

Applications of AI:-

① AI in Gaming: Chess, Poker, tic-toe.

↳ Machine can think large no. of moves.

② AI in NLP: Natural Language Processing

↳ Machine can understand human lang.

③ AI in Healthcare: Fast diagnosis

↳ Robotic Surgery.

④ AI in Finance: Adaptive Intelligence.

↳ automatic chatbots, algorithm trading.

⑤ AI in Data Security: Helps in making data/applications more secure.

↳ AEG bot, AI2

⑥ Expert System: Integration of software, machine and special info to provide reasoning & advise.

⑦ Computer Vision: Understand the visual automatically by machine.

⑧ Speech Recognition: Extract - the meaning of sentence by human talk. [slang removal, noise rem..]

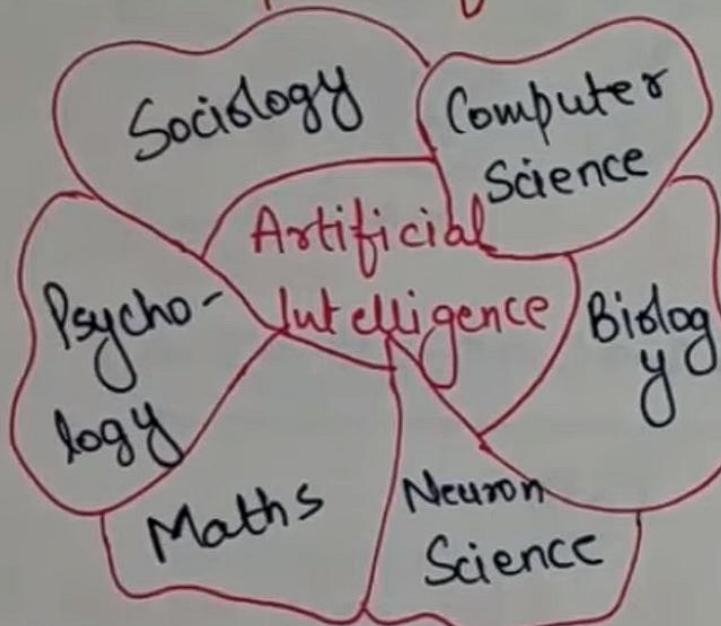
⑨ Robotics:

Talk and behave like humans. ↳ Erica and Sophia.

⑩ AI in e-Commerce: Automatic recommendations.



AI is Comprised of :-



- ↳ Reasoning
- ↳ Learning
- ↳ Problem Solving
- ↳ Language Understanding.

Advantages of AI

Accuracy ↑ & Error ↓

Fast Decision Making.

Reliability is more

usefulness in Risky Area.

Digital Assistant

Disadvantages of AI

COST ↑

Can't think beyond the limits.

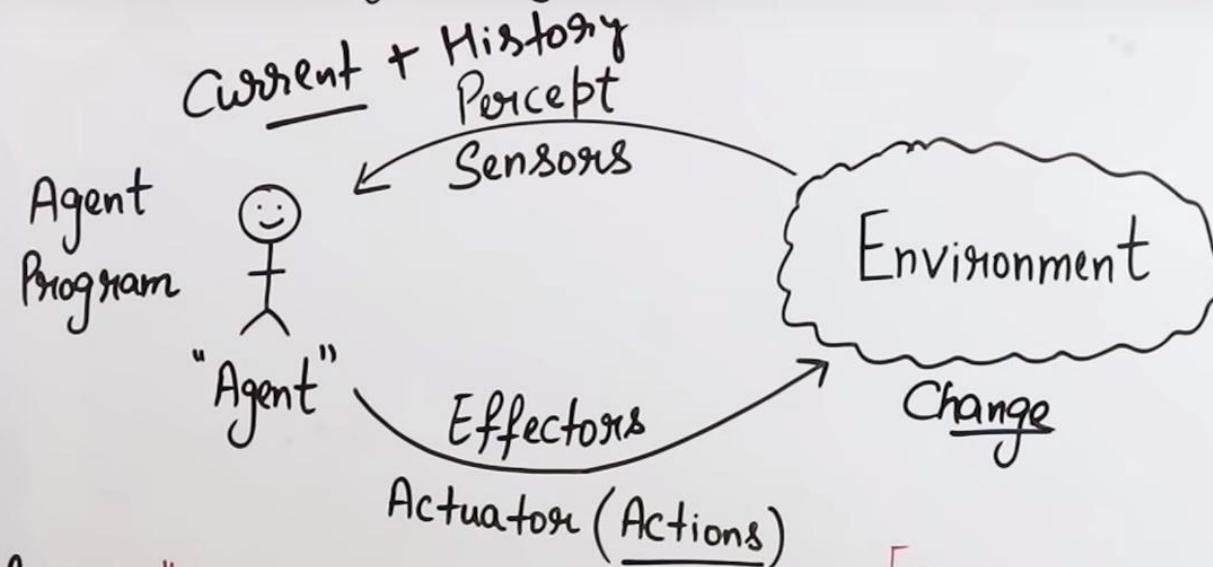
No feelings & emotions.

more dependency on machines ↑.

No original thinking.

→ Introduction to Intelligent Agents and their types with Example in Artificial Intelligence

Agents / Intelligent Agents



"Goals of Agent"

→ High Performance
Optimized Result
Rational Action

P : Performance
E : Environment
A : Actions
S : Sensors

Agent → Percept → Decision → Actions

"Types"

- 1) Simple Reflex Agents
- 2) Model Based Reflex
- 3) Goal Based Agents
- 4) Utility-Based Agents
- 5) Learning Agents



Types of AI Agents: [Responsible for any work output obtained from AI is defined as study of Rational System .

Agents. → Person
firm
→ Machines/w

Make
Decisions

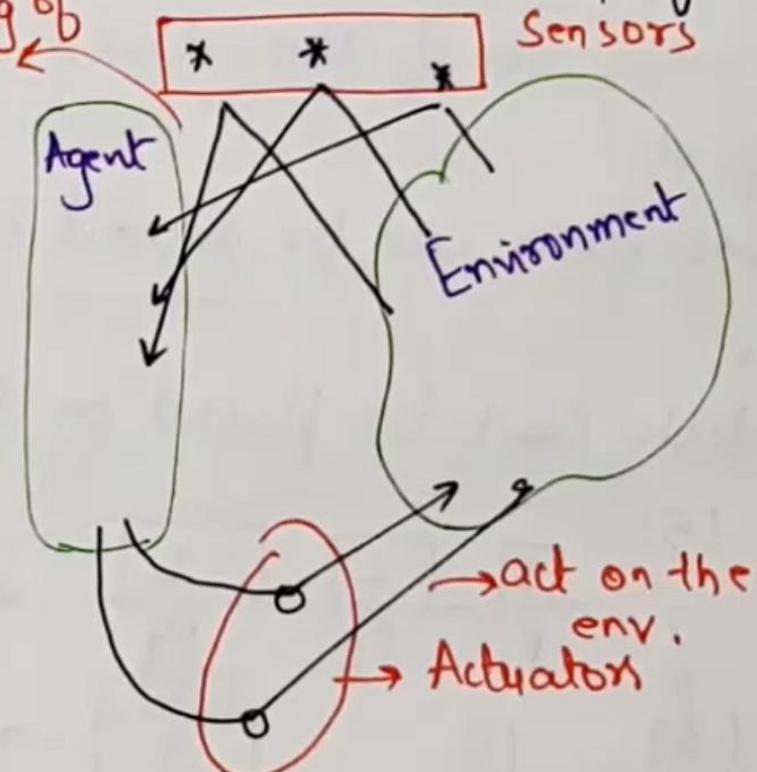
AI System is composed of Agent
Environment

Agent is anything like:-

- ii) perceiving its environment through Sensors.
- iii) Acting upon that environment through actuators.

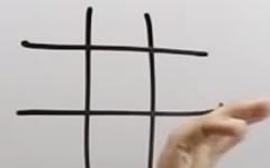
Perceiving
Info".

Agent → Info gathering.
→ action perform.

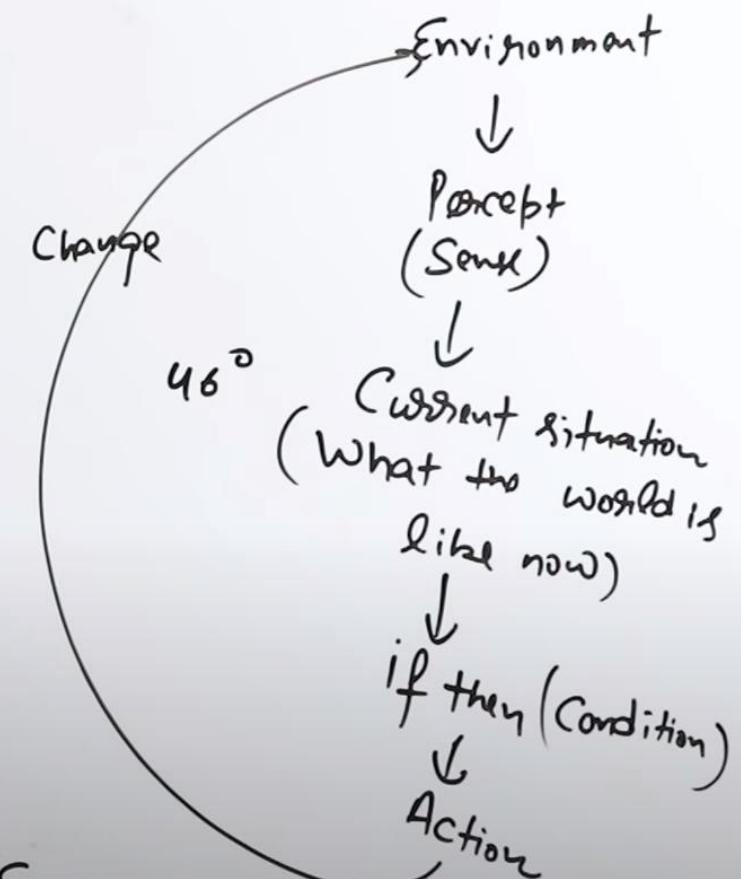


"Simple Reflex Agents"

- Act only on the basis of current perception
- Ignore the rest of percept history
- Based on If - Then Rules
- Environment should be fully observable.



Partially
if temp > 45°
then Switch on AC

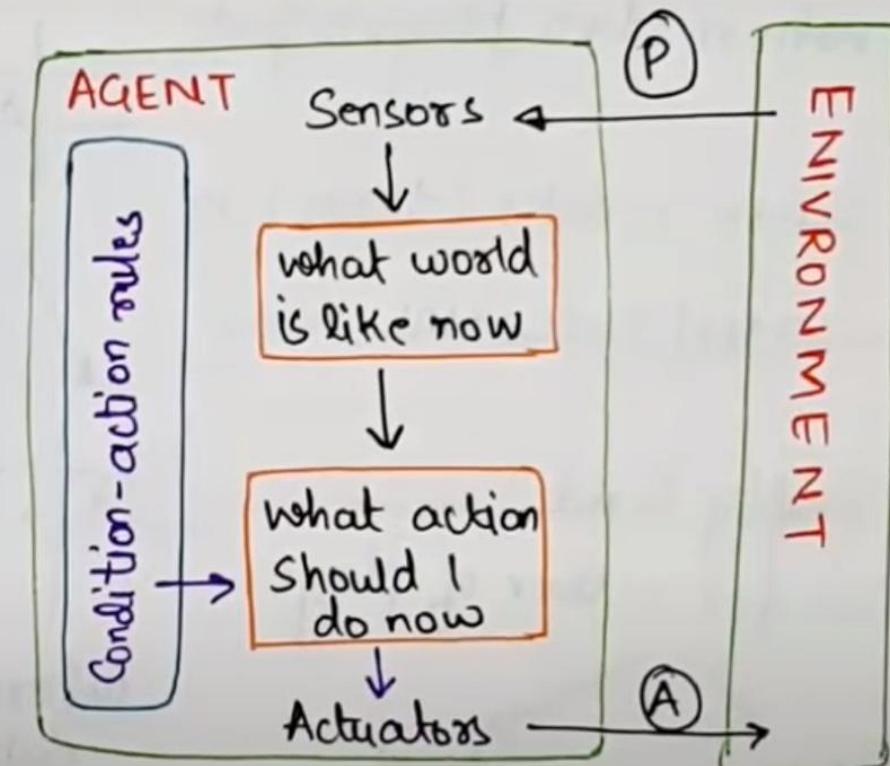


Simple Reflex Agents:

Works only on Current situation / perception and ignores the history of previous state. True
↳ Condition - Action Rule

Limitations:-

- ↳ i) Very limited Intelligence.
- ii) No knowledge about non-perceptual parts of state
- iii) Can go into infinite loop.

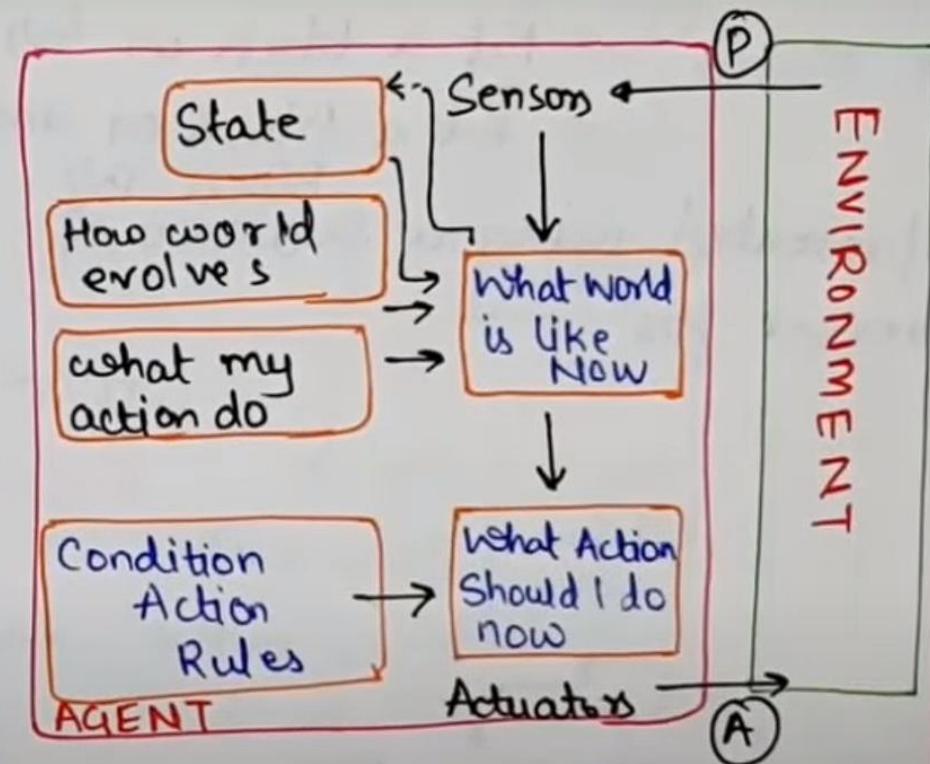


② ~~Model~~ Model based Reflex Agent:

- ↳ Works by finding the rule whose condⁿ matches current situation.
- ↳ Can work in partially observable env., and track situation.
- ↳ Agent keeps track of internal State which is adjusted by each percept and that depends on percept history.
- ↳ Model: How things happen in world.

Agent State update required Infoⁿ:

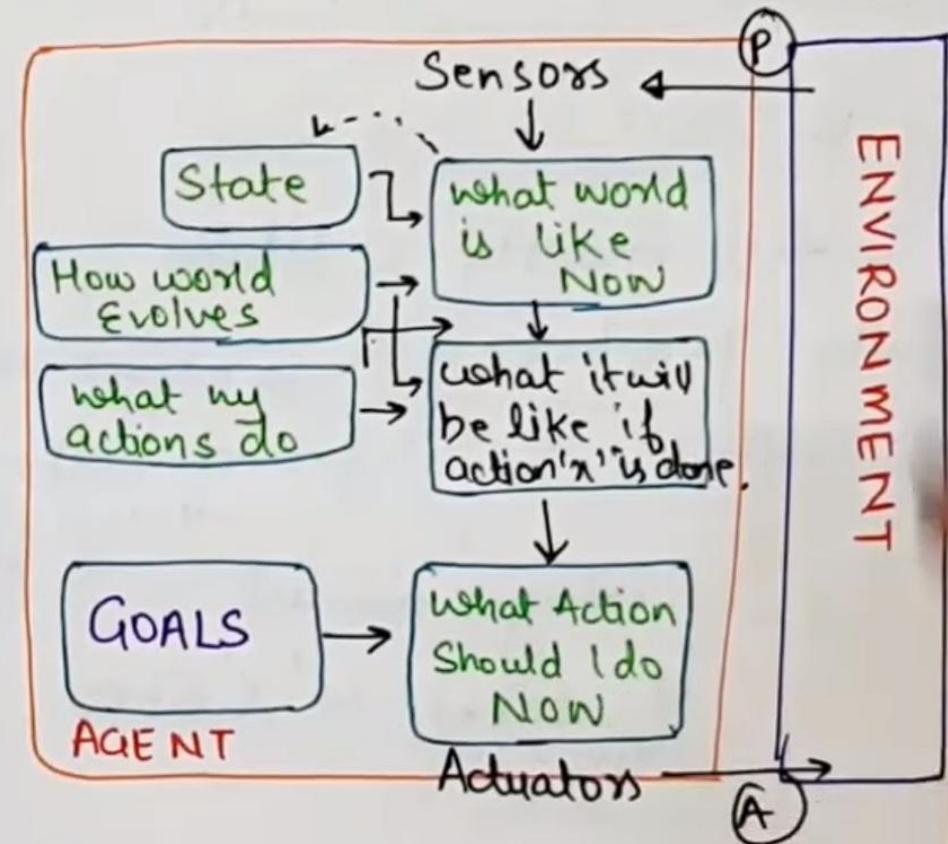
- ① How world is evolving
- ② How agent's action affect the word.





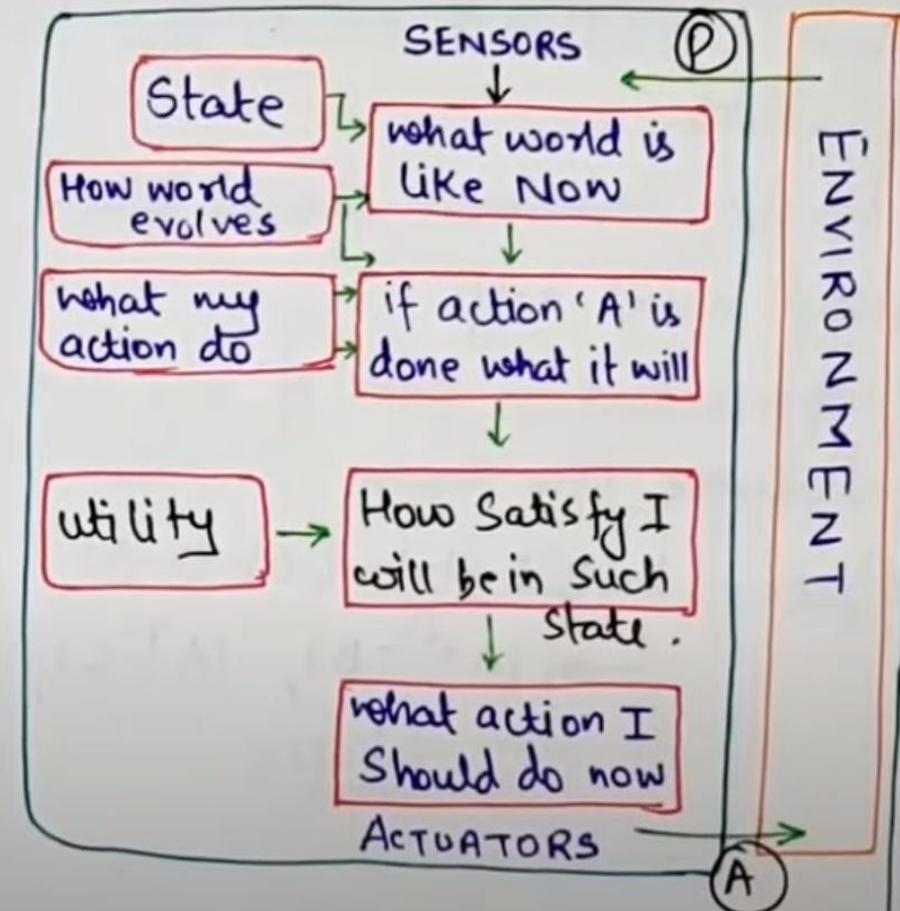
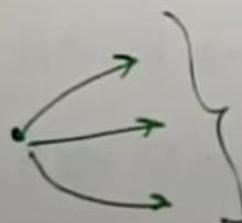
Goal-Based Agents:

- Focuses only on reaching the goal set.
- ↳ Agent takes decision based on how far it is currently from the Goal State.
- ↳ Every action is taken to minimize distance to Goal State.
- ↳ More flexible Agent.



Utility-Based Agents:-

- Agents are more concerned about the utility (Preference) for each state.
- Act based not only on goals but also the best way to achieve goal.
- Useful when there are multiple possible alternatives and agent has to choose in order to perform best action.



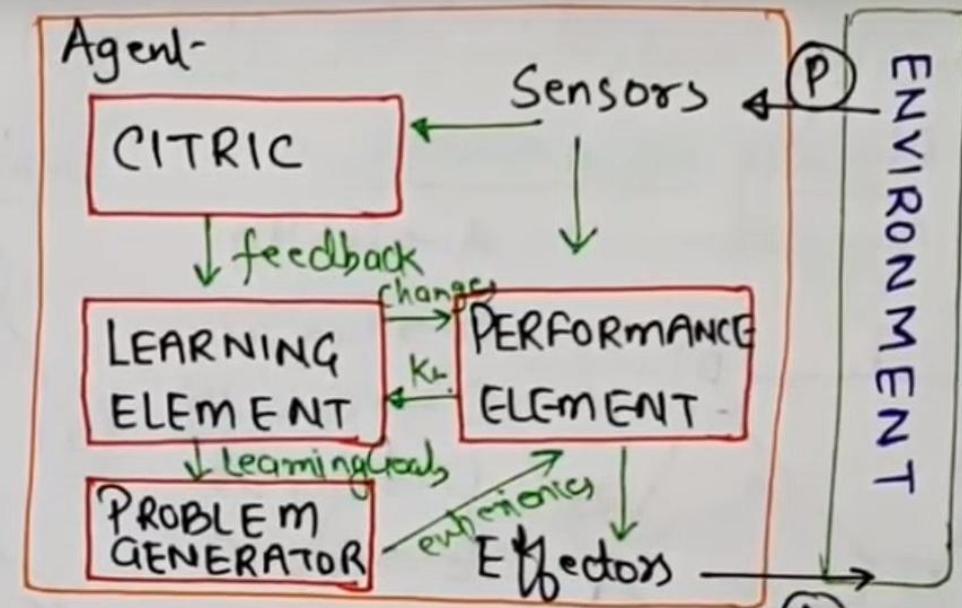
Example of Beam Search algorithms.

5) Learning Agents:-

- Can Learn from its past experiences.
- Starts to ACT with basic knowledge and then able to act by adapting Learning.

Components:-

- Learning Element: Makes Improvement in System by learning from env.
- CITRIC: Gives feedback about Agent's Performance based on Standard.
- Performance Element:
- Problem Generator:



PEAS: Grouping of AI Agents:

- ↳ used to group similar type of agents together.
- ↳ PEAS:
 - Sensor:- Devices from which agent perceives observation from env
 - Actuators:- devices, H/w, S/w through which Agent performs action on env.
 - Environment
 - All Surrounding things and conditions.
- Performance measure
 - It is the info we get from an Agent.
 - Results obtained after Agent Processing.

Example:-

SELF DRIVING CAR

- (P):- Comfort, Safety, Time, Legal driving.
- (E):- Cond'n of Roads, Crossings, Traffic Signals.
- (A):- Steering, Brakes, Horn, Accelerator.
- (S):- Camera,

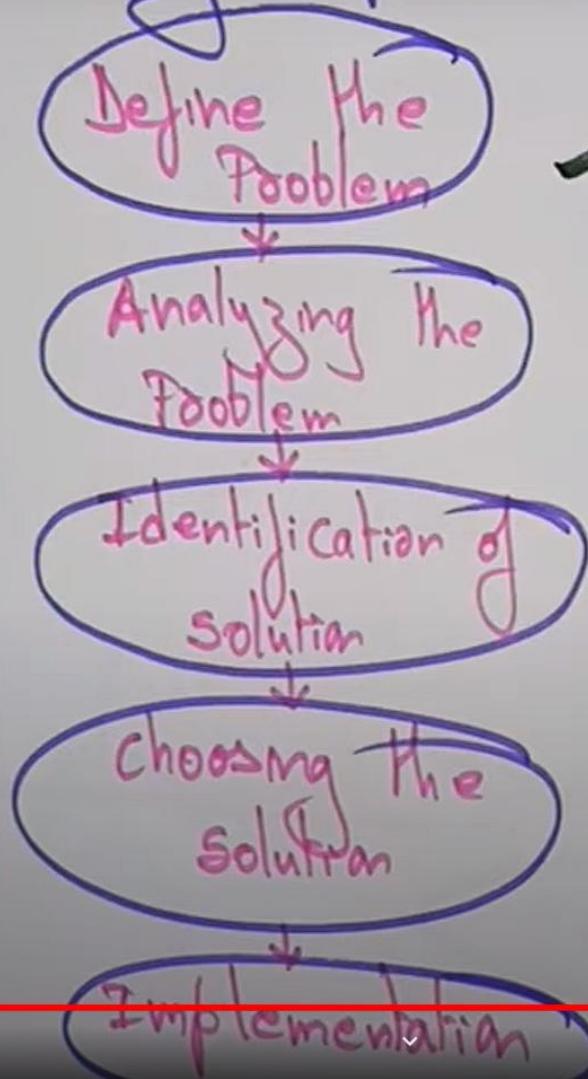
- Problem Solving is in games such as "Sudoku" eg. It can be done by building an AI system to solve that particular problem.
- To do this one needs to define the problem statement first and then generating the solution by keeping the condition in mind.
- Some of the most popularly used problem solving with the help of AI are:

Chess, Travelling Salesman Problem,
Tower of Hanoi problem, Water Jug problem,
N-Queen problem

Problem Searching

- In general, searching refers to as finding information one needs
- Searching is the most commonly used technique of Problem Solving in A.I

The process of solving a problem consists of 5 steps



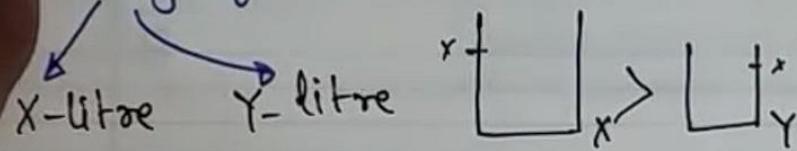


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WATER JUG Problem and its State Representation: Example:- Suppose Capacity of two jugs $\begin{cases} 2 \text{ litre} \\ 3 \text{ litre} \end{cases} \leftarrow \langle x, y \rangle$

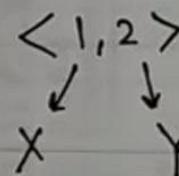
No Jugs of different Capacities are given.



No Marking is there on any JUG.

Goal is to fill exactly 'L' litres of water into 'Y'-litre JUG.

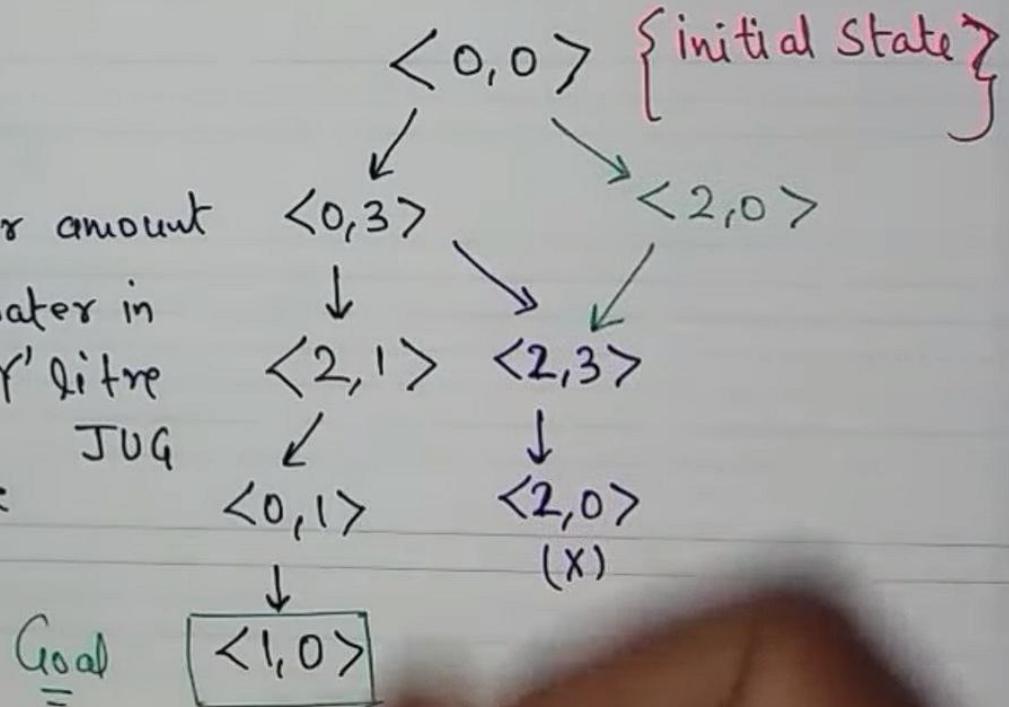
State is represented as $\langle x, y \rangle$ of water in 'Y' litre JUG



integer amount of water in 'X' litre JUG

Two jugs $\begin{cases} 2 \text{ litre} \\ 3 \text{ litre} \end{cases} \leftarrow \langle x, y \rangle$

GOAL: To Get exactly '1' liter of water in 2 liter JUG. $\langle 1, 0 \rangle$ (Goal State)



↳ Explores all the nodes at given depth before proceeding to the next level.

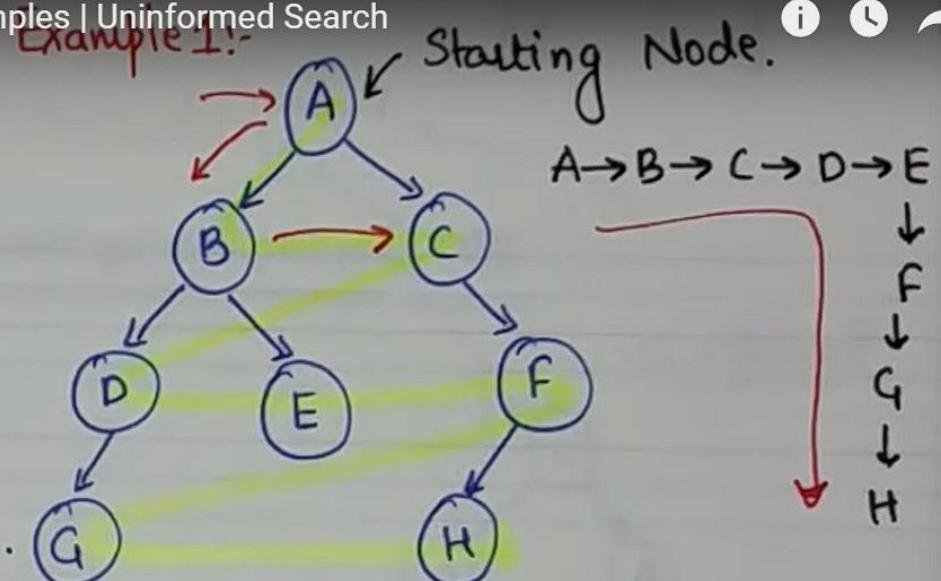
↳ Uses Queue to implement.

ALGORITHM:

- Enter Starting nodes on Queue.
- If Queue is empty, then return fail and stop.
- If first element on Queue is GOAL Node, then return Success and stop.

ELSE

- (IMP) Remove and expand first element from Queue and place children at end of Queue.
- Goto Step (ii)



Initial Queue $\{A\}$ = Goal node x

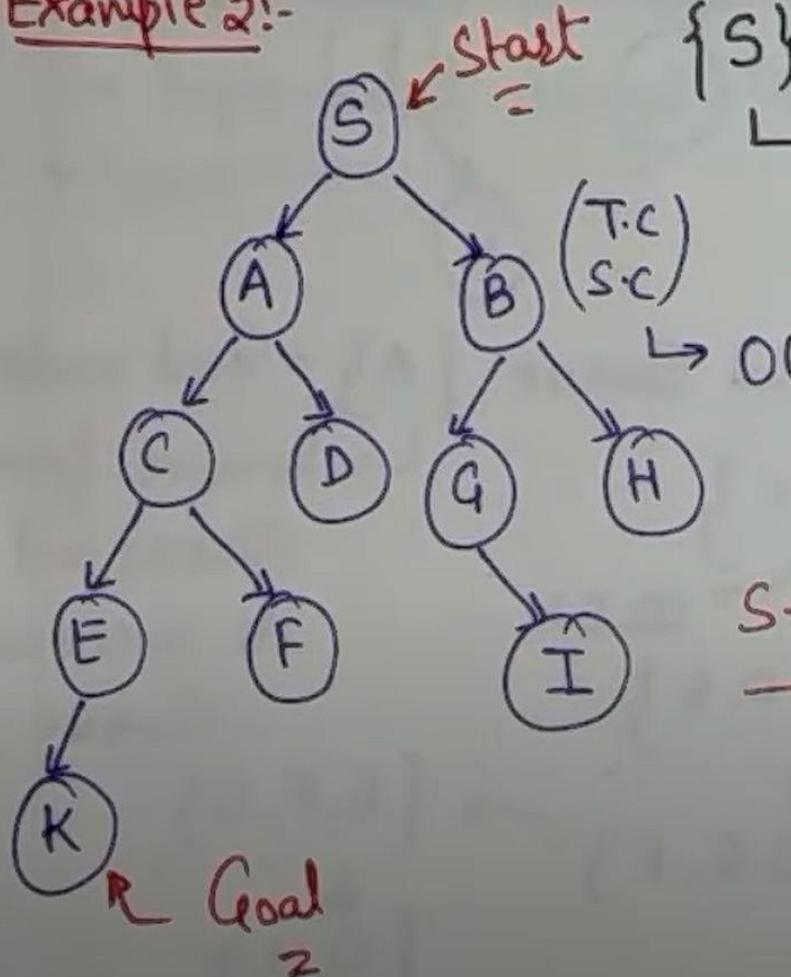
Remove from Queue and add its Successor to Queue.

$\{B, C\}$

\downarrow
 $\{C, D, E\}$

$\{D, E, F\} \rightarrow \{E, F, G\}$

\downarrow
 $\{G, H\}$

Example 2:-

$\{S\}$
 $\xrightarrow{\quad}$ $\{A, B\}$
 $\xrightarrow{\quad}$ $\{B, C, D\}$
 $\xrightarrow{\quad}$ $\{C, D, G, H\}$
 $\xrightarrow{\quad}$ $\{D, G, H, E, F\}$
 $\xrightarrow{\quad}$ $\{H, E, F, I\}$
 $\xrightarrow{\quad}$ $\{F, I, K\}$

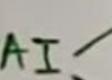
$S \rightarrow A \rightarrow B \rightarrow C$
 \downarrow
 D
 \downarrow
 $G \rightarrow H \rightarrow E \rightarrow F \rightarrow I \rightarrow K$

Adv: - find a Solⁿ if its exists.
 \hookrightarrow minimal Solⁿ in least no. of steps.

Disadv: More memory
 \hookrightarrow need lots of time
 \hookrightarrow Solⁿ is far from root node.

Artificial Intelligence: AI is the study of How to make computer do things which people do better. [machine + human Intelligence]

↳ AI can cause a machine to work as human.

↳  AI → Artificial [Man-Made]
→ Intelligence [Power of thinking]

GOALS OF AI:

- i) Replication of Human Intelligence.
- ii) Solving problems that require knowledge.
- iii) Building a machine that can do human Intelligence task. [CHESS, Proving theorem, automated car driving ...]
- iv) Providing advise to the user.
- v) Intelligent comm' b/w perception and

Reasons of Boost in AI:

↳ i) SW or device can be made to solve Real-time Problems.

ii) Creation of Virtual assistant [SIRI, CORTANA]

iii) Robots development.
[Helps in dangerous env. condⁿ]

iv) New Job opportunities.

DFS: Depth-First Search.

↳ Recursive algorithm.

↳ Starts from root node and follows each path to its greatest depth node before moving to the next path.

↳ Implemented using STACK (LIFO)

ALGORITHM: → (PUSH)

i) Enter ROOT node on Stack

ii) Do until Stack is not empty

 ↳ a) Remove Node → (POP)

 ↳ ii) If Node = Goal Stop.

 ↳ Push all children of Node in Stack

Adv:- Less memory

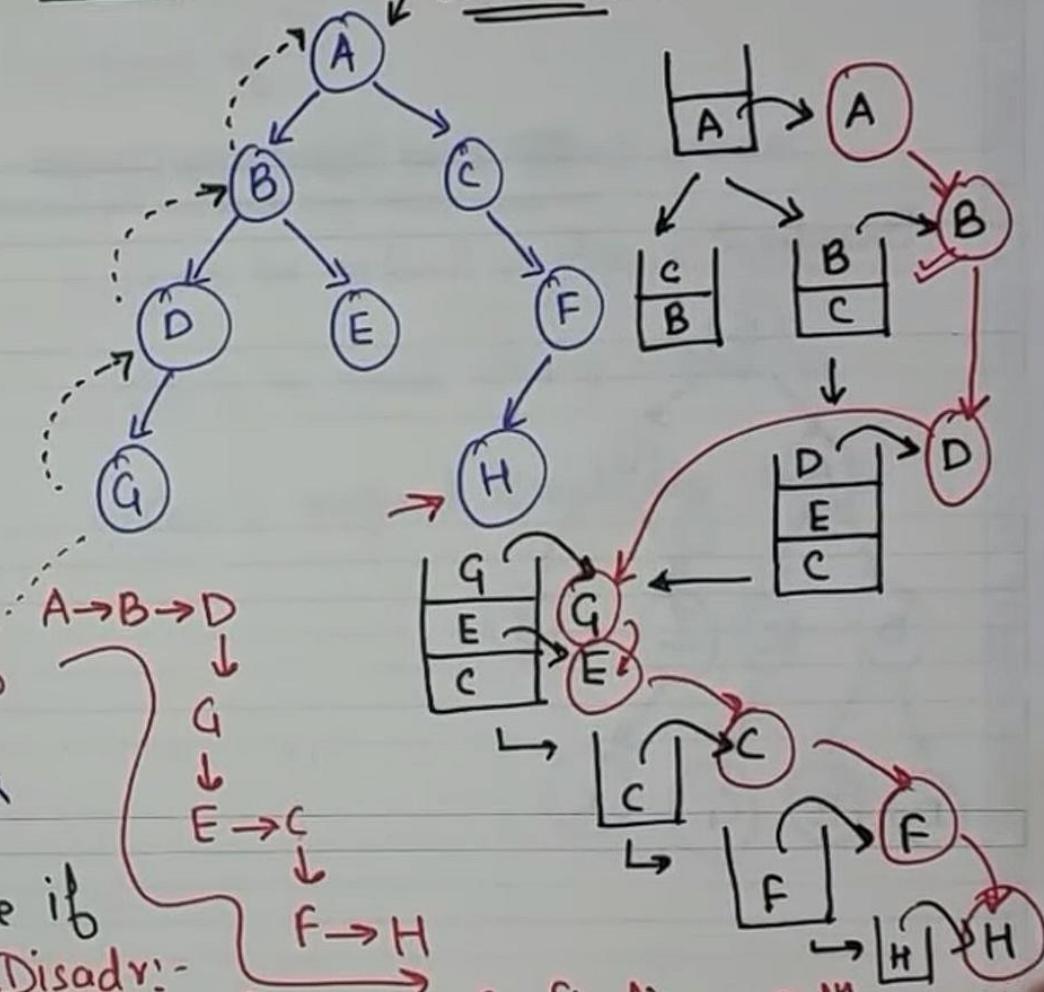
↳ Less time to reach goal node if traversal in right path.

Disadv:-

↳ No guarantee of finding soln.
↳ Infinite loop.

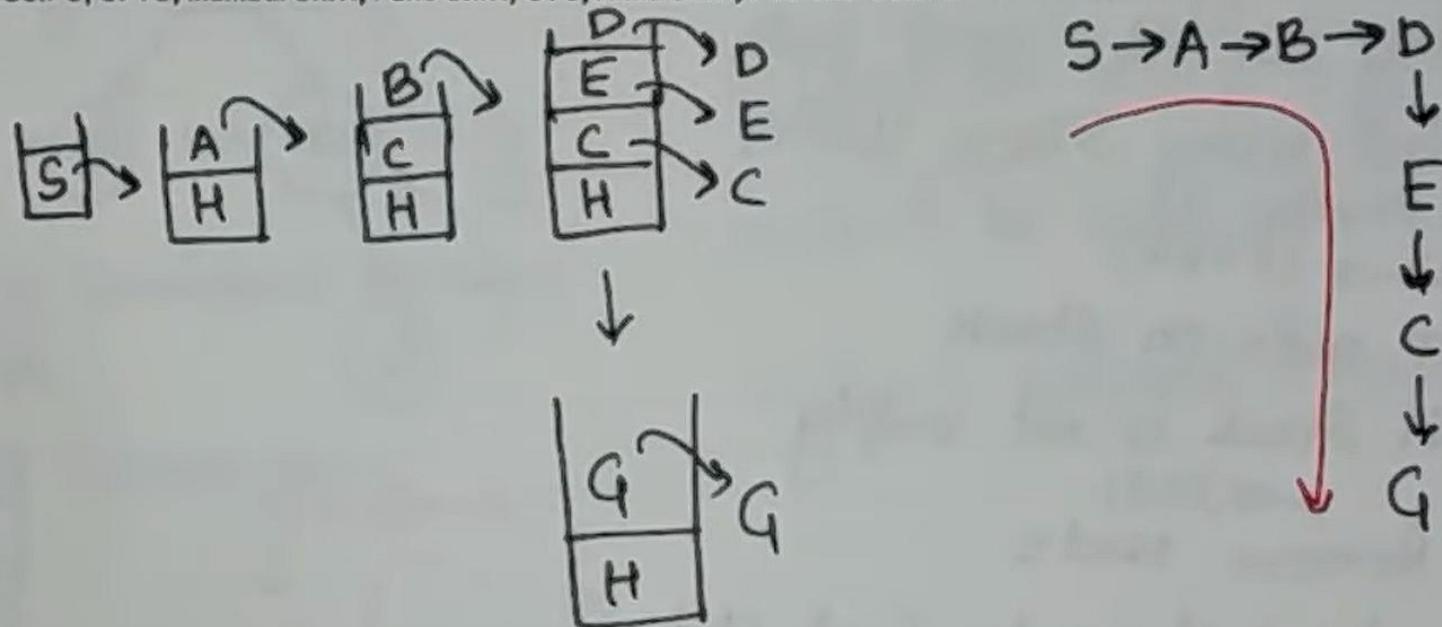
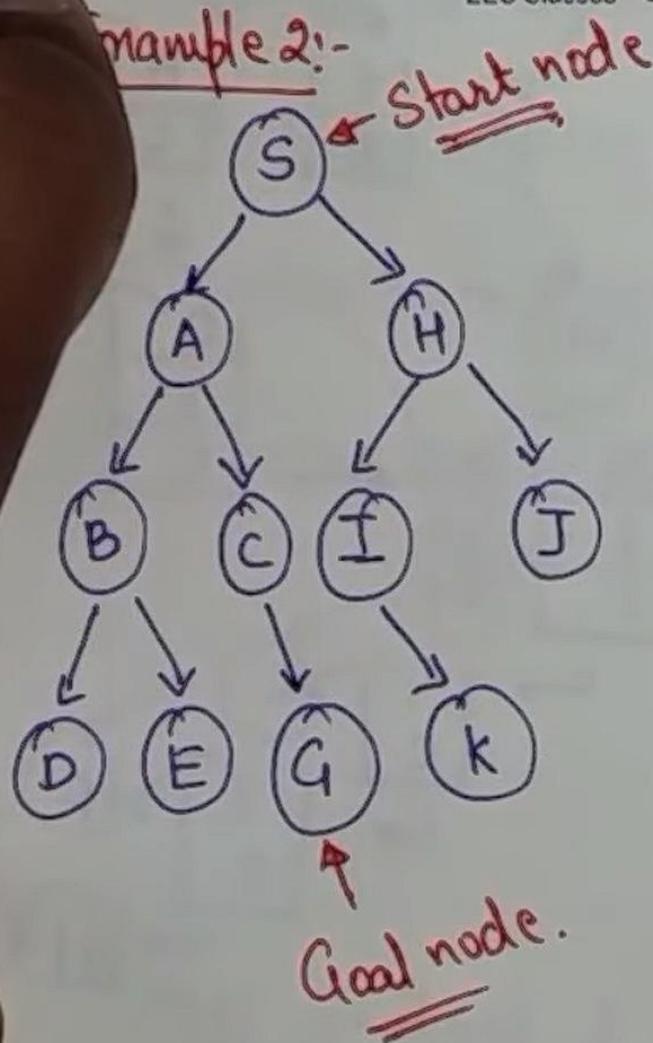
Example 1:

Start node.





Example 2:-



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- + 156 of 311

Draw Read aloud

Space
Optimal?
Complete?

b: branching factor d: solution depth m: maximum depth

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Department of Computer Science & Engineering. Subject Name: Artificial Intelligence. Instructor Name : Deepika Kumar



Search Strategies: Blind Search

Criterion	Breadth-First	Depth-First
Time	b^d	b^m
Space	b^d	b^m
Optimal?	Yes	No
Complete?	Yes	No

b: branching factor d: solution depth m: maximum depth

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Informed Search: \rightarrow Heuristic Search
 \rightarrow Heuristic function.

\hookrightarrow Information about GOAL State is present.

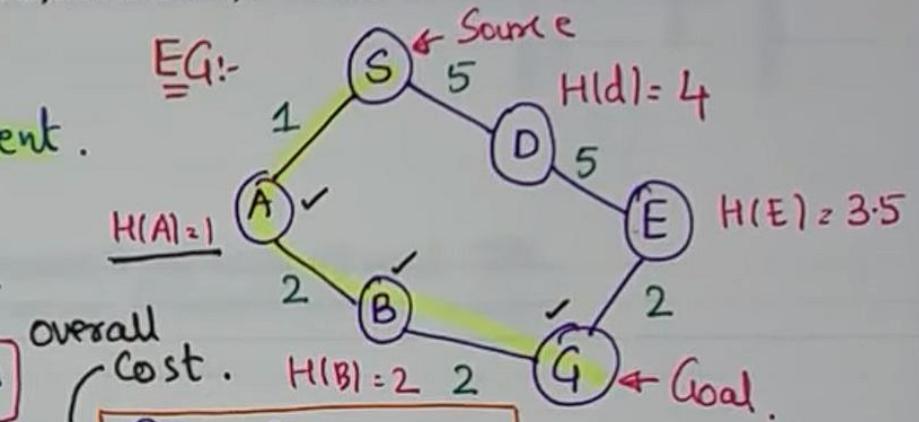
\hookrightarrow Better-than UnInformed Search.

\hookrightarrow finds optimal Solⁿ to reach GOAL State.

min. Path cost. \rightarrow Using HEURISTIC FUNCTION

\hookrightarrow It is a Search which tries to reduce amount of Search that must be done by making intelligent choices for the nodes that are selected for expansion.

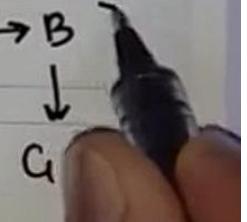
\hookrightarrow Eg:- i) Best fit Search ALGO
 ii) A* Search ALGO .



$$(A) f(n) = 1 + 1 = 2$$

$$5 \rightarrow D \quad f(n) = 5 + 4 = 9$$

$$A \rightarrow B \quad [f(n) = 3 + 2 = 5]$$



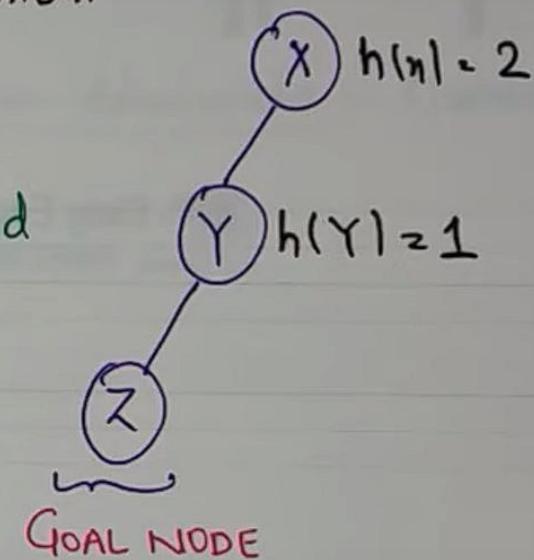
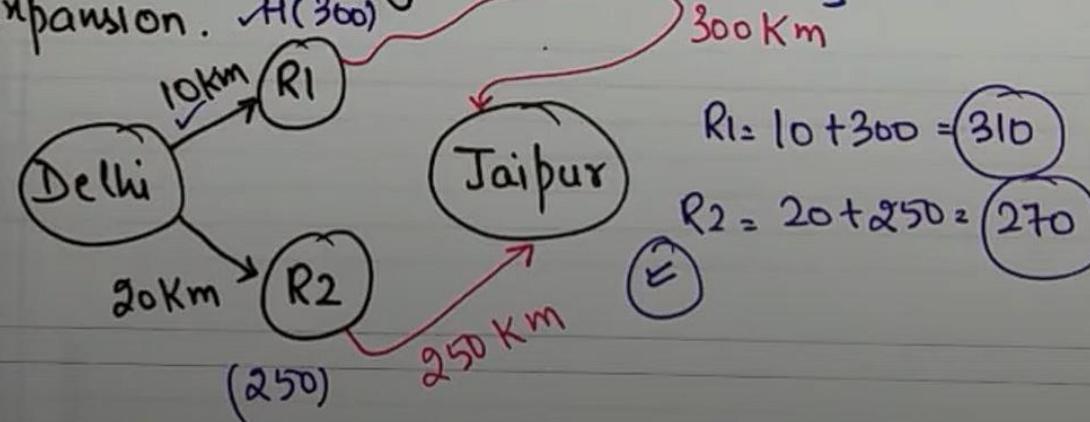
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Heuristic Search: Tries to Solve Problem in minimum

↳ Tries to optimize a problem using Steps/cost.
heuristic function. [Informed Search].

Heuristic Function: It is a function $h(n)$,
that gives an estimation on the cost of
getting from node ' n ' to the GOAL state.

[Helps in Selecting optimal node for
expansion. $h(300)$]





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Types of Heuristic: (underestimate)

→ i) Admissible: In this Heuristic function, never overestimates the cost of reaching the Goal. $H(n) \leq H'(n) \{ \text{Goal} \}$

→ $h(n)$ is always less than or equal to actual cost of lowest-cost path from node 'n' to goal.

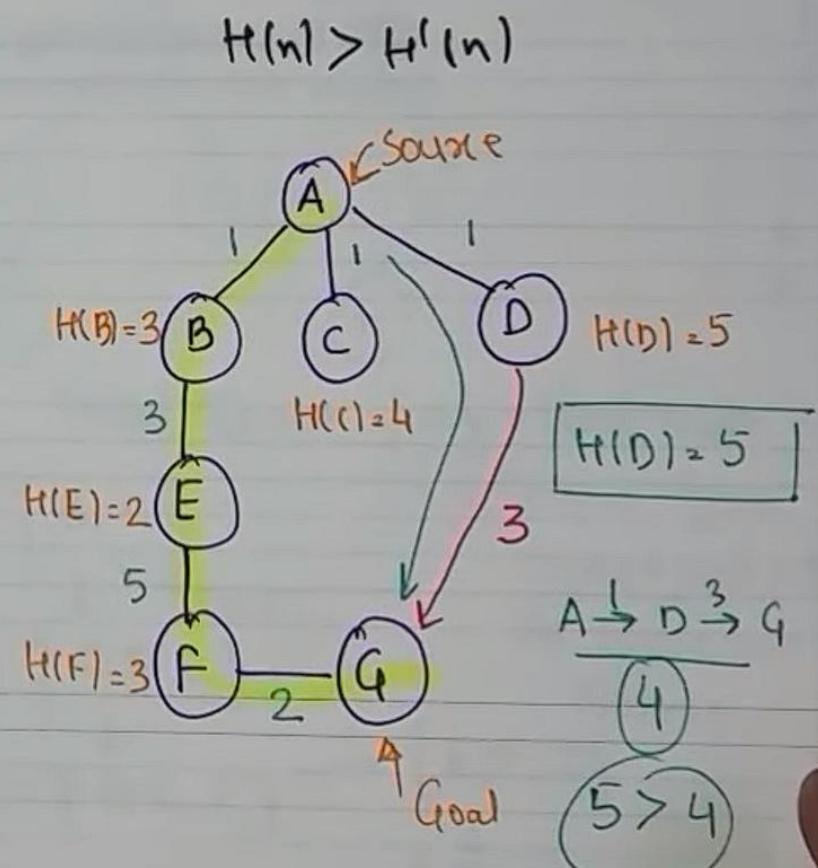
$$H(B)=3, H(C)=4, H(D)=5$$

$$f(n) = H(n) + G(n)$$

$$B=4, C=5, D=6.$$

Actual = 11

$$3 < 11$$



(AI78)



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Ques:- Differentiate b/w blind and heuristic Search.

Blind Search:- It is also known as unknown/uninformed Search.

↳ There is no infoⁿ about the Searching.

↳ No Knowledge of where the GOAL.

↳ Eg:- Depth first, Breadth first Search

↳ Efficiency is low

↳ Slower than Heuristic

↳ Large memory is used

↳ No funcⁿ (Special) is used.

Heuristic Search:- It is a method of Solving problems more easily and fast. They have knowledge of where goal or finish of the graph. (Informed Search)

Eg:- Hill climbing, A*, AO*

↳ Highly efficient ↳ less time
↳ less cost

↳ finds solⁿ quickly.

↳ no large memory is required.

↳ Heuristic funcⁿ is used.



BEST FIRST SEARCH: GREEDY SEARCH. (BFS) DFS

↳ Uses evaluation Algorithm (funcⁿ) to decide which adjacent node is most promising and then explore.

↳ Category of Heuristic or Informed Search.

↳ Priority Queue is used to store Cost of nodes.

ALGORITHM:

→ Sorted order.

Priority Queue 'PQ' containing initial States

Loop

if PQ = Empty Return FAIL

Else

NODE ← Remove_First(PQ)

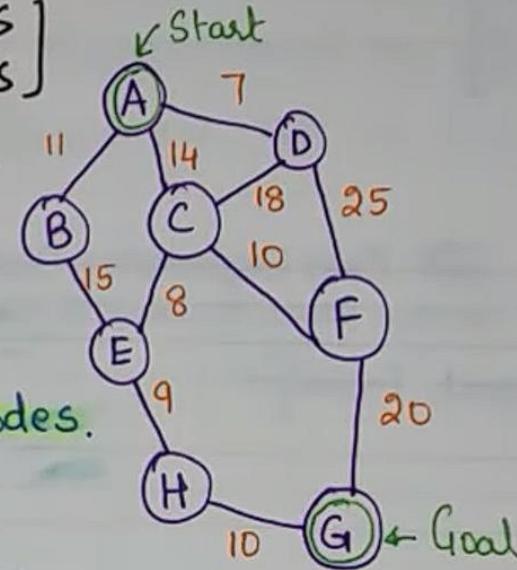
if NODE = GOAL

Return Path from Initial to NODE

Else

Generate all Successors of NODE
and insert newly generated NODE
into PQ according to cost value.

END LOOP



BEST FIRST SEARCH:

(REEDY SEARCH.)

[BFS
DFS]

↳ Uses evaluation Algorithm (funcⁿ) - to decide which adjacent node is most promising and then explore.

↳ Category of Heuristic or Informed Search.

↳ Priority Queue is used to store Cost of nodes.

ALGORITHM:

→ sorted order.

Priority Queue 'PQ' containing initial States

Loop

Space if PQ = Empty Return FAIL

Com:- $O(b^d)$ Else

NODE ← Remove_First(PQ)

T.C:- $O(b^d)$

if NODE = GOAL

b: branching factor

d: depth

END LOOP

Return Path from Initial to NODE

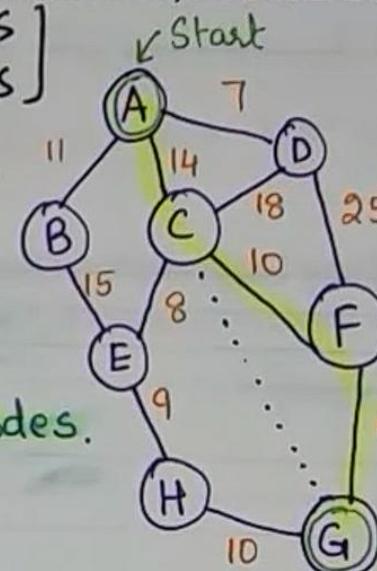
[B, D] [A, C]

Else Generate all Successors of NODE

[F, E, B, D] [A, C]

and insert newly generated NODE [E, B, D]

[A, C, F, G]



Straight Line distance.

$$A \rightarrow G = 40$$

$$B \rightarrow G = 32$$

$$C \rightarrow G = 25$$

$$D \rightarrow G = 35$$

$$E \rightarrow G = 19$$

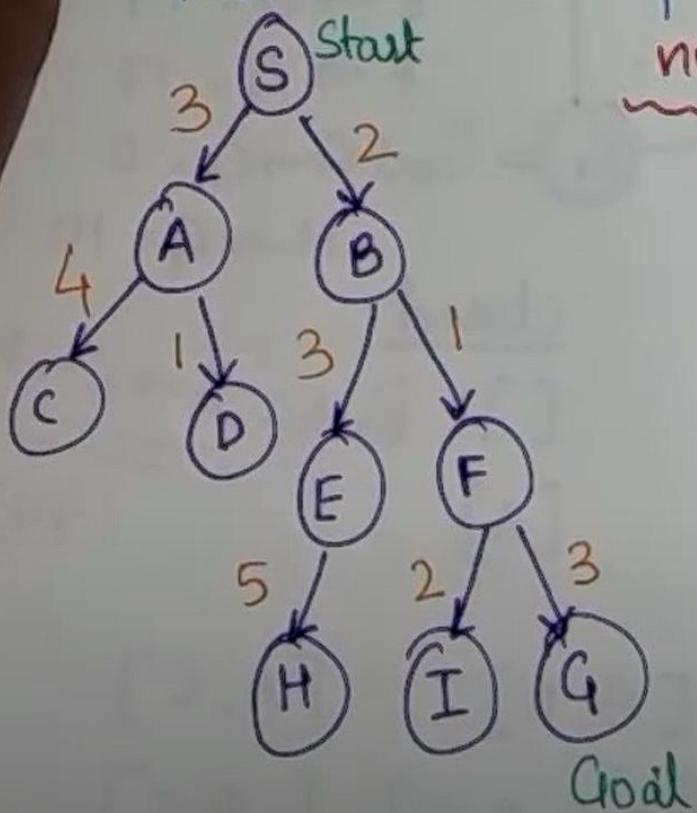
$$F \rightarrow G = 17$$

$$G \rightarrow G = 0$$

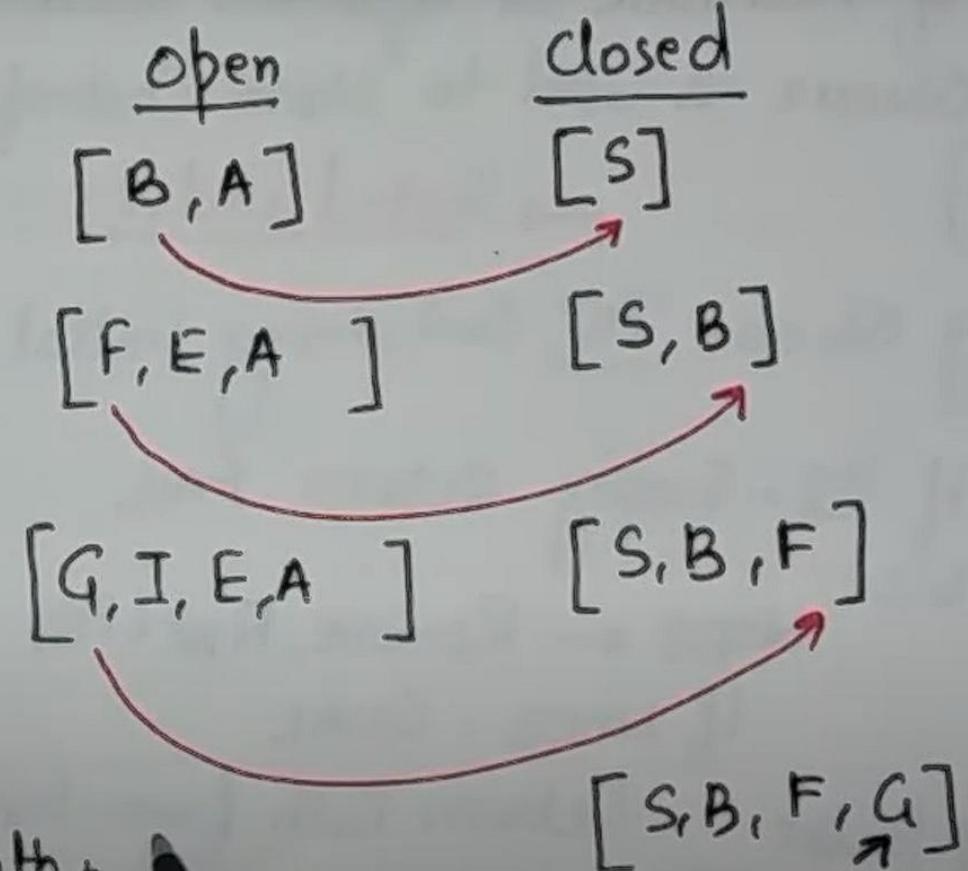
$$H \rightarrow G = 10$$

Path: A → C → F → G
(44)

Best First Search Example:



node(n)	$H(n)$
A	12
B	4
C	7
D	3
E	8
F	2
H	4
I	9
S	13
G	0



(A156)

Ques:- Explain A* Algorithm for Search.

↳ Uses heuristic funcⁿ $h(n)$ and cost to reach the node 'n' from start state $g(n)$.

↳ finds shortest path through search space.

↳ fast and optimal result.

$$f(n) = g(n) + h(n)$$

heuristic Value (child node)

estimated cost

Cost to reach node

ALGORITHM:

↳ i) Enter starting node in OPEN list.

ii) If OPEN list is empty return FAIL

iii) Select node from OPEN list which has smallest value ($g + h$).

↳ if node = Goal, return Success Goal

iv) Expand node 'n' and generate all successors

↳ Compute ($g + h$) for each successor node.

v) if node 'n' is already in OPEN/CLOSED, attach to backpointer.

vi) Go to (iii)

Advantages:-

- ↳ i) Best searching algorithms.
- ii) Optimal and complete.
- iii) Solving complex problems.

Disadvantages:-

- ↳ i) Doesn't always produce shortest.
- ii) Complexity issues.
- iii) Requires memory.

$$S \rightarrow A = 1 + 6 = 7 \checkmark$$

$$S \rightarrow B = 4 + 2 = 6 \checkmark$$

$$S \rightarrow B \rightarrow C = 4 + 2 + 1 = 7 \checkmark$$

$$S \rightarrow B \rightarrow C \rightarrow D = 4 + 2 + 3 + 0 = 9 \quad r_1$$

$$S \rightarrow A \rightarrow B = 1 + 2 + 2 = 5 \checkmark$$

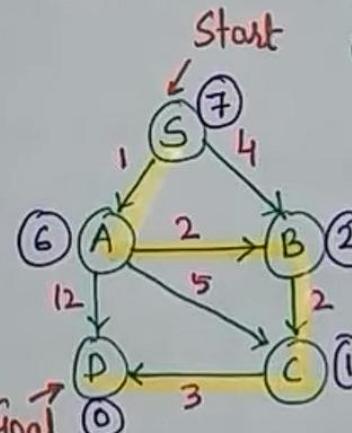
$$S \rightarrow A \rightarrow C = 1 + 5 + 1 = 7 \checkmark$$

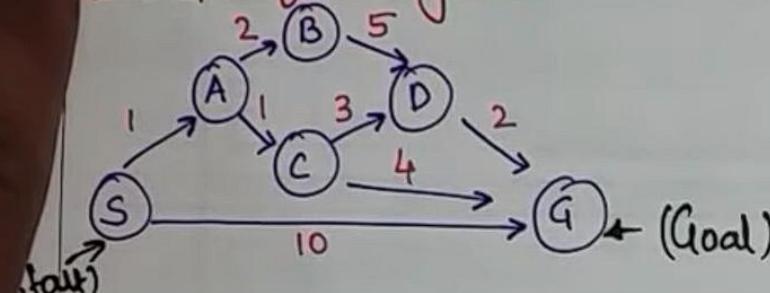
$$S \rightarrow A \rightarrow D = 1 + 12 = 13 \quad r_2$$

$$S \rightarrow A \rightarrow B \rightarrow C = 1 + 2 + 2 + 1 = 6 \checkmark$$

$$S \rightarrow A \rightarrow B \rightarrow C \rightarrow D = 1 + 2 + 2 + 3 = 8$$

$$S \rightarrow A \rightarrow C \rightarrow D = 1 + 5 + 3 = 9 \quad r_4$$



Example of A* Algorithm:-

State	$h(n)$
S	5
A	3
B	4
C	2
D	6
G	0

$$S \rightarrow A = 1 + 3 = 4$$

$$S \rightarrow G = 10 + 0 = 10$$

$$S \rightarrow A \rightarrow B = 1 + 2 + 4 = 7 \quad \checkmark$$

$$S \rightarrow A \rightarrow C = 1 + 1 + 2 = 4 \quad \checkmark$$

$$S \rightarrow A \rightarrow C \rightarrow D = 1 + 1 + 3 + 6 = 11 \quad \checkmark$$

$$S \rightarrow A \rightarrow C \rightarrow G = 1 + 1 + 4 = 6 \quad \checkmark$$

$$S \rightarrow A \rightarrow B \rightarrow D = 1 + 2 + 5 + 6 = 14 \quad \checkmark$$

$$S \rightarrow A \rightarrow C \rightarrow D \rightarrow G = 1 + 1 + 3 + 2 = 7 \quad \checkmark$$

$$S \rightarrow A \rightarrow B \rightarrow D \rightarrow G, 1 + 2 + 5 + 2 = 10$$

AI-9



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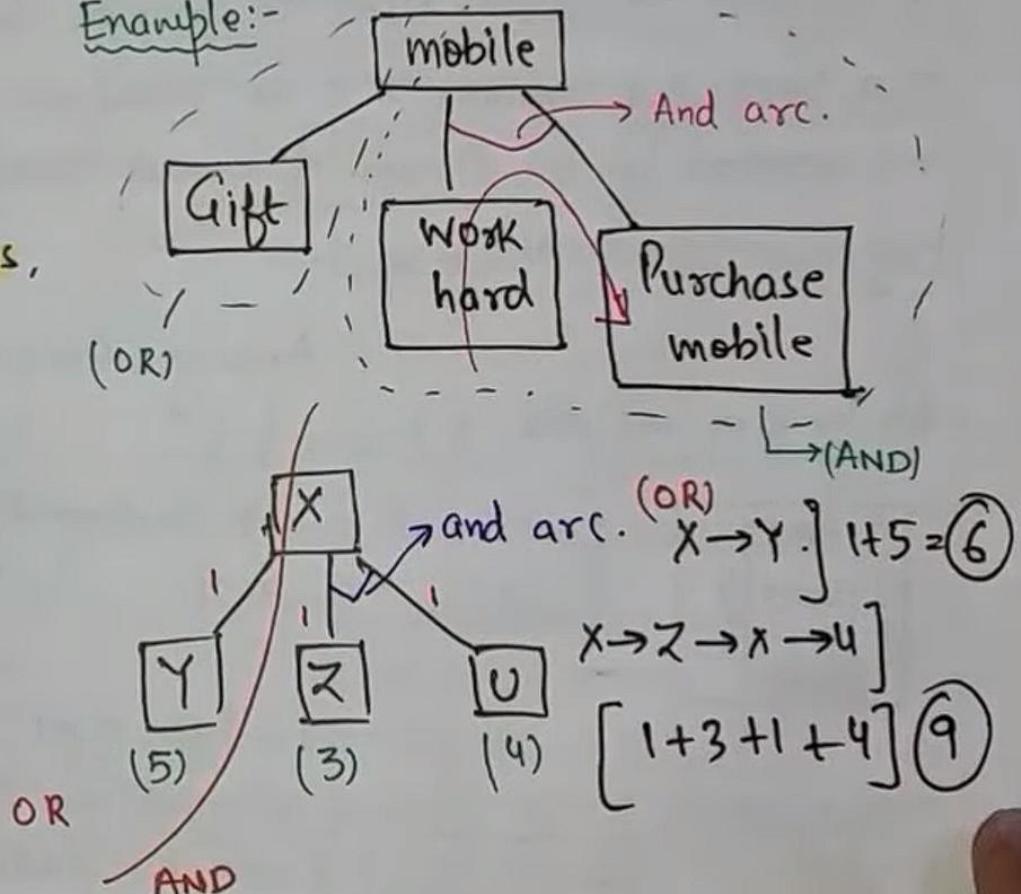
Ques:- Describe how Problem Reduction is done with AO*
Algorithm.

AND-OR Graphs:- useful for representing the problem solution that can be solved by decomposing them into smaller set of problems, all of which must be solved.
→ ANDARCS. } May point to 'n' no. of Successor nodes.

↳ Algo. like Best-fit Search can be used that has the ability to handle AND Arcs.

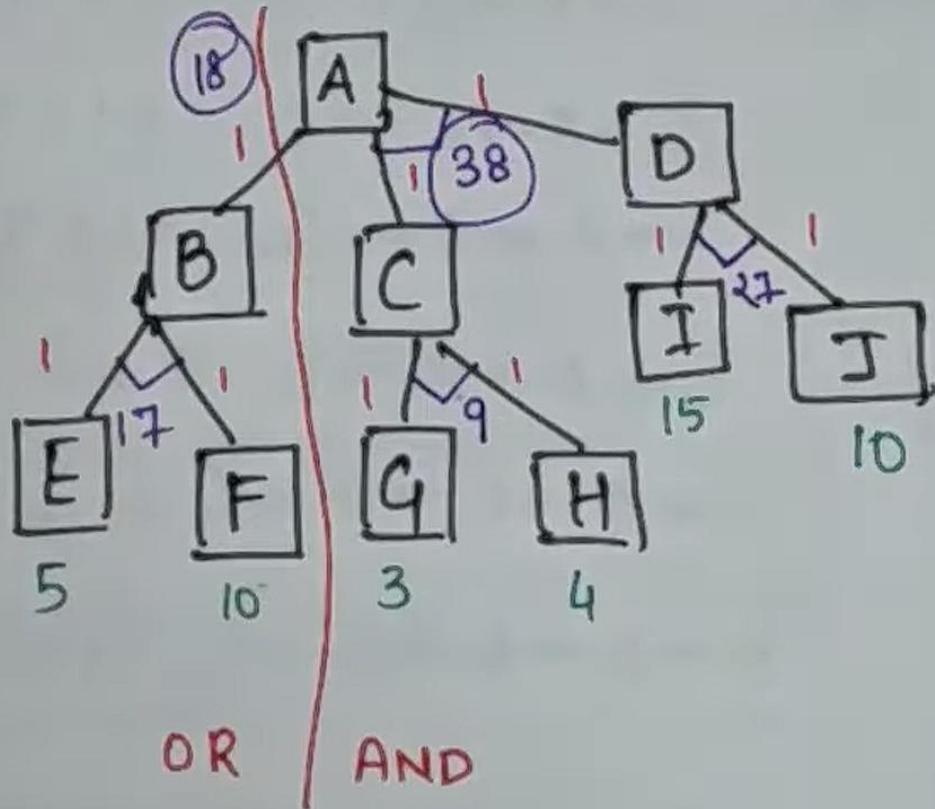
FUTILITY: Should be chosen to correspond to a threshold value. if Est. cost > futility.
Stop Search.

Example:-





Algo:-



Ques:- Write short note on "Hill-climbing Search" [→ Local Search algo] [→ Greedy Approach] No Backtracking.

↳ Variant of generate and test method in which feedback from test procedure is used to help generator decide which dirⁿ to move in search space.] always moves in a single dirⁿ.

↳ It is like DFS }

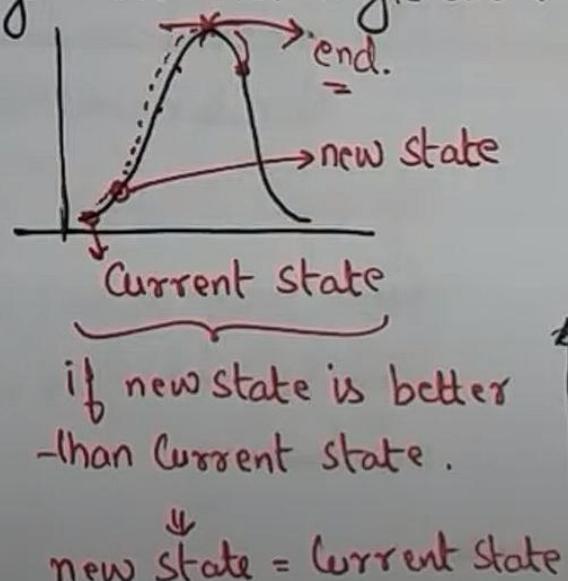
Eg:-

1	2	4
5		7
3	6	8

(Starting State)

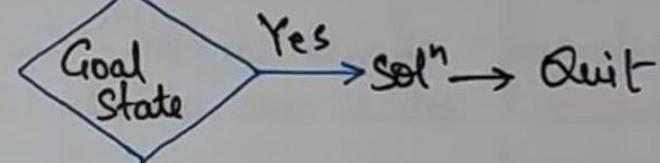
(4) (5) (6)

↳ we will choose this



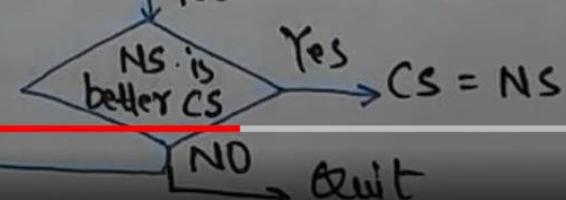
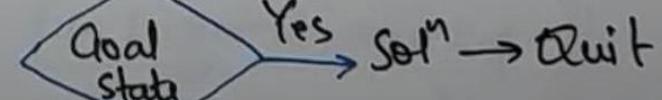
Flowchart :-

Evaluate Initial State



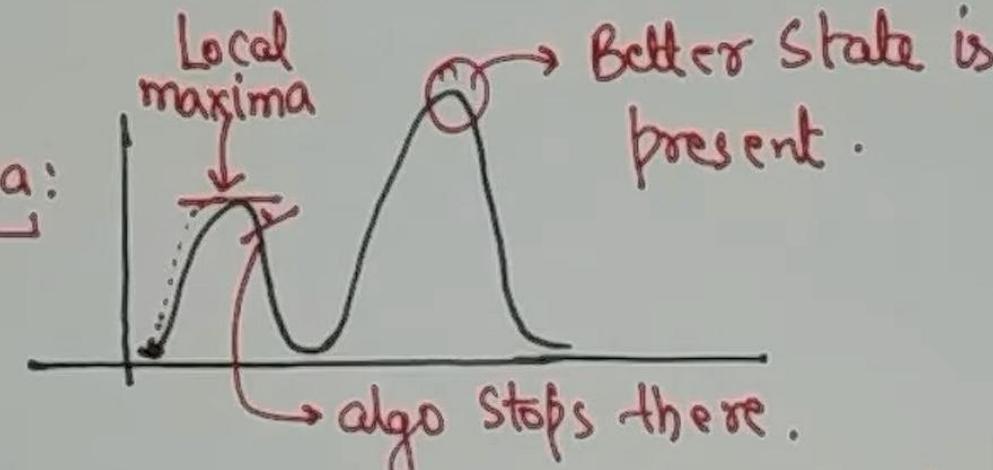
Current State = Initial State
 ↓ (CS)

Apply operator 'o' and get new state. (NS)

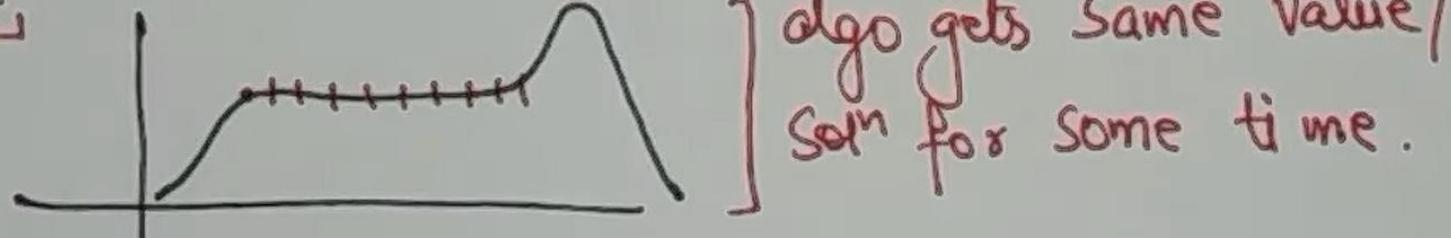


Limitations:-

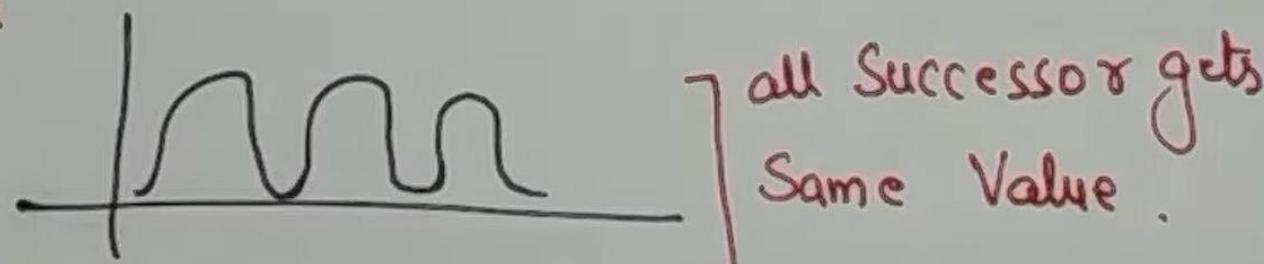
① Local maxima:



② Plateau:



③ Ridge:-



State Space Search: Used in Problem Solving.

→ It is a process used in A.I. in which successive configurations or states of an instance are considered with intention of finding a GOAL state with desired property.

→ Problems are modelled as State Space

→ Representation:

Set of all possible actions

$S: (S, A, Action(s), Result(s,a), Cost(s,a))$

Set of all possible states.

Funcⁿ [which action is possible for current state]

Funcⁿ [State reached by performing action 'a' on start 's']

Set of states in which a problem can be.

Start(s)

1	4	3
2		5
8	6	7

EIGHT TILE PUZZLE

GOAL(G)

1	2	3
8		4
7	6	5

Actions Possible:-
'Right'

Up
down
Left
Right

Legal moves for a state.

1	4	3
2	5	
8	6	7

new state($s1$)

right is not possible now
Up
down
Left

7	4	2
1	5	3
6	3	8

(START)

7	4	2
1	3	5
6	3	8

left

7	4	3
1	5	2
6	3	8

up

7	4	2
1	5	8
6	3	2

down

7	3	2
1	4	5
6	3	8

up

7	4	2
3	1	5
6	3	8

left

7	4	2
1	3	5
6	2	8

down

up

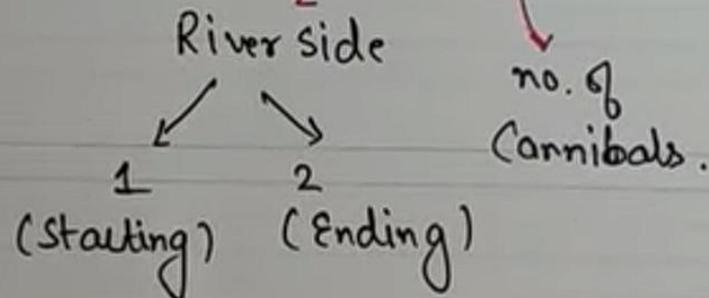
1	2	3
8	6	5
7	4	3

(GOAL)

Missionaries and Cannibals Problem:

- Missionaries and 3 Cannibals were on Side of the river.
- All want to cross the river.
 - On Same Side of river missionaries count can't be less than Cannibals.
 - Only one boat available that can hold only two people at a time.
- no. of missionaries

State Representation: $\langle R, M, C \rangle$



$\langle 1, 3, 3 \rangle \langle 2, 0, 0 \rangle$] Initial State



$\langle 1, 3, 1 \rangle \langle 2, 0, 2 \rangle$



$\langle 1, 3, 2 \rangle, \langle 2, 0, 1 \rangle$



$\langle 1, 3, 0 \rangle \langle 2, 0, 3 \rangle$



$\langle 1, 3, 1 \rangle, \langle 2, 0, 2 \rangle$



$\langle 1, 1, 1 \rangle \langle 2, 2, 2 \rangle$



$\langle 1, 2, 2 \rangle, \langle 2, 1, 1 \rangle$



$\langle 1, 0, 2 \rangle \langle 2, 3, 1 \rangle \rightarrow \langle 1, 0, 3 \rangle, \langle 2, 3, 0 \rangle$

$\langle 1, 0, 0 \rangle, \langle 2, 3, 3 \rangle \leftarrow \langle 1, 0, 2 \rangle \langle 2, 3, 1 \rangle \leftarrow \langle 1, 0, 1 \rangle \langle 2, 3, 2 \rangle$

L42: Tic Tac Toe Problem in Artificial Intelligence with Solution | AI Lectures in Hindi

EEC Classes GGSIPU, UPTU, Mumbai Univ., Pune Univ., GTU, Anna Univ., PTU and Others EEC Classes



TIC-TAC-TOE PROBLEM: {Zero-Kata}

TWO-Player Game where one player called **MAX** marks a letter '**X**' and the opponent called **MIN** marks a letter '**O**'.
↳ '3x3' Grid where two players put their letters.

↳ Player with same marks (three) in complete Row/ Column/ Diagonal wins the Game.

↳ Start State = Empty Grid.

↳ Goal State = Win for either of player

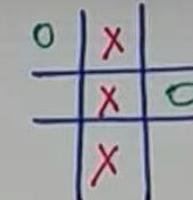
MAX

(3 consecutive X)

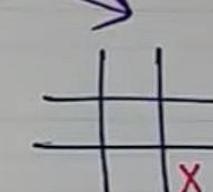
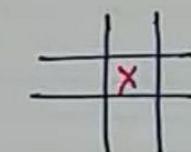
MIN

(2 consecutive O)

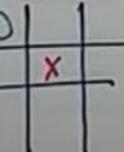
Example:



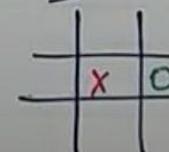
Initial State



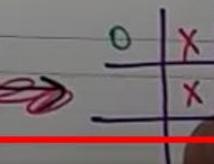
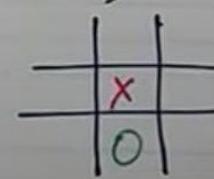
Informed States



Informed States



Informed States



MAX
ing



Travelling Salesman Problem and its State Representation.

Salesman has list of cities, each of which must be visited exactly once. Starting point.

↳ In List, there are direct roads b/w point. each pair of cities.

↳ To find Route, Salesman should follow shortest possible round trip.

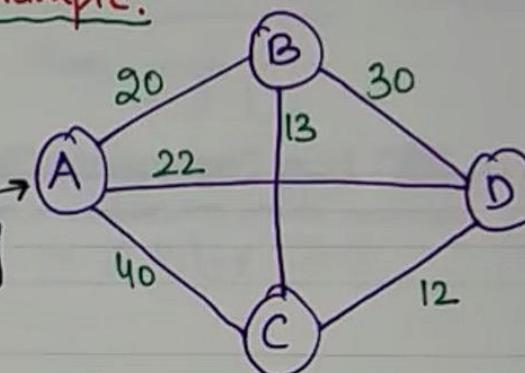
↳ State is represented as pair of any two cities and distance b/w them.

State Space:- Initial State (State A)

↳ $\{(A \xrightarrow{20} B), (A \xrightarrow{40} C), (A \xrightarrow{22} D)\}$

State

Example:



Possible Routes:-

$$(A \xrightarrow{20} B \xrightarrow{13} C \xrightarrow{12} D \xrightarrow{22} A) = 67 \checkmark$$

$$(A \rightarrow B \rightarrow D \rightarrow C \rightarrow A) = 102$$

$$(A \rightarrow D \rightarrow B \rightarrow C \rightarrow A) = 105$$

$$(A \rightarrow D \rightarrow C \rightarrow B \rightarrow A) = 67 \checkmark$$

$$(A \rightarrow C \rightarrow D \rightarrow B \rightarrow A) = 102$$

$$(A \rightarrow C \rightarrow B \rightarrow D \rightarrow A) = 105$$