

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB RECORD

Bio Inspired Systems (23CS5BSBIS)

Submitted by

Anish Budavi (1BM23CS401)

in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

(Autonomous Institution under VTU)

BENGALURU-560019

Sep-2024 to Jan-2025

B.M.S. College of Engineering,
Bull Temple Road, Bangalore 560019
(Affiliated To Visvesvaraya Technological University, Belgaum)
Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “ Bio Inspired Systems (23CS5BSBIS)” carried out by **Anish Arjun Budavi (1BM23CS401)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

Prof. Surabhi S Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
--	--

Index

Sl. No.	Date	Experiment Title	Page No.
1	9-10-24	Genetic Algorithm	1-6
2	16-10-24	Ant Colony Optimization	7-16
3	30-10-24	Particle Swarm Optimization	17-21
4	13-11-24	Cuckoo Search Algorithm	22-27
5	20-11-24	Grey Wolf Optimizer	28-33
6	27-11-24	Parallel Cellular Algorithm	34-37
7	4-12-24	Gene Expression Algorithm	38-42

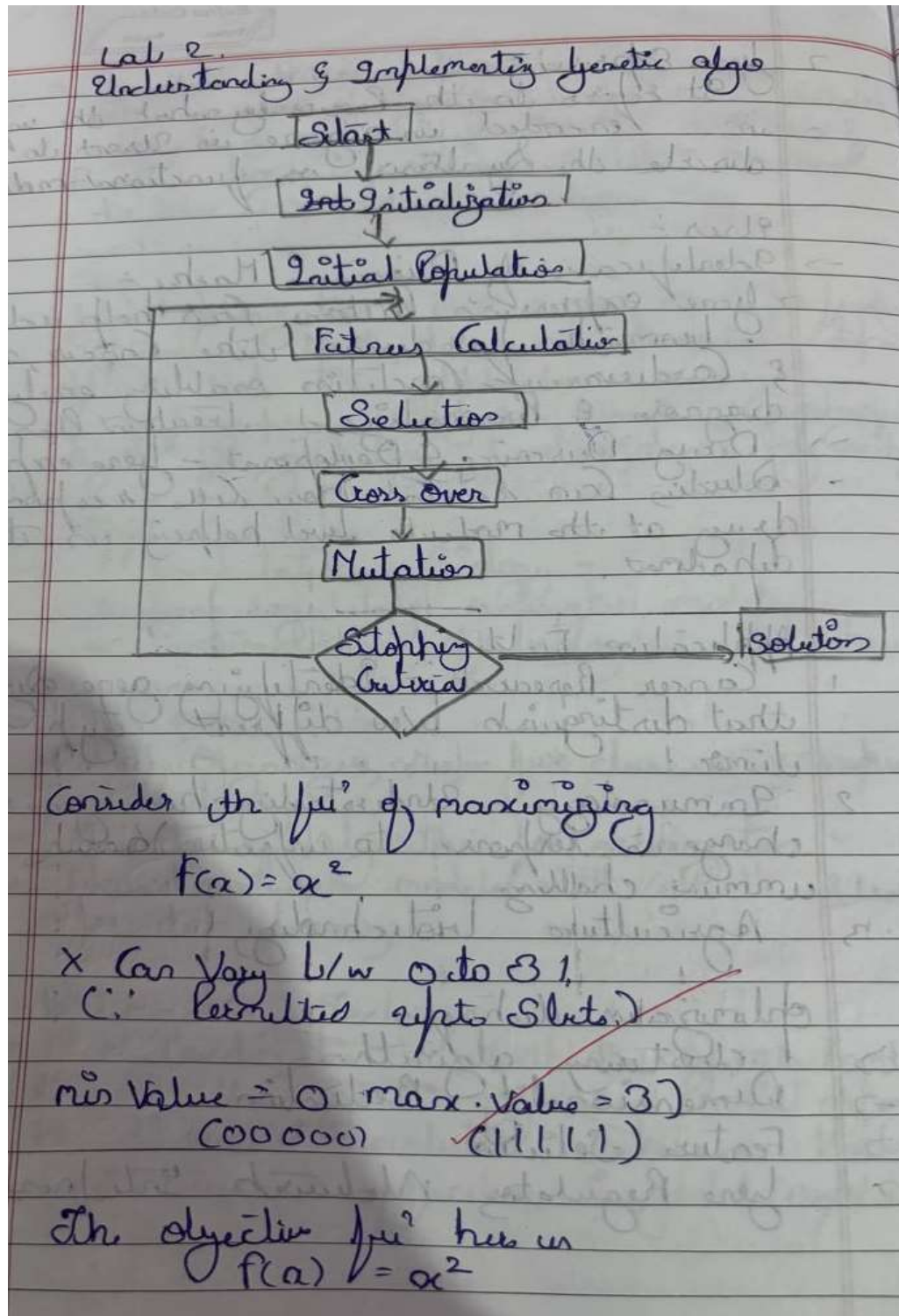
Github Link:

<https://github.com/Anishbudavi/ANISH-BUDAVI-1BM23CS401-BIS-LAB.git>

Program 1

Genetic Algorithm for Optimization Problems

Algorithm:



Step 1: Selecting Initial Population.
Let's randomly select.
Here initial Population of size A is
chosen.

Initial Population (randomly chosen) \rightarrow 011001

110001
00100
10010

now
Calculate Fitness Value

~~Serial~~ ~~initial~~ ~~Popl~~ ~~X Value~~ ~~Fitness~~ ~~Real~~ ~~% Real~~ ~~Expected~~ ~~n~~
 ~~$f(x) \cdot n^2$~~ ~~Count~~

S/No	initial Popl	X Value	Fitness $f(x) \cdot n^2$	Real	% Real	Expected Count	Actual Count
1	01101	13	169	0.155	15.5	0.6230	1
2	11000	24	576	0.5208	52.08	2.1235	2
3	00100	4	16	0.0147	1.47	0.0589	0
4	10010	18	324	0.8206	82.06	1.1944	1
Sum			1085	1.0	100	4.0	4
avg			271.25	0.25	25	1	1
Max			576	0.5208	52.08	2.1235	2

~~Expt~~ ~~F(x)~~
~~Avg (2 F(x))~~

$$P(x) = \frac{FC(x)}{\sum FC(x)} \Rightarrow \frac{(18)^2}{1085} \rightarrow \frac{(24)^2}{1085}$$

$$\Rightarrow \frac{(24)^2}{1085} \quad \frac{(18)^2}{1085}$$

$$\text{Expected Count} = \frac{P(x)}{\text{Avg}(\sum FC(x))}$$

String no	Matrix Pool	Crossover Count	offspring after Crossover	X Value	Fitness $F(x) = x^2$
1	01101	32	01100	12	144
2	11000		11001	25	25
3	11000	2	11010	26	676
4	10010		10000	16	256
Sum					1701
avg					425.25
max					676

The fitness values 676 is higher than earlier 576

Mutation

String no	offspring after Crossover	Mutation Chromosome for offspring	offspring after Mutation	X value	Fitness $F(x) = x^2$
1	01106	10000	11100	28	784
2	11001	00000	11001	25	625
3	11010	00000	11010	26	676
4	10000	00101	101001	21	441
Sum					2526
avg					631.5
max					784

784 > 676
Current Revers
Max Max

Complete the
algorithm.

Step 2: Fitness Calculation & Selection

Step 3: Crossover

Mating Pool: So from the mating pool we
look into the actual Count of fitness.
Calculation Table: no. of Values in actual
Fitness Column in the number of times that
Value will be used in Mating Pool

Step 4: Mutation of the Crossover.

Code:

```
import random
# Set a random seed for reproducibility
random.seed(42)
def fitness(chromosome):
    x = int("".join(map(str, chromosome)), 2)
    return x ** 2

def binary_string_to_chromosome(binary_string):
    return [int(bit) for bit in binary_string]

def generate_population_from_input():
    population = []
    for _ in range(population_size):
        while True:
            binary_string = input("Enter a binary string of size 5 (e.g., '11001'): ")
            if len(binary_string) == 5 and all(bit in '01' for bit in binary_string):
                population.append(binary_string_to_chromosome(binary_string))
                break
            else:
                print("Invalid input. Please enter a binary string of size 5.")
    return population

def select_pair(population, fitnesses):
    total_fitness = sum(fitnesses)
    selection_probs = [f / total_fitness for f in fitnesses]
    parent1 = population[random.choices(range(len(population)), selection_probs)[0]]
    parent2 = population[random.choices(range(len(population)), selection_probs)[0]]
    return parent1, parent2

def crossover(parent1, parent2):
    point = random.randint(1, len(parent1) - 1)
    offspring1 = parent1[:point] + parent2[point:]
    offspring2 = parent2[:point] + parent1[point:]
    return offspring1, offspring2

def mutate(chromosome, mutation_rate):
    return [gene if random.random() > mutation_rate else 1 - gene for gene in chromosome]

# Parameters
population_size = 4
generations = 20
```



```

mutation_rate = 0.01

# Initialize population from user input
population = generate_population_from_input()

for generation in range(generations):
    fitnesses = [fitness(chromosome) for chromosome in population]

    new_population = []

    # Create new population
    while len(new_population) < population_size:
        parent1, parent2 = select_pair(population, fitnesses)
        offspring1, offspring2 = crossover(parent1, parent2)
        new_population.append(mutate(offspring1, mutation_rate))
        new_population.append(mutate(offspring2, mutation_rate))

    # Ensure the new population has the right size
    population = new_population[:population_size]

# Get the maximum fitness
fitnesses = [fitness(chromosome) for chromosome in population]
max_fitness = max(fitnesses)

print(f"Maximum Possible Fitness: {max_fitness}")

```

Output:

```

Enter a binary string of size 5 (e.g., '11001'): 11011
Enter a binary string of size 5 (e.g., '11001'): 01011
Enter a binary string of size 5 (e.g., '11001'): 11100
Enter a binary string of size 5 (e.g., '11001'): 01101
Maximum Possible Fitness: 841

```

Program 2

Ant Colony Optimization

Algorithm:

Ant Colony Optimization
Marco Dorigo in 1992

- the main inspiration of the ACO algorithm comes from stigmergy
- Stigmergy refers to the interaction & coordination of organisms in nature by modifying the environment

Ant & Stigmergy

- It produces chemicals called Pheromones
- They use Pheromones to communicate
- this is similar to water in our analogy
- They use a very simple technique our analogy to find the shortest path from them to a source of food they make decision based on probability

Mathematical Model of ACO

- Pheromone (Model & Vaporization)
- Decision Making

Pheromone Matrix

$\Delta \tau_{ij}^k = \begin{cases} 1/LK & \text{if } k^{\text{th}} \text{ ant travels on edge } i \rightarrow j \\ 0 & \text{otherwise} \end{cases}$

- To Calculate the amount of a Pheromone

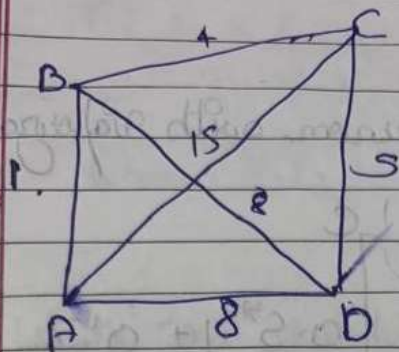
$\tau_{ij}^k = \sum_{k=1}^m \Delta \tau_{ij}^k$ without Vaporization

with Vaporization

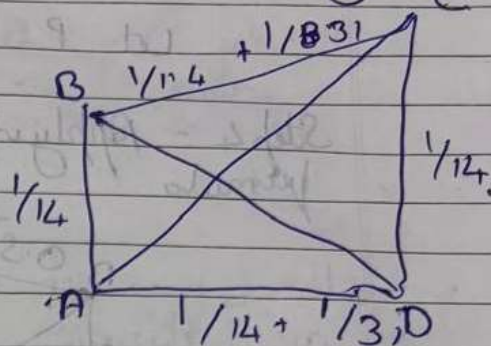
$\tau_{ij}^k = (1 - \rho) \tau_{ij}^k + \sum_{k=1}^m \Delta \tau_{ij}^k$ with Vaporization

ρ is a Constant

Cost graph.

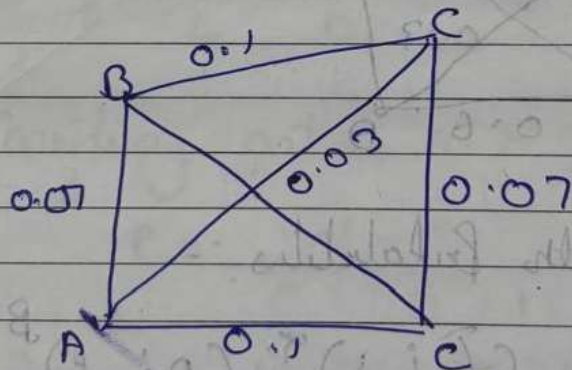


Maximum graph

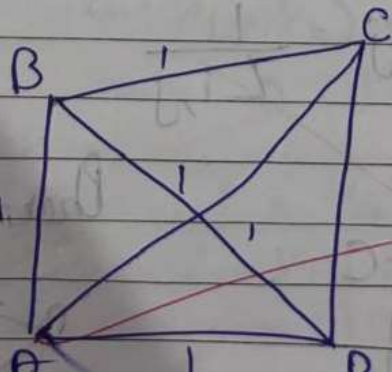


Ans 1 $L_1 = 14 \rightarrow A \bar{L}_{i,j} = 1/14, \bar{L}_{i,j} \leq \sum_{k=1}^m \bar{L}_{i,j}^k$
 Ans 2 $L_2 = 31 \rightarrow \Delta \bar{L}_{i,j} = 1/31$

Step 2: Maximum graph.



Step 3

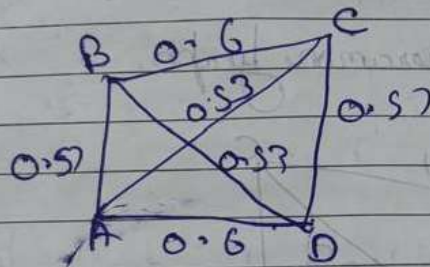
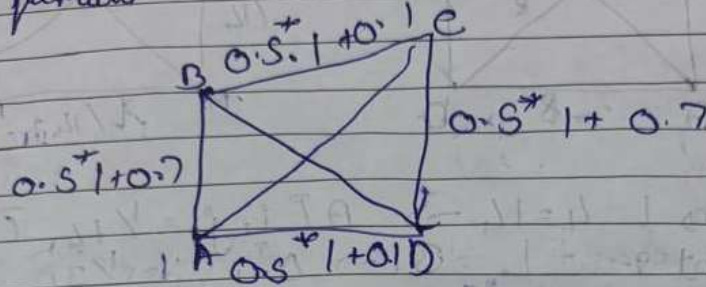


We assume weight is $L_{i,j} = \bar{L}_{i,j}$

$$\bar{L}_{i,j} = (1-P) \bar{L}_{i,j} + \sum_{k=1}^m D^k \bar{L}_{i,j}$$

Let $P = 0.5$

Step 4: Applying theorem with vaporization formula

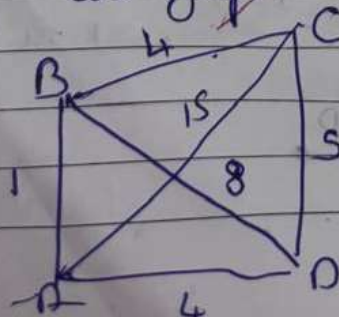


Calculating the Probabilities:-

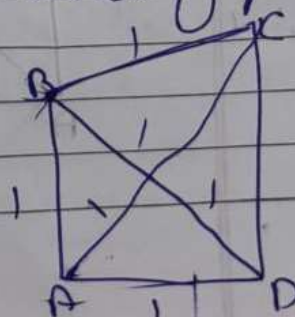
$$P_{i,j} = \frac{(\bar{L}_{i,j})^T (n_{i,j})^B}{\sum ((\bar{L}_{i,j})^T (n_{i,j})^B)}$$

When $n_{i,j} = \frac{1}{\bar{L}_{i,j}}$

Eg Cost graph



Thermone graph

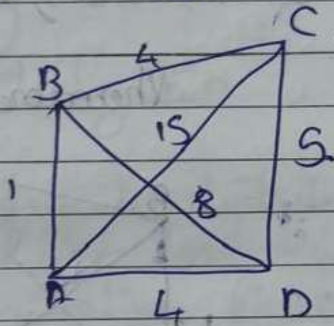


Considering Calculating the Probabilities :-

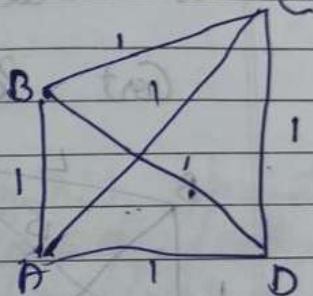
$$P_{i,j} = \frac{(\tau_{i,j})^\alpha (\eta_{i,j})^\beta}{\sum_k ((\tau_{i,k})^\alpha (\eta_{i,k})^\beta)}$$

$$\text{where } \eta_{i,j} = \frac{1}{L_{i,j}} \quad \alpha = 1, \beta = 1$$

Eg: cost graph



Prisoner graph



Considering ant as on A, has to make dec

for Edge
A, B

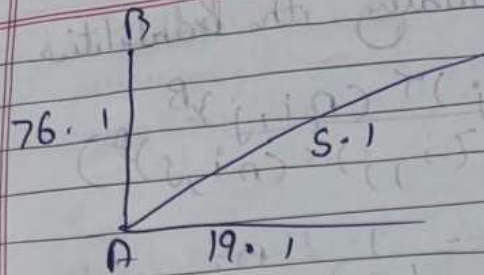
$$P = \frac{1 \times 1/1}{(1 \times 1/1) + (1 \times 1/15) + (1 \times 1/4)} \Rightarrow 0.7595$$

for Edge
A, C

$$P = \frac{1 \times 1/15}{(1 \times 1/1) + (1 \times 1/15) + (1 \times 1/4)} \Rightarrow 0.0506$$

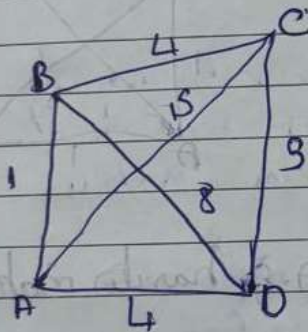
for Edge
A, D

$$P = \frac{1 \times 1/4}{(1 \times 1/1) + (1 \times 1/15) + (1 \times 1/4)} \Rightarrow 0.1899$$

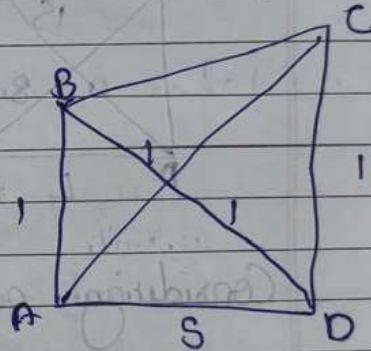


This shows the impact of Cost when we have same Phoron in the Deg - we will see the Phoron level on A to D & see the impact

Cost Path



Phoron Cost



$$A \text{ to } B = \frac{1 \times 1/1}{1 \times 1/1 + (1 \times 1/5) + (5 \times 1/4)} \Rightarrow 0.4317 = 43\%$$

$$A \text{ to } C = \frac{1 \times 1/5}{(1 \times 1/1) + (1 \times 1/5) + (5 \times 1/4)} \Rightarrow 0.5396 = 54\%$$

Now the path which will be chosen is A to D
 Path Solution - It is based on method called
 Roulette wheel where we use the selection path of
 genetic algorithm

Probabilities 0.76 | 0.19 | 0.05

Cumulative Sum $[1 \mid 0.24 \mid 0.08]$

Now We Select from Cumulative Sum for
that We generate a random (x) in
 $[0, 1]$

$\begin{cases} 0.24 < x < 1.00 \end{cases}$ We choose A to B (left)
 $\begin{cases} 0.08 < x \leq 0.24 \end{cases}$ We choose A to D (from)
 $\begin{cases} 0.00 \leq x \leq 0.08 \end{cases}$ We choose A to C (right)

Algorithm

Initialization

- Define the distance matrix which represents the cost b/w each pair of nodes
- Initialize pheromone level on all edges uniformly
- Set Parameters such as the no of ants, the no of best to consider, the no of iterations, pheromone decay rate & the duration of pheromone & distance on path selected

Iteration :-

Generate Path :-

- For each ant generate a complete path starting from a designated starting node
- Keep track of visited nodes to avoid cycles
- For each node, choose the next node based on pheromone level & distance using a probabilistic selection
- Once an ant completes its path return

=> the starting node
evaluate Path

Calculate the total distance of each Path
generated by ants.

update Pheromone levels

=> Sort the Path based on this distance &
Select the best n -best Path.

=> For each move in these best Paths increase
the Pheromone level on that Path based
on the inverse of the distance

=> Apply Pheromone decay to all Paths &
simulate evaporation

=> update Shortest Paths
Keep track of the Shortest Path
found so far during the iterations

O/P

After completing the iterations return the
best Path

By
23.10

Code:

```
import random
import numpy as np
import operator

FUNCTIONS = {'+': operator.add, '-': operator.sub, '*': operator.mul, '/': operator.truediv}
TERMINALS = ['x', 1, 2, 3, 4] # x and constants

def random_gene(length=10):
    return [random.choice(list(FUNCTIONS.keys()) + TERMINALS) for _ in range(length)]

def decode_chromosome(chromosome, x):
    stack = []
    for gene in chromosome:
        if gene in FUNCTIONS: # If it's a function, pop arguments and apply
            if len(stack) < 2: # Avoid errors if stack has fewer than 2 elements
                stack.append(0)
                continue
            b = stack.pop()
            a = stack.pop()
            try:
                result = FUNCTIONS[gene](a, b)
            except ZeroDivisionError:
                result = 1 # Avoid division by zero
            stack.append(result)
        elif gene == 'x':
            stack.append(x)
        else:
            stack.append(gene)
    return stack[0] if stack else 0 # Return top of stack as output

def fitness_function(chromosome, target_function, x_values):
    predictions = [decode_chromosome(chromosome, x) for x in x_values]
    targets = [target_function(x) for x in x_values]
    mse = np.mean([(p - t) ** 2 for p, t in zip(predictions, targets)])
    return mse

def selection(population, fitnesses):
    total_fitness = sum(1 / (f + 1e-6) for f in fitnesses) # Avoid division by zero
```

```

probabilities = [(1 / (f + 1e-6)) / total_fitness for f in fitnesses]
return population[np.random.choice(len(population), p=probabilities)]

def mutate(chromosome, mutation_rate=0.1):
    new_chromosome = chromosome[:]
    for i in range(len(new_chromosome)):
        if random.random() < mutation_rate:
            new_chromosome[i] = random.choice(list(FUNCTIONS.keys()) + TERMINALS)
    return new_chromosome

def crossover(parent1, parent2):
    point = random.randint(1, len(parent1) - 1)
    child1 = parent1[:point] + parent2[point:]
    child2 = parent2[:point] + parent1[point:]
    return child1, child2

def ant_colony_optimization(cost_matrix, n_ants=10, n_iterations=100, evaporation_rate=0.5,
alpha=1, beta=2):
    n_nodes = len(cost_matrix)
    pheromones = np.ones((n_nodes, n_nodes)) # Initialize pheromones

    def calculate_probability(i, j, visited):
        if j in visited:
            return 0
        return (pheromones[i][j] ** alpha) * ((1 / cost_matrix[i][j]) ** beta)

    def construct_solution():
        path = [random.randint(0, n_nodes - 1)]
        while len(path) < n_nodes:
            i = path[-1]
            probabilities = [calculate_probability(i, j, path) for j in range(n_nodes)]
            total = sum(probabilities)
            probabilities = [p / total if total > 0 else 0 for p in probabilities]
            next_node = np.random.choice(range(n_nodes), p=probabilities)
            path.append(next_node)
        path.append(path[0]) # Return to start
        return path

    def path_cost(path):
        return sum(cost_matrix[path[i]][path[i + 1]] for i in range(len(path) - 1))

    best_path = None

```



```

best_cost = float('inf')

for iteration in range(n_iterations):
    solutions = [construct_solution() for _ in range(n_ants)]
    costs = [path_cost(solution) for solution in solutions]
    for i, cost in enumerate(costs):
        if cost < best_cost:
            best_cost = cost
            best_path = solutions[i]

    pheromones *= (1 - evaporation_rate) # Evaporation
    for i, solution in enumerate(solutions):
        for j in range(len(solution) - 1):
            pheromones[solution[j]][solution[j + 1]] += 1 / costs[i]

    print(f"Iteration {iteration + 1}: Best Cost = {best_cost}")

print("Best Path:", best_path)
print("Best Cost:", best_cost)

cost_matrix = [
    [0, 2, 2, 5, 7],
    [2, 0, 4, 8, 2],
    [2, 4, 0, 1, 3],
    [5, 8, 1, 0, 2],
    [7, 2, 3, 2, 0]
]
ant_colony_optimization(cost_matrix, n_ants=5, n_iterations=20)

```

Output:

```

Iteration 15: Best Cost = 9
Iteration 16: Best Cost = 9
Iteration 17: Best Cost = 9
Iteration 18: Best Cost = 9
Iteration 19: Best Cost = 9
Iteration 20: Best Cost = 9
Best Path: [1, 0, 2, 3, 4, 1]
Best Cost: 9

```

Program 3

Particle Swarm Optimization

Algorithm:

Bafna Gold
Date: Page:

PSO:- Particle Swarm Optimization
PSO is a powerful meta-heuristic optimization algorithm & by Swarm behaviour. Observed in nature such as birds schooling it is a simplified social system.

- Cognitive Co-efficient :- It influences how much a Particle relies on its best known Particle.
- Social Co-efficient :- It determines the influence of the global best position found by Swarm.

PSO algorithm

- Initialize the Particle Population array $x \Rightarrow$ loop
- For each Particle Calculate the fitness using the fitness function $f(x-i)$
- Compare the Current fitness Value with its best. Replace the best with the Current Value $x-i$ if it is better than the best.
- Check the Swarm best Particle from under - check Particle best & assign the best array to the global best P_g
- Calculate the Velocity $(V-i(t+1))$ & update the position of the Particle to $x-i(t+1)$
- If a Termination is met exit the loop
- End loop

Ex. Let Consider we have to find the Minimum Value $f(x, y) = x^2 + y^2$ it has a minimum at point $(0, 0)$

Initialization - imagine we have a Swarm Particle each particle represents a Potential Solⁿ Positioned in a Search Space
no of Particles 5.

initial random Particle

P_1, P_2, P_3, P_4, P_5

evaluate fitness:

$$P_1: f(x, y) = x^2 + y^2$$

$$P_2 = P_3 = P_4 = P_5$$

⇒ update the Personal & Global best
Each Particle remembers its best position
Swarm identifies the best position found by the Particle

⇒ update Velocity & its Position
based on their own experience & global best

⇒ Global - Repeat for a lot of iteration
Particles explore Space based on their updated Velocity

⇒ Continuously evaluate the fitness

Convergence - after several iteration the Particle will cluster around global best position $(0, 0)$ as the best min. value

Code:

```
import random
import numpy as np
from matplotlib import pyplot as plt
from matplotlib import animation

def fitness_function(x1, x2):
    f1 = x1 + 2 * -x2 + 3
    f2 = 2 * x1 + x2 - 8
    z = f1**2 + f2**2
    return z

def update_velocity(particle, velocity, pbest, gbest, w_min=0.5, max=1.0, c=0.1):
    new_velocity = np.zeros_like(particle)
    r1 = random.uniform(0, max)
    r2 = random.uniform(0, max)
    w = random.uniform(w_min, max)

    for i in range(len(particle)):
        new_velocity[i] = (w * velocity[i] +
                           c * r1 * (pbest[i] - particle[i]) +
                           c * r2 * (gbest[i] - particle[i]))
    return new_velocity

def update_position(particle, velocity):
    new_particle = particle + velocity
    return new_particle

def pso_2d(population, dimension, position_min, position_max, generation, fitness_criterion):
    # Initialization
    particles = np.array([[random.uniform(position_min, position_max) for _ in range(dimension)] for
                           _ in range(population)])
    pbest_position = particles.copy()
    pbest_fitness = np.array([fitness_function(p[0], p[1]) for p in particles])

    gbest_index = np.argmin(pbest_fitness)
    gbest_position = pbest_position[gbest_index]

    velocity = np.zeros((population, dimension))

    images = [] # For animation
```



```

for t in range(generation):
    if np.average(pbest_fitness) <= fitness_criterion:
        break

    for n in range(population):
        velocity[n] = update_velocity(particles[n], velocity[n], pbest_position[n], gbest_position)
        particles[n] = update_position(particles[n], velocity[n])

    pbest_fitness = np.array([fitness_function(p[0], p[1]) for p in particles])
    for n in range(population):
        if pbest_fitness[n] < fitness_function(pbest_position[n][0], pbest_position[n][1]):
            pbest_position[n] = particles[n]

    gbest_index = np.argmin(pbest_fitness)
    gbest_position = pbest_position[gbest_index]

    # Plotting the current positions of the particles
    fig = plt.figure(figsize=(10, 10))
    ax = fig.add_subplot(111, projection='3d')
    ax.set_xlabel('x')
    ax.set_ylabel('y')
    ax.set_zlabel('z')

    x = np.linspace(position_min, position_max, 80)
    y = np.linspace(position_min, position_max, 80)
    X, Y = np.meshgrid(x, y)
    Z = fitness_function(X, Y)
    ax.plot_wireframe(X, Y, Z, color='r', linewidth=0.2)

    ax.scatter3D(
        particles[:, 0],
        particles[:, 1],
        [fitness_function(p[0], p[1]) for p in particles],
        c='b'
    )

    # Capture the frame for animation
    plt.title(f'Generation: {t + 1}')
    plt.tight_layout()
    plt.savefig(f'frame_{t}.png')
    plt.close(fig)

```



```

# Create animation
frames = [plt.imread(f'frame_{i}.png') for i in range(t)]
fig, ax = plt.subplots(figsize=(10, 10))
ax.axis('off')
image = ax.imshow(frames[0])

def update(frame):
    image.set_array(frames[frame])
    return image,

ani = animation.FuncAnimation(fig, update, frames=len(frames), interval=100)
ani.save('./pso_simple.gif', writer='pillow')

# Print the results
print('Global Best Position: ', gbest_position)
print('Best Fitness Value: ', min(pbest_fitness))
print('Average Particle Best Fitness Value: ', np.average(pbest_fitness))
print('Number of Generations: ', t)

# Run the PSO algorithm
pso_2d(population=30, dimension=2, position_min=-10, position_max=10, generation=100,
fitness_criterion=1e-3)

```

Output:

```

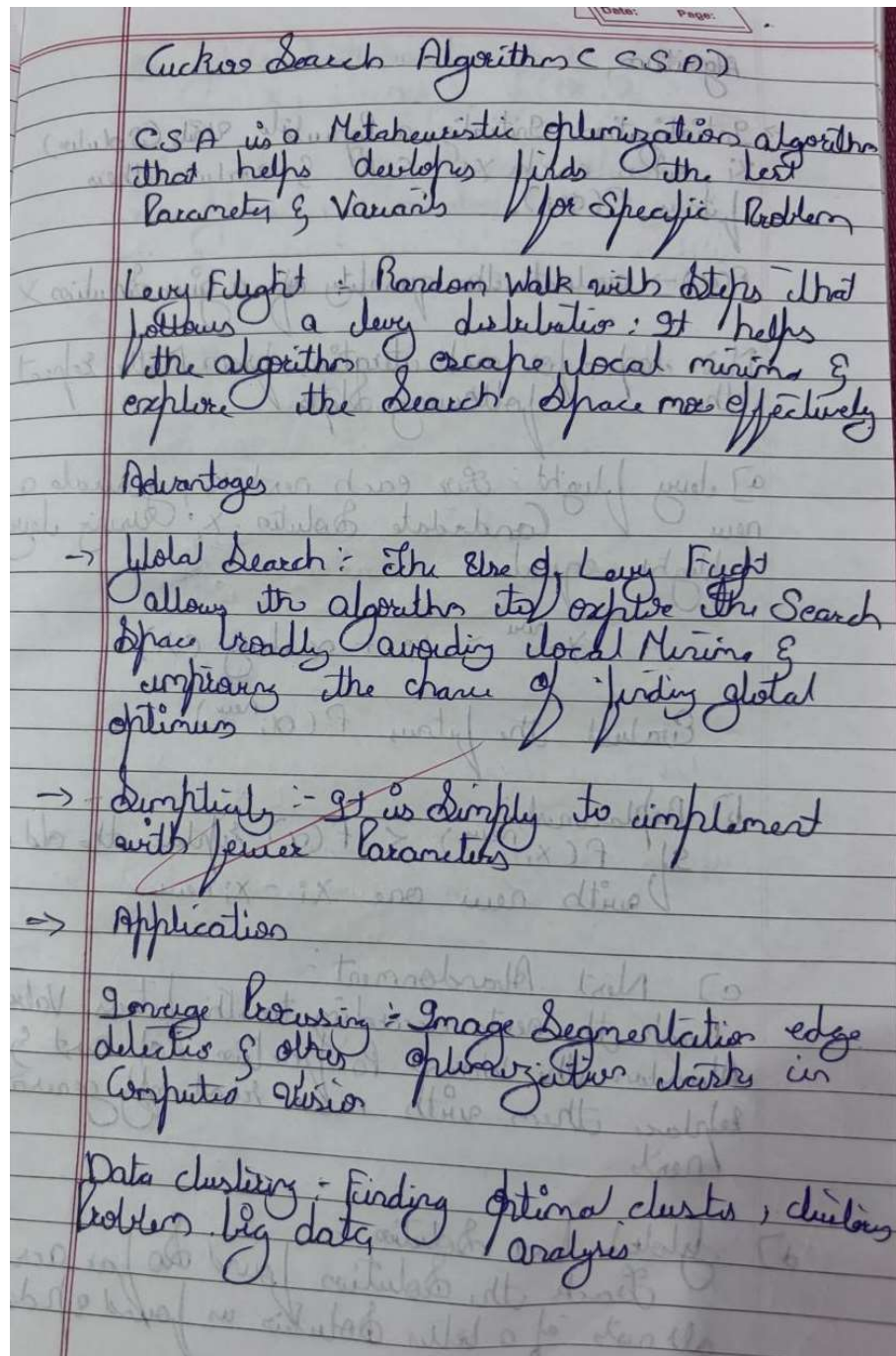
Global Best Position:  [2.59992843 2.79914636]
Best Fitness Value:    3.6691186243893878e-06
Average Particle Best Fitness Value:  0.0007223322365523365
Number of Generations: 45

```

Program 4

Cuckoo Search Algorithm

Algorithm:



Algorithm.

→ Initialization: Initialize a population of n solutions x_i , where each $x_i \in R^D$ & evaluate their fitness $f(x_i)$.

$f(x) \rightarrow$ evaluates the quality of a given solution x

Main loop: for each iteration from 1 to $MaxIter$ repeat the following steps

a) Levy flight: For each nest x_i , generate a new candidate solution x_i^{new} using Levy flight equation

$$x_i^{new} = x_i + \alpha \text{Levy}(x)$$

Evaluate the fitness $f(x_i^{new})$.

b) Replacement:

if $f(x_i^{new}) < f(x_i)$ replace the old nest with new one $x_i = x_i^{new}$.

c) Nest Abandonment:

Rank the nests according to their fitness value. Abandon the worst p_n fraction of nest & replace them with new randomly generated nests.

d) Global best solution:

Track the solution found so far across all nests. If a better solution is found update

the global best solution
 $x_{best} = \arg \min f(x_i)$

Termination: After Max iterations elapse
 the global best solution x_{best}

13/11

output

Best solution $E = 0.07413483 \quad 0.16305051$
 $-9.87130585 \quad -1.84049331 \quad 0.09155671$

Best Value (Rastrigin's Function): 47.52852531
 333939

Code:

```
import numpy as np
import matplotlib.pyplot as plt

# Objective function: Rastrigin Function
def rastrigin(x):
    A = 10
    return A * len(x) + sum(xi**2 - A * np.cos(2 * np.pi * xi) for xi in x)

# Lévy flight function for generating random steps
def levy_flight(beta=1.5, dim=2):
    sigma_u = np.power(np.math.gamma(1 + beta) * np.sin(np.pi * beta / 2) / np.math.gamma((1 + beta) / 2) / np.power(2, (beta - 1) / 2), 1 / beta)
    sigma_v = 1
    u = np.random.normal(0, sigma_u, dim)
    v = np.random.normal(0, sigma_v, dim)
    return u / np.power(np.abs(v), 1 / beta)

# Cuckoo Search Algorithm
class CuckooSearch:
    def __init__(self, func, dim, population_size, max_generations, pa=0.25, beta=1.5, lower_bound=-5, upper_bound=5):
        self.func = func          # Objective function
        self.dim = dim            # Dimension of the problem
        self.population_size = population_size # Number of nests (solutions)
        self.max_generations = max_generations # Maximum number of generations
        self.pa = pa              # Probability of alien eggs (nest replacement)
        self.beta = beta          # Lévy flight exponent
        self.lower_bound = lower_bound # Lower bound of the search space
        self.upper_bound = upper_bound # Upper bound of the search space

        # Initialize population (nests)
        self.nests = np.random.uniform(self.lower_bound, self.upper_bound, (self.population_size, self.dim))
        self.fitness = np.array([self.func(nest) for nest in self.nests]) # Fitness of each nest
        self.best_nest = self.nests[np.argmin(self.fitness)] # Best solution found
        self.best_fitness = np.min(self.fitness) # Best fitness value

    # Update nests using Lévy flights and objective function evaluations
    def generate_new_nests(self):
        new_nests = []
```



```

for i in range(self.population_size):
    step = levy_flight(self.beta, self.dim)
    new_nest = self.nests[i] + step
    # Apply boundary check
    new_nest = np.clip(new_nest, self.lower_bound, self.upper_bound)
    new_nests.append(new_nest)
return np.array(new_nests)

# Main cuckoo search algorithm
def search(self):
    history = [] # To record the best fitness values over generations

    for generation in range(self.max_generations):
        # Generate new nests based on Lévy flight
        new_nests = self.generate_new_nests()
        new_fitness = np.array([self.func(nest) for nest in new_nests])

        # Replace nests with new ones if they are better
        for i in range(self.population_size):
            if new_fitness[i] < self.fitness[i] or np.random.rand() < self.pa:
                self.nests[i] = new_nests[i]
                self.fitness[i] = new_fitness[i]

        # Find the best nest in the current population
        current_best_fitness = np.min(self.fitness)
        current_best_nest = self.nests[np.argmin(self.fitness)]

        # Update the global best solution
        if current_best_fitness < self.best_fitness:
            self.best_fitness = current_best_fitness
            self.best_nest = current_best_nest

        # Record the best fitness for the current generation
        history.append(self.best_fitness)
        print(f'Generation {generation+1}: Best fitness = {self.best_fitness}')

    return self.best_nest, self.best_fitness, history

# Analyze the Cuckoo Search Algorithm
def analyze_cuckoo_search():
    # Set up parameters for Cuckoo Search
    dim = 2

```

```
population_size = 50
max_generations = 100
cuckoo_search = CuckooSearch(func=rastrigin, dim=dim, population_size=population_size,
max_generations=max_generations)

# Run the Cuckoo Search algorithm
best_nest, best_fitness, history = cuckoo_search.search()

# Plot the convergence curve
plt.plot(history)
plt.title("Convergence Curve of Cuckoo Search Algorithm")
plt.xlabel("Generation")
plt.ylabel("Best Fitness")
plt.show()

print(f"Best solution found: {best_nest}")
print(f"Best fitness: {best_fitness}")

# Run the analysis
analyze_cuckoo_search()
```

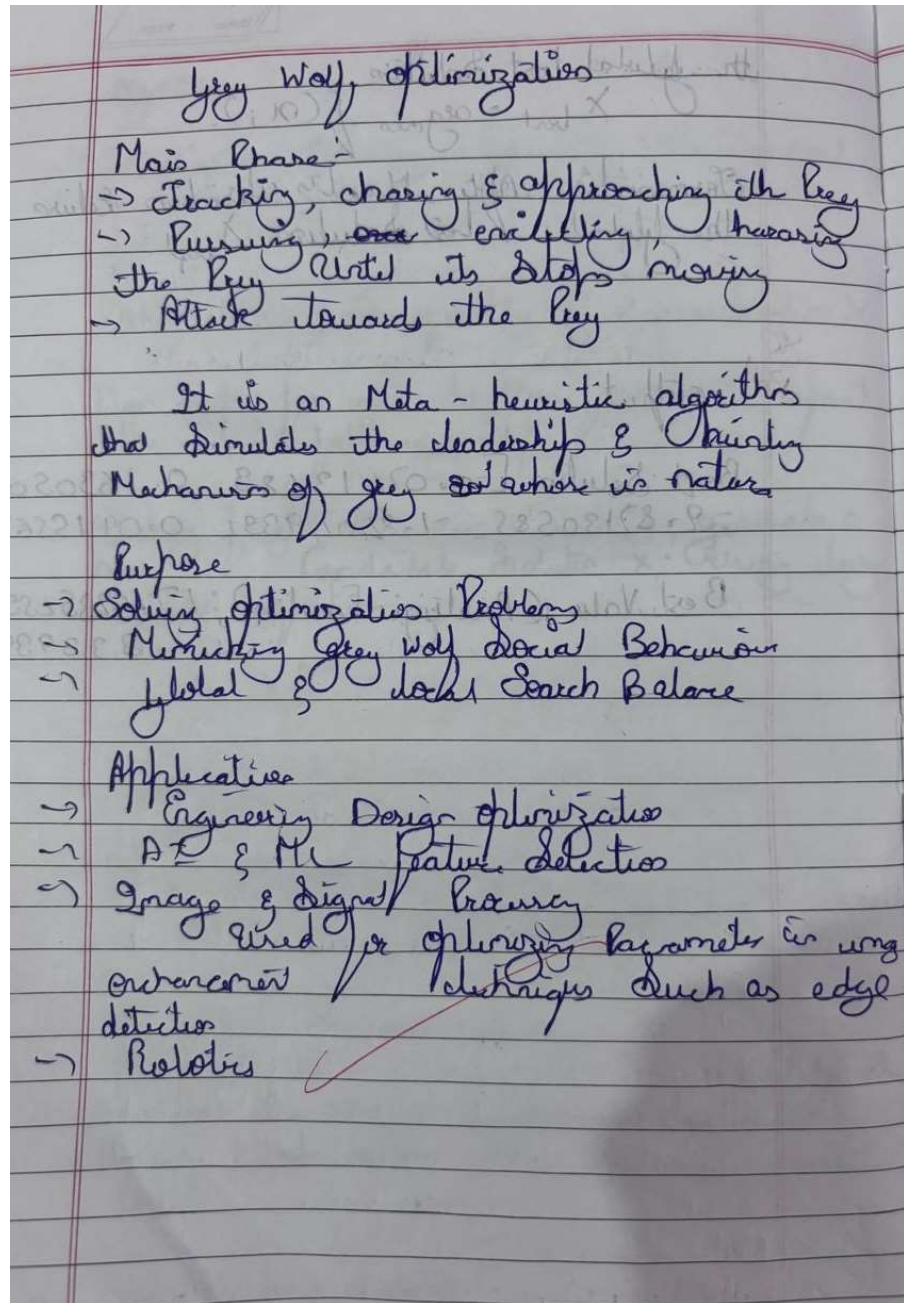
Output:

```
Best solution found: [1.30548027 2.02026344]
Best fitness: 0.16306139523513963
```

Program 5

Grey Wolf Optimizer

Algorithm:



Algorithm

1] Initialize Parameters

- Randomly initialize the position in the search space
- X_i represent the position of the i^{th} wolf
- Initialize parameters

$$a = 2 \text{ (decreases overtime)}$$

$$A = 2a \cdot r_1 \text{ \& } C = 2 \cdot r_2$$

where r_1 & r_2 are random vectors

Evaluate Fitness

- ⇒ Evaluate the fitness of each wolf using the objective function $f(x_i)$
- ⇒ Identifying the best three wolves

$X_\alpha \rightarrow$ best fitness

$X_\beta \rightarrow$ second best

$X_\gamma \rightarrow$ third best

- 3 Main Loop (For each iteration t from 1 to T)
update the coefficient a based on the iteration

$$a = 2 \times (1 - \frac{t}{T})$$

If control the exploration & exploitation balance
 t -increases a -decreases

update position of wolves for each wolf;
Calculate the new position using position
of α , β , & γ

⇒ Calculate distance b/w the each wolf & each wolf of leaders

$$D_1 = |C_1 \cdot X_1(t) - X_i(t)|,$$

$$D_2 = |C_2 \cdot X_2(t) - X_i(t)|,$$

$$D_3 = |C_3 \cdot X_3(t) - X_i(t)|,$$

update the position of each wolf

$$X_1(t+1) = X_1(t) - A_1 \cdot D_1,$$

$$X_2(t+1) = X_2(t) - A_2 \cdot D_2,$$

$$X_3(t+1) = X_3(t) - A_3 \cdot D_3$$

The new position wolf is the average of the updated position

$$X_i(t+1) = \frac{X_1(t+1) + X_2(t+1) + X_3(t+1)}{3}$$

⇒ update the fitness of all wolves

⇒ update the leader (X_1, X_2, X_3) based on the new fitness values

2. Termination Condition

⇒ If the stopping criteria are stop the algorithm

3. Return Best Solution

The final solution is the position of 1 wolf X_1 , as it represent the best solution found by the algorithm.

subject

Optimal Solution: $[1.33185437e-11, 1.78705732e-11, 9.88388617e-12, 8.8134495e-12]$

Optimal Value: $1.7709399328127607e-11$

20.11

Code:

```
import numpy as np

def objective_function(x):
    return np.sum(x**2)

class GreyWolfOptimizer:
    def __init__(self, objective_function, n_wolves, n_variables, max_iter, lb, ub):
        self.obj_func = objective_function # Objective function
        self.n_wolves = n_wolves # Number of wolves
        self.n_variables = n_variables # Number of variables in the problem
        self.max_iter = max_iter # Maximum number of iterations
        self.lb = lb # Lower bound for the search space
        self.ub = ub # Upper bound for the search space

        self.wolves = np.random.uniform(self.lb, self.ub, (self.n_wolves, self.n_variables))

        self.alpha = np.zeros(self.n_variables)
        self.beta = np.zeros(self.n_variables)
        self.delta = np.zeros(self.n_variables)
        self.alpha_score = float("inf")
        self.beta_score = float("inf")
        self.delta_score = float("inf")

    def update_wolves(self):
        fitness = np.apply_along_axis(self.obj_func, 1, self.wolves)

        sorted_indices = np.argsort(fitness)
        self.wolves = self.wolves[sorted_indices]
        fitness = fitness[sorted_indices]

        # Update alpha, beta, and delta wolves
        self.alpha = self.wolves[0]
        self.beta = self.wolves[1]
        self.delta = self.wolves[2]
        self.alpha_score = fitness[0]
        self.beta_score = fitness[1]
        self.delta_score = fitness[2]

    def optimize(self):
        for t in range(self.max_iter):
```

```

        A = 2 * np.random.random((self.n_wolves, self.n_variables)) - 1 # Random values for
exploration
        C = 2 * np.random.random((self.n_wolves, self.n_variables)) # Random values for
exploitation
        for i in range(self.n_wolves):
            D_alpha = np.abs(C[i] * self.alpha - self.wolves[i]) # Distance to alpha wolf
            D_beta = np.abs(C[i] * self.beta - self.wolves[i]) # Distance to beta wolf
            D_delta = np.abs(C[i] * self.delta - self.wolves[i]) # Distance to delta wolf

            self.wolves[i] = self.alpha - A[i] * D_alpha

            self.wolves[i] = np.clip(self.wolves[i], self.lb, self.ub)

        self.update_wolves()

        print(f'Iteration {t+1}/{self.max_iter}, Best Score: {self.alpha_score}')

    return self.alpha, self.alpha_score # Return the best solution found

n_wolves = 30 # Number of wolves
n_variables = 5 # Number of decision variables
max_iter = 100 # Maximum number of iterations
lb = -10 # Lower bound of the search space
ub = 10 # Upper bound of the search space

gwo = GreyWolfOptimizer(objective_function, n_wolves, n_variables, max_iter, lb, ub)
best_solution, best_score = gwo.optimize()
print("Best Solution Found:", best_solution)
print("Best Score:", best_score)

```

Output:

```

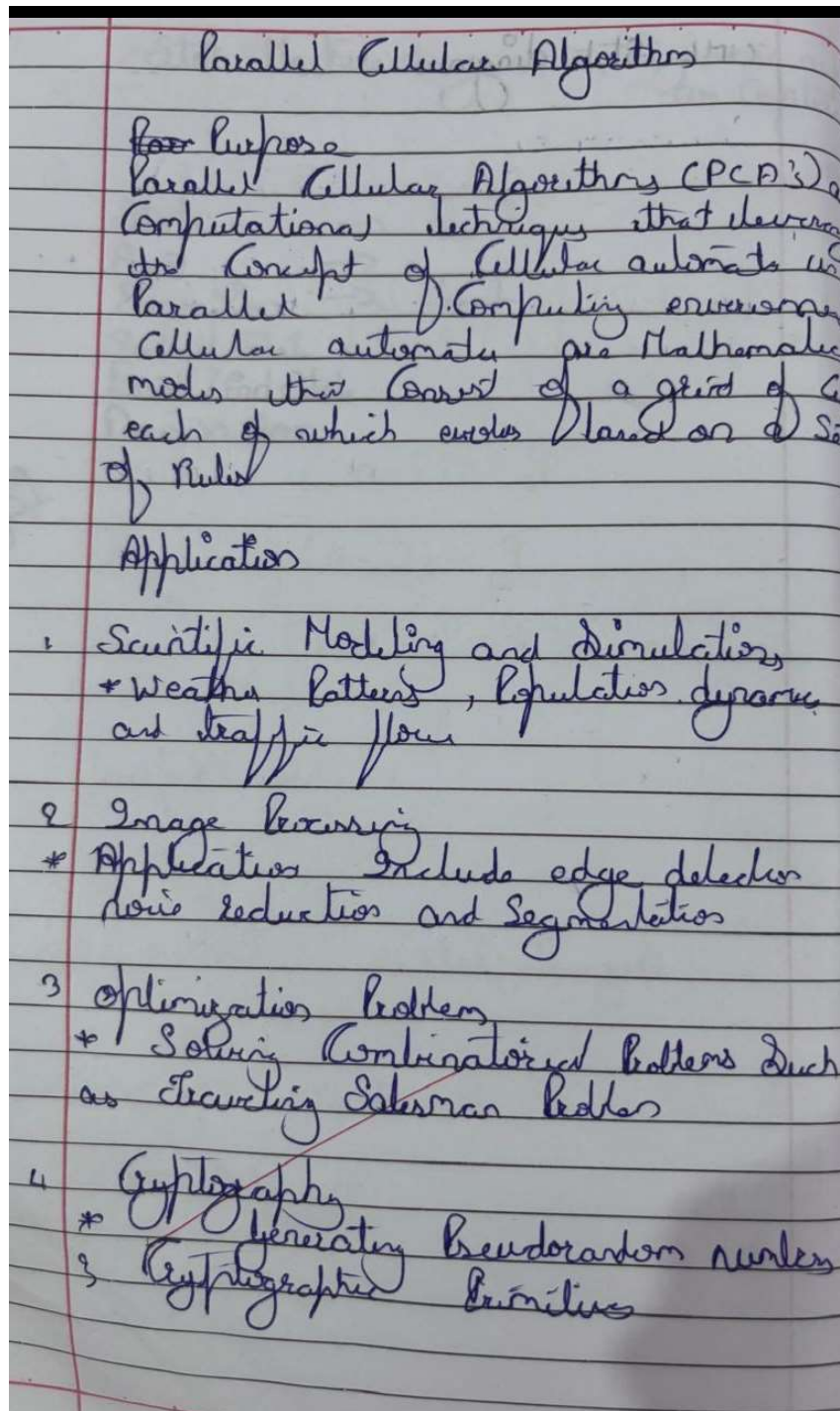
Iteration 100/100, Best Score: 1.985808550535119e-30
Best Solution Found: [-4.38373504e-17 -4.54363691e-16 -1.31663573e-15 -2.05502414e-16
 4.09828696e-17]
Best Score: 1.985808550535119e-30

```


Program 6

Parallel Cellular Algorithm

Algorithm:



Algorithm

1. Initialization

* Define a 2D grid $G(t)$ of size $M \times N$ where

$G_{ij}(t) \in \{0, 1\}$, $1 \leq i \leq M$, $1 \leq j \leq N$
represents the state of the cell (i, j) at time t .

2. Neighborhood

Define the neighborhood $N_{ij}(t)$ of cell $G_{ij}(t)$ as

$$N_{ij}(t) = \{G_{i+a, j+b}(t) \mid 0, b \in \{-1, 0, 1\} \\ \{a, b\} \neq (0, 0)\}$$

3. State update Rule

* Compute the sum of direct neighbors $S_{ij}(t)$:

$$S_{ij}(t) = \sum_{(a, b) \in \{-1, 0, 1\}, (a, b) \neq (0, 0)} G_{i+a, j+b}(t)$$

update the state of the cell $G_{ij}(t+1)$

4. Parallelization

* Divide the grid into sub-grid for parallel processing

* Each Process computes the updated state $G_{ij}(t+1)$

5. Synchronization

Exchange boundary data between sub-problems after each iteration to maintain consistency of neighbouring states

6. Termination

Repeat steps 3-5 for a fixed number of iterations T , or stop when $G(t+1) = G(t)$, indicating a steady state

Output

1	0	0	1	0	0
1	0	0	0	0	0
1	0	0	0	0	1
1	0	0	0	0	0
1	0	1	0	0	0

27.11

Code:

```
import numpy as np
from multiprocessing import Pool
def update_cell(cell_index, grid, size):
    x, y = cell_index
    neighbors = [
        ((x-1) % size, y), ((x+1) % size, y),
        (x, (y-1) % size), (x, (y+1) % size)
    ]
    new_state = sum(grid[n[0], n[1]] for n in neighbors) % 2 # example: majority rule
    return (x, y, new_state)
def parallel_update(grid, size, num_iterations):
    pool = Pool(processes=4)
    for iteration in range(num_iterations):
        print(f'Iteration {iteration + 1}:')
        indices = [(x, y) for x in range(size) for y in range(size)]
        result = pool.starmap(update_cell, [(i, grid, size) for i in indices])

        for x, y, new_state in result:
            grid[x, y] = new_state
        print(grid)
    return grid
grid_size = 10
grid = np.random.randint(2, size=(grid_size, grid_size))
print("Initial state:")
print(grid)
num_iterations = 2
updated_grid = parallel_update(grid, grid_size, num_iterations)
```

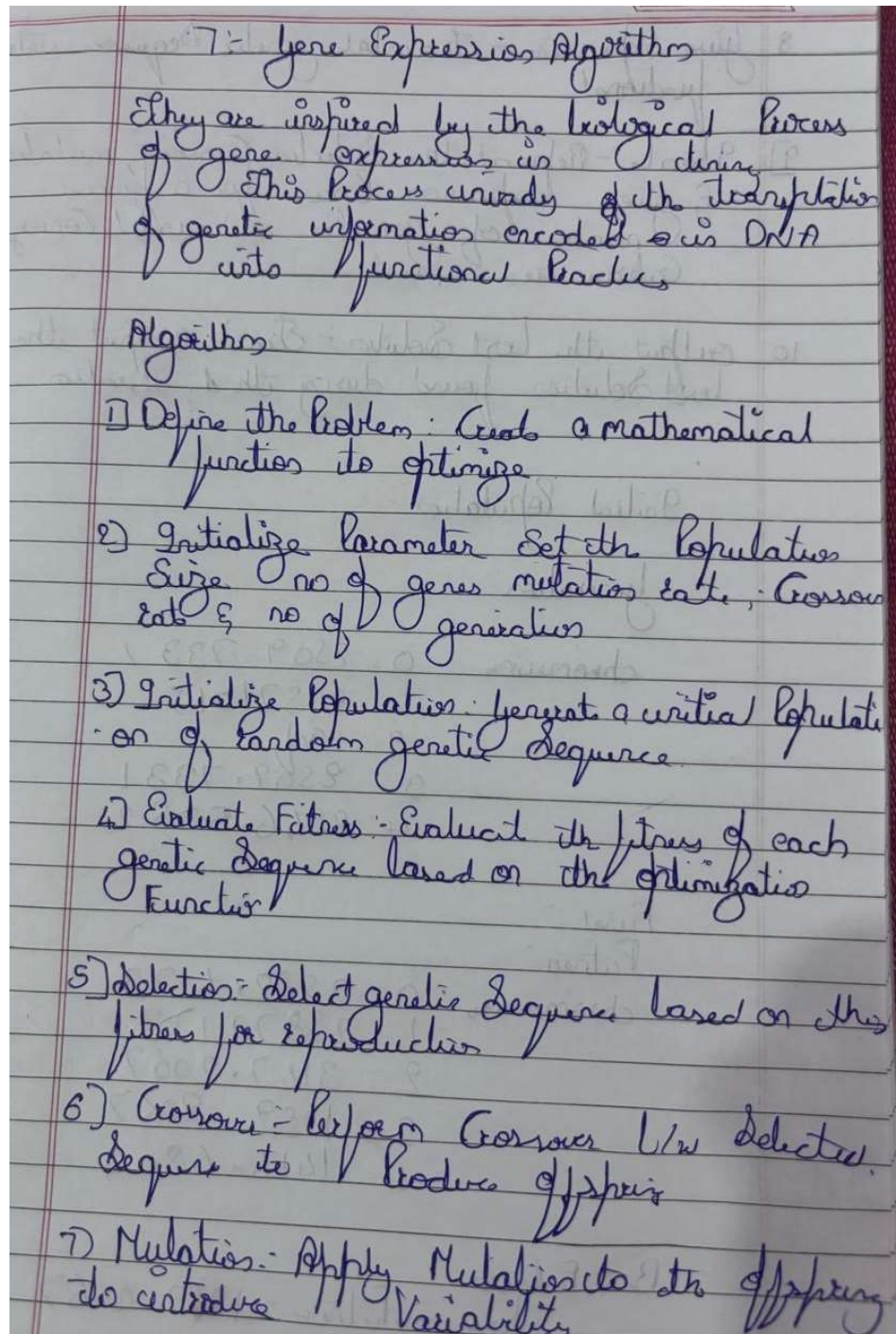
Output:

```
Iteration 1:
[[1 0 0 1]
 [1 0 1 0]
 [1 0 0 1]
 [0 1 0 1]]
Iteration 2:
[[0 0 0 0]
 [0 0 0 0]
 [0 0 0 0]
 [0 0 0 0]]
```


Program 7

Gene Expression Algorithm

Algorithm:



- 8 Give Expression - Translate genetic sequence into functional
- 9 Iterate - Repeat the Selection, Crossover, mutation & give expression fitness for a fixed number of generations until convergence criteria are met
- 10 Output the best Solution - Track & output the best solution found during the iteration

Initial Population:-

Generation:-

chromosomes : 0: 2509.7331
 1: 2657.1015
 2: 91
 3: 2569.7331
 4: 2546.5752

Final:-

Fitness:-

chromosomes : 0: 2582.4173
 1: 2587.1173
 2: 3147.2067
 3: 1959.2067
 4: 1416.6804

Best Fitness:-

chromosome fitness = 1959.2067

Code:

```
import random
import numpy as np
import operator

# Function set and terminal set
FUNCTIONS = {'+': operator.add, '-': operator.sub, '*': operator.mul, '/': operator.truediv}
TERMINALS = ['x', 1, 2, 3, 4] # x and constants

def random_gene(length=10):
    """Generate a random chromosome (gene)."""
    return [random.choice(list(FUNCTIONS.keys()) + TERMINALS) for _ in range(length)]

def decode_chromosome(chromosome, x):
    """Decode chromosome into a functional expression tree (phenotype)."""
    stack = []
    for gene in chromosome:
        if gene in FUNCTIONS: # If it's a function, pop arguments and apply
            if len(stack) < 2: # Avoid errors if stack has fewer than 2 elements
                stack.append(0)
                continue
            b = stack.pop()
            a = stack.pop()
            try:
                result = FUNCTIONS[gene](a, b)
            except ZeroDivisionError:
                result = 1 # Avoid division by zero
            stack.append(result)
        elif gene == 'x':
            stack.append(x)
        else:
            stack.append(gene)
    return stack[0] if stack else 0 # Return top of stack as output

def fitness_function(chromosome, target_function, x_values):
    """Calculate fitness based on Mean Squared Error."""
    predictions = [decode_chromosome(chromosome, x) for x in x_values]
    targets = [target_function(x) for x in x_values]
    mse = np.mean([(p - t) ** 2 for p, t in zip(predictions, targets)])
```

```
return mse
```

```
def selection(population, fitnesses):  
    """Select individuals based on fitness (roulette wheel selection)."""  
    total_fitness = sum(1 / (f + 1e-6) for f in fitnesses) # Avoid division by zero  
    probabilities = [(1 / (f + 1e-6)) / total_fitness for f in fitnesses]  
    return population[np.random.choice(len(population), p=probabilities)]  
  
def mutate(chromosome, mutation_rate=0.1):  
    """Apply mutation to a chromosome."""  
    new_chromosome = chromosome[:]  
    for i in range(len(new_chromosome)):  
        if random.random() < mutation_rate:  
            new_chromosome[i] = random.choice(list(FUNCTIONS.keys()) + TERMINALS)  
    return new_chromosome
```

```
def crossover(parent1, parent2):  
    """Perform one-point crossover between two parents."""  
    point = random.randint(1, len(parent1) - 1)  
    child1 = parent1[:point] + parent2[point:]  
    child2 = parent2[:point] + parent1[point:]  
    return child1, child2
```

```
def gene_expression_algorithm(target_function, x_values, population_size=10, generations=20):  
    """Main Gene Expression Algorithm."""  
    # Initialize random population  
    population = [random_gene() for _ in range(population_size)]  
  
    print("Initial Population:")  
    for i, chrom in enumerate(population):  
        print(f'Chromosome {i}: {chrom}')  
  
    for generation in range(generations):  
        print(f'\nGeneration {generation + 1}:')  
        # Calculate fitness for each individual  
        fitnesses = [fitness_function(chrom, target_function, x_values) for chrom in population]  
        for i, (chrom, fit) in enumerate(zip(population, fitnesses)):  
            print(f'Chromosome {i}: {chrom}, Fitness: {fit:.4f}')
```



```

# Select the next generation
new_population = []
for _ in range(population_size // 2):
    parent1 = selection(population, fitnesses)
    parent2 = selection(population, fitnesses)
    child1, child2 = crossover(parent1, parent2)
    child1 = mutate(child1)
    child2 = mutate(child2)
    new_population.extend([child1, child2])
population = new_population

# Final results
print("\nFinal Population and Fitness:")
fitnesses = [fitness_function(chrom, target_function, x_values) for chrom in population]
for i, (chrom, fit) in enumerate(zip(population, fitnesses)):
    print(f'Chromosome {i}: {chrom}, Fitness: {fit:.4f}')

best_index = np.argmin(fitnesses)
print("\nBest Solution:")
print(f'Chromosome: {population[best_index]}, Fitness: {fitnesses[best_index]:.4f}')

# Target function for regression
def target_function(x):
    return x**2 + 2*x + 1 # Example:  $f(x) = x^2 + 2x + 1$ 

# Input values
x_values = np.linspace(-10, 10, 20)

# Run the algorithm
gene_expression_algorithm(target_function, x_values, population_size=10, generations=10)

```

Output:

```

Best Solution:
Chromosome: [1, 3, '+', 2, 1, 4, '*', '*', '*', 3], Fitness: 1259.2067
<ipython-input-3-6df17022c257>:25: RuntimeWarning: divide by zero encountered in scalar divide
result = FUNCTIONS[gene](a, b)

```