

arr  $\rightarrow$   $T^*$   
 size  $\rightarrow$  size\_t  
 capacity  $\rightarrow$  size\_t

int Pay - 4

Vector Implementation

capacity=1  
 size=0

~~new~~ Insert: (T & val)

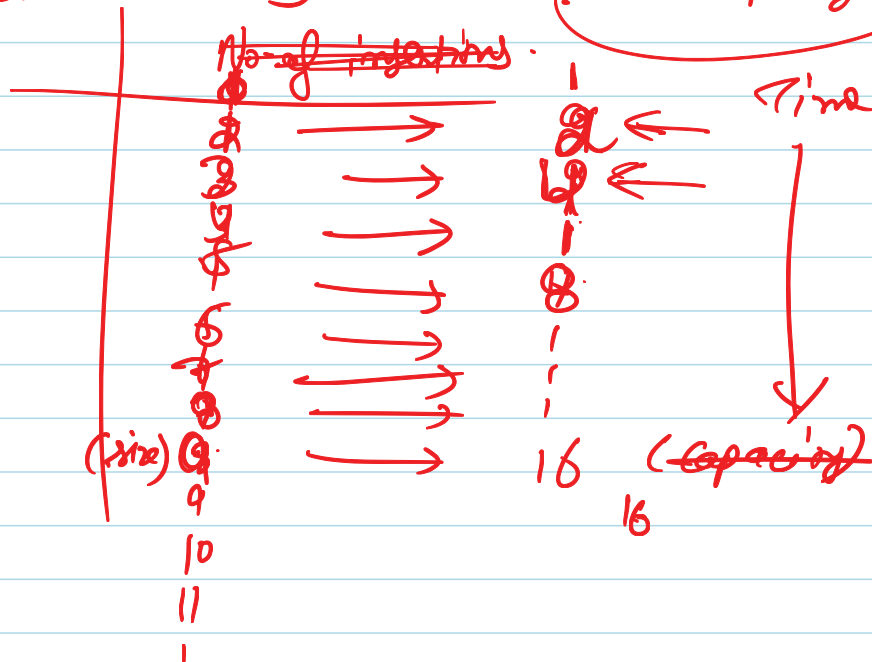
```
{
    if (size == capacity)
        capacity *= 2;
    auto arr = new T[capacity];
    for (int i=0; i < size; i++)
```

```
arr[i] = this->arr[i];
    size++; arr[size-1] = val;
    delete[] this->arr;
    this->arr = arr;
}
```

How to access arr of class instead of local variable.

```
void pop_back()
{
    assert(size > 0);
    size--;
}
```

Insertion time



Insertion  
time

$$1 + 2 + 4 + 1 + 1 + \dots + 8 + \underbrace{1 + 1 + 1 + 1 + 1}_{8 \text{ times}} + 16 + \underbrace{1 + 1 + 1 + 1 + 1 + 1 + 1 + 1}_{16 \text{ times}} + 32$$

$$n \geq \begin{pmatrix} 100 \\ 1000 \end{pmatrix}$$

$n$

$$\leq \underline{2n} \text{ operations} \Rightarrow \underline{O(1) \text{ per element}}$$

size --;

delete

{ delete[] arr;  
}

Union-Find (PSU)

$n$  skills

skill  $i \rightarrow T_i$   
 $\rightarrow i \rightarrow +P_i$

Some skills are in a group  
 $(x, y)$

$G \rightarrow i$

Time =  $\sum T_i$   
~~Sum~~  
 Power gain =  $\sum P_i$

in  $B$  time, find the maximum power gain you can achieve.

$C \rightarrow G$

$n \leq 1000$   
 $B \leq 10^3$   
 $T_i \leq 10^3$   
 $P_i \leq 10^6$

②  $N$

→ good form = remove duplicate prime factors of  $N$ .  
 $N=12, 12 = 2^2 \times 3$   
 $\rightarrow 2 \times 3$  (M)

better form = multiplication of all divisors of  $M$   
 $\rightarrow P$

best form = No. of divisors of  $P$ . (→)

$t=1$   
 ~~$N \leq 10^2$~~   
 $N \leq 10^{15}$

modulo  $10^9+7$

$\sqrt{n} \rightarrow (P_i, \alpha_i)$

$$N = \prod_{i=1}^K P_i^{\alpha_i}$$

$\sqrt{10^{15}} = 10^7$   
 and: 1

$(\alpha_i + 1)$

$$12 = 2^2 \times 3 \xrightarrow{M} 2 \times 3 = 6$$

$P \Rightarrow 6 \rightarrow (1, 2, 3, 6) \rightarrow (36)$

$$1, 2, 3, 4, 6, 9, 12, 18, 36 \rightarrow (9)$$

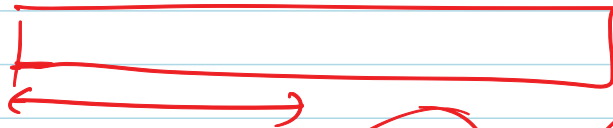
let good form =  $M = \prod_{i=1}^k p_i$

Better form =  $\prod_{i=1}^k p_i^{a_i}$

Best form =  $(2^{k-1} + 1)^k$

H.W. (3)

array, size  $n$



segment size =  $x$

$$n > x$$

for each segment, find the minimum

Priority Queue

(a) count of minimums =  $n - x + 1$



(b)

$$t = 1$$

$$1 \leq n \leq 10^6$$

$$1 \leq x \leq n$$

$$1 \leq a_i \leq 10^9$$

max

(Without using segment Tree)

$T = ?$

4

vector <string>

$$N \leq 10^5$$

$$\text{len}(a_i) \leq 50$$

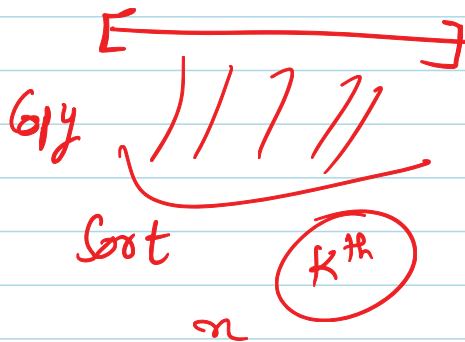
$$a_{ij} \in \{ 'a', 'b', \dots, 'z' \}$$

$$0 \leq 10^5$$

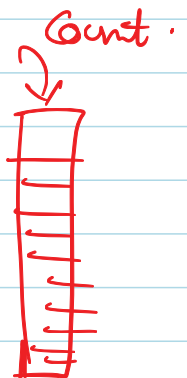
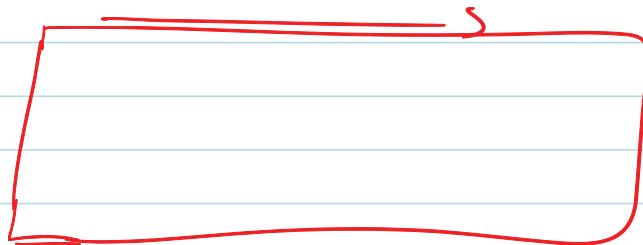
$$1 \leq L \leq R \leq N$$

$$a_L, a_{L+1}, \dots, a_R$$

$$1 \leq K \leq \sum_{i=L}^R \text{size}(a_i)$$



$$26 \times n \sim 26 \downarrow$$

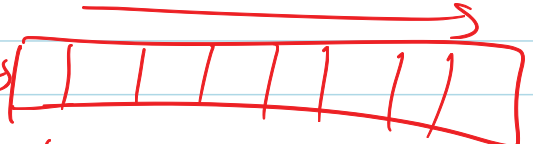


Investor

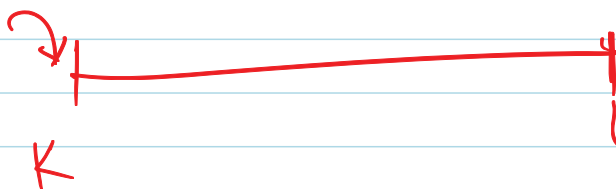
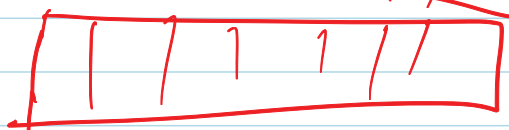
$S \rightarrow$  Savings

$n$

current Value of Stocks



future Value of Stocks  
(i.e. 11111)



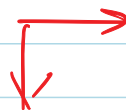
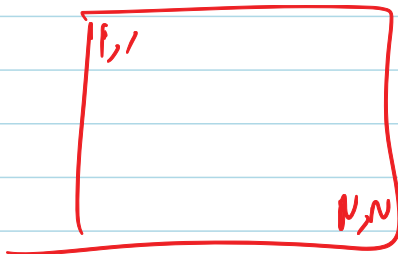
Profit

~~Loss~~ = Profit

$0 \leq n \leq 100$   
 $0 \leq \text{string} \leq 30,000$   
 $0 \leq \text{cur}[i][f[0]] \leq 300$

5

matrix

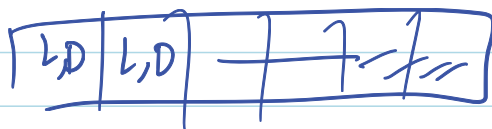


①  $(1,1) \rightarrow (N,N) \rightarrow \text{count}$

②  $(1,1) \rightarrow (N,N) \rightarrow \text{print all paths}$

N:

$\rightarrow n$   
 $\downarrow n$



$\sum \text{path length of each path} \leq 10^9$

$$2^n \binom{2n}{n} \leq 10^7$$

Recursion:

$(1,1) \rightarrow (1,2) \rightarrow (1,3) \rightarrow (2,3) \dots$

int N;

for (int i, int j)

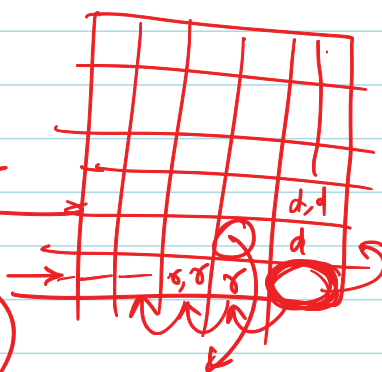
vector<vector<vector<string>>>>

for (i = N-1 to 1)  
for (j = N-1 to 1)

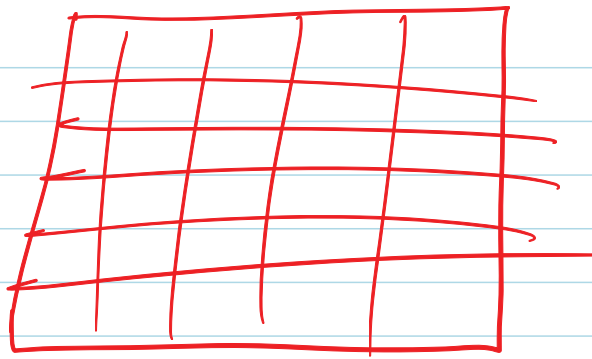
{

$dp[i][j] = (dp[i+1][j] \cup dp[i][j+1])$

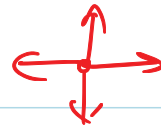
$dp[i][j] = dp[i][j+1] \cup dp[i+1][j]$



H.W.



$N \times M$



$$m[i][j] = a_{ij}$$

$$1 \leq a_{ij} \leq 10^9$$

$$i \in \{1, 2, \dots, N\}$$

$$j \in \{1, 2, \dots, M\}$$

Find the length of longest increasing path.

$$P: a_{i_1, j_1} < a_{i_2, j_2} < a_{i_3, j_3} \dots$$

$$a_{i_1, j_1} < a_{i_2, j_2} < a_{i_3, j_3} \dots$$

$$\rightarrow dp[i][j] = \text{len} \text{ starting from } [i][j]$$



pseudo code

$$1 \leq T \leq 1$$

$$1 \leq N, M \leq 5 \times 10^3$$

dp + recursion

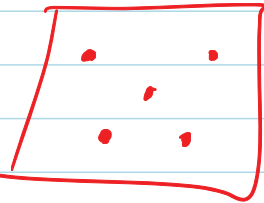
{ value  
i  
j }

starting

starting



for each starting point



{  
~  
}

dp + recursion  
(memoization)

[ ]

[ ]

4 Aug → 3 small, answer + stab.

5 August → basic implem of ~~stab~~ vector ← Code ←

2 small (Test)

Don't upload  
txt  
code

reasoning