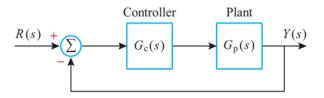
EE49001: Control and Electronic System Design

Assignment-3: Lead-Lag Compensator Design

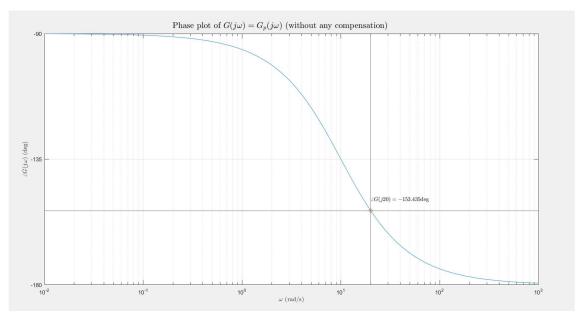
Submitted By:

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In the above block diagram,

$$G_p = \frac{10}{s(s+10)}$$



Design of Lead Compensator

For a lead compensator the controller is assumed to be of form

$$G_{c1} = \frac{K(Ts+1)}{\beta Ts + 1}$$

Where, K > 0, T > 0 and $0 < \beta < 1$

$$\omega_c = 0.995 \, \mathrm{rad/s}$$

From the above plot it can be observed that, uncompensated phase margin is $PM_u = \angle G(j20) + 180^\circ = 26.565^\circ$

Therefore, the controller parameters are

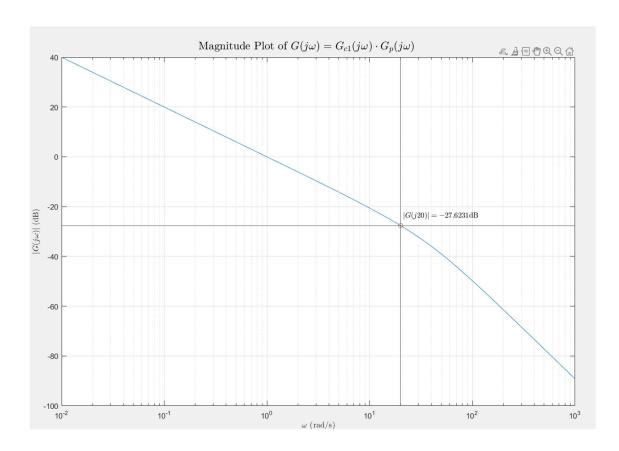
$$\phi_m = PM - PM_u = 33.435^{\circ}$$

$$\beta = \frac{1 - \sin \phi_m}{1 + \sin \phi_m}$$

$$\approx 0.2895$$

$$T = \frac{1}{\omega_c \sqrt{\beta}}$$

$$\approx 0.093$$



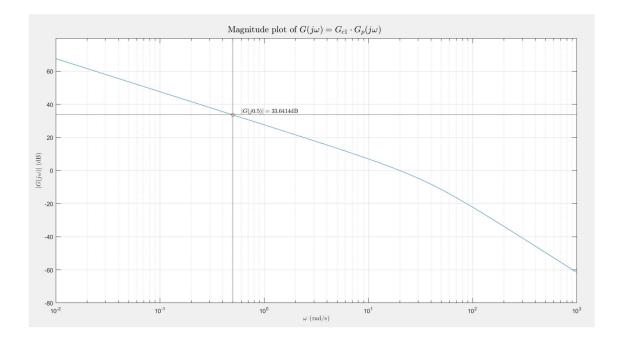
From the graph it can be observed that $20 \log |G_{c1} \cdot G_p(j20)| = -27.6231$ dB. Hence to make $|G_{c1} \cdot G_p(j20)| = 1$, the magnitude plot needs to be brought up by 27.6231dB. Therefore, our required DC gain is

$$K = 10^{\frac{27.6231}{20}} \approx 24.0522$$

Design of Lag Compensator

For a lag compensator the controlled is assumed to be of form

$$G_{c2} = \frac{\alpha (T_1 s + 1)}{\alpha T_1 s + 1}$$



Where, $T_1 > 0$, $\alpha > 1$

Here,

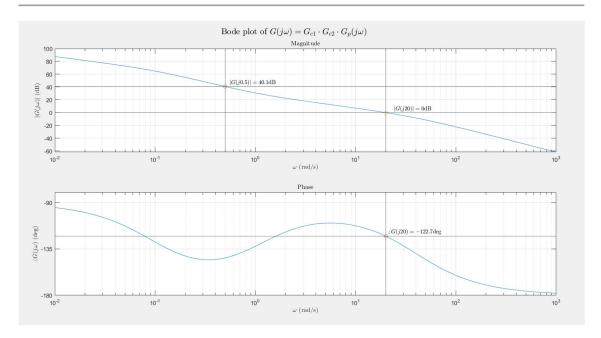
$$T_1 = \frac{7}{\omega_c} \approx 0.35$$

And from the above plot is observed that $20\log \left|G_{c1}\cdot G_p(j0.5)\right|=33.6414.$ Therefore,

Thus, the controller parameters are

$$F = \frac{100}{|G_{c1} \cdot G_p(j0.5)|} \approx 2.08 \quad \alpha \ge F = 10$$

Verification



The compensated system is $G(s) = G_{c1} \cdot G_{c2} \cdot G_p(s)$ and from the above plot it can observed that the gain crossover frequency is $20 \, \mathrm{rad/s}$ and the corresponding phase margin is $\angle G(j20) + 180 = 57.3 \, \mathrm{deg}$. Also loop gain at $\omega \in [0,0.5] \geq 100 \, (40 \, \mathrm{dB})$ as $|G(j\omega)|$ is decreasing in the lower frequencies and $20 \, \log |G(j0.5)| = 40.1 \, \mathrm{dB}$.

Thus, the desired specifications are met.