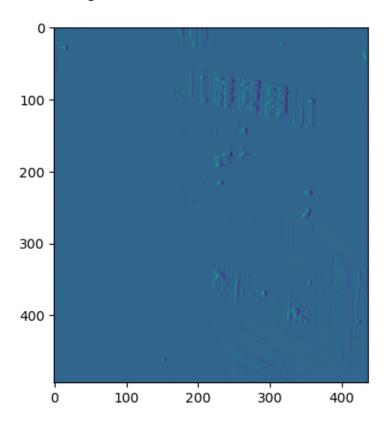
```
[14]: # Creating fused gradient field
      def fuse_gradient_field(img_amb_norm, img_flash_norm, H) :
          a_grad_x, a_grad_y = gradient(img_amb_norm)
          phi_dash_grad_x, phi_dash_grad_y = gradient(img_flash_norm)
          h_grad_x, h_grad_y = gradient(H)
          a grad x org = a grad x.copy()
          a_grad_y_org = a_grad_y.copy()
          phi_dash_grad_x_org = phi_dash_grad_x.copy()
          phi_dash_grad_y_org = phi_dash_grad_y.copy()
          h_grad_x_org = h_grad_x.copy()
          h_grad_y_org = h_grad_y.copy()
          a_grad_x, phi_dash_grad_x, h_grad_x = a_grad_x[1:,:], phi_dash_grad_x[1:,:
       →], h_grad_x[1:,:]
          a_grad_y, phi_dash_grad_y, h_grad_y = a_grad_y[:,1:], phi_dash_grad_y[:,1:
       →], h_grad_y[:,1:]
          h_proj_alpha = lambda h_grad,a_grad : a_grad * (h_grad * a_grad) / np.

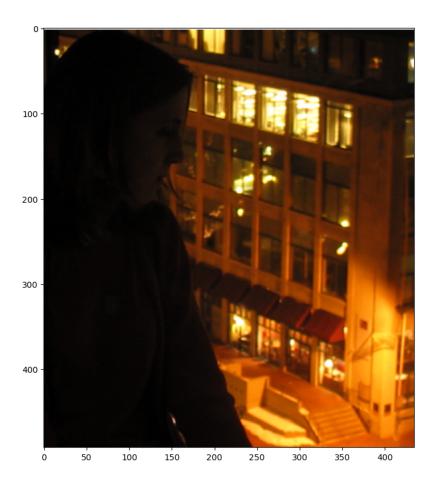
sqrt(np.sum(a_grad**2))
          sigma = 0.01
          tau ue = 0.1
          wue = np.zeros(a_grad_x.shape)
          wue[:-1,:-1] = 1 - np.tanh(sigma * (img_flash_norm-tau_ue))
          wue = (wue - np.min(wue)) / (np.max(wue) - np.min(wue))
            print(ws.shape, a grad x.shape, M.shape, phi dash grad x.shape, a grad y.
       ⇔shape, phi_dash_grad_y.shape)
```

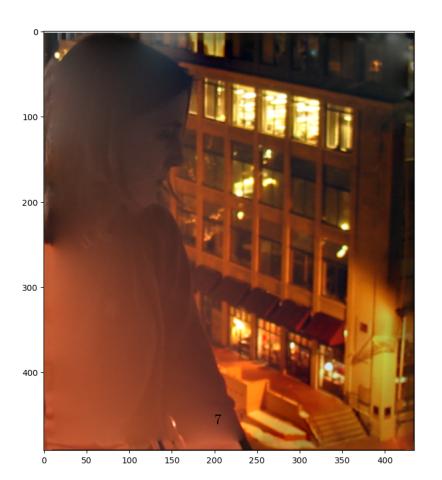
```
phi_star_grad_x = np.zeros(a_grad_x_org.shape)
    phi_star_grad_y = np.zeros(a_grad_y_org.shape)
    phi_star_grad_x[1:,:] = wue * a_grad_x + (1-wue) * (h_proj_alpha(h_grad_x,_u
  →a_grad_x))
    phi_star_grad_y[:,1:] = wue * a_grad_y + (1-wue) * (h_proj_alpha(h_grad_y,_u
  →a grad y))
    plt.imshow(phi_star_grad_x)
    div = divergence(phi_star_grad_x,phi_star_grad_y)
    return div
fused_image_r_div = fuse_gradient_field(museum_amb_norm[:,:,0],__
  \rightarrowmuseum_flash_norm[:,:,0], H[:,:,0])
fused_image_g_div = fuse_gradient_field(museum_amb_norm[:,:,1],__
  →museum_flash_norm[:,:,1], H[:,:,0])
fused_image_b_div = fuse_gradient_field(museum_amb_norm[:,:,2],__
 →museum_flash_norm[:,:,2], H[:,:,0])
I_star_r = poisson_solver(fused_image_r_div, H[:,:,0], N=5000, eps=0.0001)
I_star_g = poisson_solver(fused_image_g_div, H[:,:,1], N=5000, eps=0.0001)
I_star_b = poisson_solver(fused_image_b_div, H[:,:,2], N=5000, eps=0.0001)
I_star = np.concatenate((np.expand_dims(I_star_r,2),np.
 ⇔stack((I_star_g,I_star_b),axis=-1)),axis=2)
fig, ax = plt.subplots(2, figsize = (20,20))
ax[0].imshow(museum amb norm)
ax[1].imshow(I_star)
plt.show()
0 31.84426646509108
200 0.18217253005695647
400 0.0704343601452927
600 0.0076339061194579646
800 0.0010530636841693238
0 20.875489673044942
200 0.10351062478934817
400 0.04289114240389554
600 0.002880652265953053
800 0.00046533325298821275
0 21.534055060107413
200 0.06001455299345685
400 0.024193333498329687
600 0.003232640287154867
```

800 0.00037635856977812353

Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).



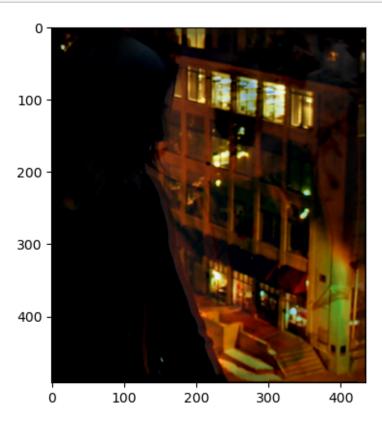


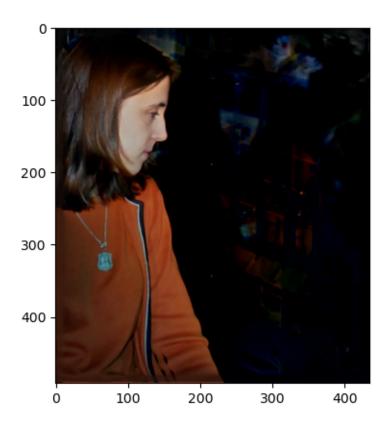


```
[8]: plt.imsave('outputs/reflection_sigma{}_tau{}_5by4.png'.format(0.01,0.1),np. 

Graph of the star o
```

```
[15]: plt.imshow(np.clip(I_star-museum_flash_norm,0,1))
    plt.show()
    plt.imshow(np.clip(museum_flash_norm-I_star,0,1))
    plt.show()
```





```
[ ]: museum_amb_norm_gradient_x.shape
[ ]: museum_amb_norm_gradient_y.shape
[ ]:
```