

# Time Series Discretization

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## 1 Introduction

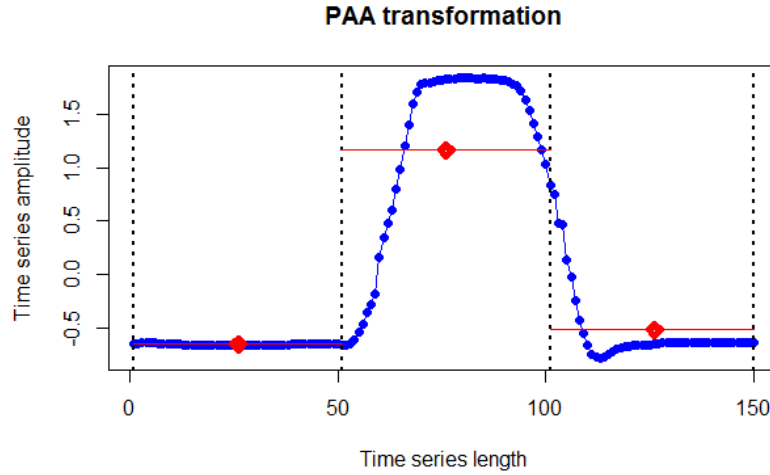
Given a dataset of  $m$  time series  $T_{i,j} = [T_1, T_2, \dots, T_m]$  where each row  $i$  is an univariate time series described by an horizontal vector of  $n$  observations  $T_{1,n}^{(i)} = [t_1^{(i)}, t_2^{(i)}, \dots, t_n^{(i)}]$ , the main goal of time series discretization known also as temporal discretization is to transform the original time series values into categorical values through a discretization scheme  $d_l = [d_1, d_2, \dots, d_l]$  where  $2 \leq l \leq n$ . To discretize a time series dataset, there are two approaches in the old and recent literature. On the one hand attribute based methods discretize the whole dataset without considering temporal order of data. On the other hand, instance based methods were designed especially for temporal data, it discretizes each instance using both time axis and vector values.

$$T_{n,m} = \begin{bmatrix} t_{11} & t_{12} & \dots & t_{1n} \\ t_{21} & t_{22} & \dots & t_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ t_{m1} & t_{m2} & \dots & t_{mn} \end{bmatrix} \quad (1)$$

## 2 Discretization method

As mentioned before, classical discretization methods were applied on time series discretization problem to split attribute values and produce a symbolic representation of the time series without reducing its size. Our idea is to break with the requirement of applying discretization on the feature values, and to use classical discretization algorithms to transform instances as univariate time series. The proposed discretization method transforms a time series  $TS$  with length  $n$  to a reduced symbolic representation  $\overline{TS}$  with length  $w$  ( $2 \leq w \leq n$ ). We propose a new approach defined as a discretization method that satisfy the additional temporal property of time series. Both classical discretization methods and PAA are combined in this approach to achieve better discretization performances. The first step in our strategy is to split the time series length to construct a set of word using PAA. Then, to split data amplitude, in the second step we apply classical discretization methods to select cut-points (alphabet).

### 2.1 Constructing a set of word via PAA



### 3 Time Series Results

Table 1: Classification accuracy (Conditional Inference Trees).

#	Dataset	SAX	w	NEW	k
1	GunPoint	0.76	12	0.9139	23
2	CBF	0.6311	9	0.661	8
3	Trace	0.75	19	0.98	6
4	FaceFour	0.159	2	0.159	2
5	Lighting2	0.754	9	0.77	18
6	Lighting7	0.52	9	0.48	6
7	ECG200	0.82	17	0.81	6
8	FISH	0.46	17	0.3885	20
9	Plane	0.876	17	0.790	7
10	Car	0.433	9	0.5	14
11	Beef	0.33	7	0.33	8
12	Coffee	0.5357	2	0.5357	2
13	OliveOil	0.66	7	0.66	7
14	ArrowHead	0.537	5	0.531	7
15	BeetleFly	0.5	2	0.5	2
16	BirdChicken	0.5	2	0.5	2
17	Ham	0.533	20	0.514	2
18	Herring	0.5937	2	0.5937	2
19	ToeSegmentation1	0.5263	2	0.5263	2
20	ShapeletSim	0.5	2	0.5	2
21	Wine	0.5	2	0.5	2
22	Meat	0.66	14	0.85	19
23	Worms	0.419	2	0.43	8
24	WormsTwoClass	0.58	2	0.58	2
25	Mean	0.564075	7.958333	0.5834625	7.375