

problem 2.

part (a): Runtime = $\Theta(n^2)$

```
for (int i=0 ; i < n ; i++)  
    for (int j=0 ; j < n ; j++)  
        s.push(j);  
}
```

$$1) \sum_{i=0}^n i = n + n-1 + \dots + 1 = \frac{(n+1)n}{2} = \Theta(n^2)$$

It's the same when it calls $s.pop()$

$$2) \sum_{i=0}^n i = n + n-1 + \dots + 1 = \frac{(n+1)n}{2} = \Theta(n^2)$$

3) for while loop
Because of the previous $pop()$ and push this nance
even got called.

$$\therefore \text{Total} = \Theta(n^2) + \Theta(n^2) \\ = \Theta(n^2)$$

Problem 2.

part (b)

when $\text{func}(0, n)$ is called

↓

$\text{func}(n-1, n-1)$

when $\text{curr} = n-1$,

it will call $\text{func}(\text{curr}-1, n)$ to reduce curr to 0
and then call $\text{func}(n-1, n-1)$ to start over, but
the time of iteration reduces 1.

$$\sum_{i=1}^n (n-i) = n-1 + n-2 + \dots + 1$$
$$= \frac{n(n-1)}{2} = \Theta(n^2)$$

problem 2

part (c)

1) $\text{for } (int\ i = 1; i \leq n; i++) \{$
 $q.enqueue(i)$
}

$$\sum_{i=1}^n i = n$$

2) For the while loop,

Because if when $(snap == true) \wedge (q.front == 1)$
it will run the for loop and ~~de~~ dequeue and delete
"1" from the queue.

therefore, the for loop will only run once.

\therefore In total, in order to eliminate the queue,
the total number of elements should be delete will be $2n$.

" To delete one element from queue,
it will have to run through both if and else, so
three $\Theta(1)$ statement to delete one element

$$\begin{aligned}\therefore \text{Total} &= n + 1 + n + 2n \cdot 3 \\ &= 8n + 1 \\ &= \Theta(n)\end{aligned}$$

problem 2
part (d)

1) Creating the linked ~~list~~ list

\therefore three statements per iteration

$$\therefore t_1 = 3n$$

2) for the for loop:

it will go through n times with $i = 1 \rightarrow n$
and every time it will go through the list from
the head to the tail.

and \therefore if $(curr \rightarrow \text{value} \% i == 0) \&\& (arr[i] == 0)$

\therefore The time that the inner for loop will run will
be $n + \frac{n}{2} + \frac{n}{3} + \frac{n}{4} + \dots + 1$

\therefore This is the worst case for $arr[i]$

\therefore assume $arr[i]$ is always 0.

\therefore the runtime for the inner loop will always
be n^2 every time

$$\therefore \text{Total} = 3n + n^2 \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + 1 \right)$$

$$= 3n + n^2 (\ln n)$$

$$= \Theta(n^2 \ln n)$$

$$= \Theta(n^2 \log n)$$

Problem 3

part (a)

The worst case runtime for somefunc is when bar() is called in the function.

$$\begin{aligned}\therefore \text{Runtime} &= \Theta(n^2) + \Theta(1) + \Theta(1) \\ &= \Theta(n^2)\end{aligned}$$

\therefore The worst case runtime is $\Theta(n^2)$

part (b)

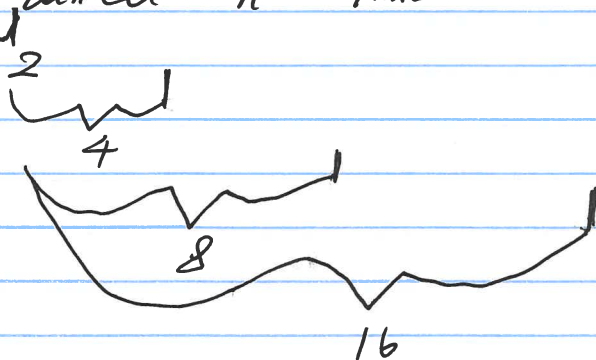
when $n=0$ and $\text{max}=1$

the function will increment n every time it goes into the somefunc()

when $n \neq \text{max}$, it will call foo() and increment n

when $n = \text{max}$, it will call bar() and double max

Therefore, when it's called n^{th} time
the call tree is



\therefore when n^{th} call, foo() will be called $n - \log n$ times
bar() will be called $\log n$ times
($n - \log n$) $\log n + \log n n^2$

$$\begin{aligned}\text{Amortised Runtime} &= \frac{(n - \log n) \log n + \log n n^2}{n} \\ &= \log n - \frac{\log n}{n} + n \log n \\ &= \Theta(n \log n)\end{aligned}$$

part (c)

It's similar to the part (c), but now $\text{bar}()$ has $\Theta(n^2)$
 foo takes $\Theta(n \log n)$

$$\text{amortised runtime} = \frac{(n - \log n) n \log n + n^2 \log n}{n}$$

$$= n \log n + \log n^2 + n \log n$$

$$= n \log n$$

$$= \underline{\underline{\Theta(n \log n)}}$$