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┌────────────────────────── MODULE hmac ───────────────────────────┐
EXTENDS Integers, Sequences, FiniteSets, TLC

VARIABLES message, key, sentHash, processedHash, equalityCheck, A, B, C, D, AA, BB, CC, DD, M, K

Prime  $\triangleq \{x \in 2 \dots 12 : \forall y \in 2 \dots (x-1) : x \% y \neq 0\}$ 

BLOCK_SIZE  $\triangleq 64$ 

GenK(n)  $\triangleq [i \in 0 \dots (n-1) \mapsto (i * 123456789) \% 987654321]$ 
GenS(n)  $\triangleq [i \in 0 \dots (n-1) \mapsto (i \% 4) * 5 + 7]$ 

LeftRotate(x, c)  $\triangleq ((x * (2^c)) \% (2^{32})) + ((x \div (2^{(32-c)})) \% (2^{32}))$ 

MD5(m)  $\triangleq$ 
  LET
    ProcessChunk(chunk)  $\triangleq$ 
      LET P  $\triangleq [j \in 0 \dots 15 \mapsto \text{SubSeq}(m, (chunk-1) * 512 + j * 32 + 1, (chunk-1) * 512 + (j +$ 
      IN
         $\wedge AA' = A$ 
         $\wedge BB' = B$ 
         $\wedge CC' = C$ 
         $\wedge DD' = D$ 
         $\wedge \forall i \in 0 \dots 63 :$ 
          LET
            F  $\triangleq$  IF i  $\in 0 \dots 15$  THEN (B  $\wedge$  C)  $\vee$  ( $\neg B$ )  $\wedge$  D)
              ELSE IF i  $\in 16 \dots 31$  THEN (D  $\wedge$  B)  $\vee$  ( $\neg D$ )  $\wedge$  C)
              ELSE IF i  $\in 32 \dots 47$  THEN  $((B^C)^D)$ 
              ELSE C(B  $\vee$  ( $\neg D$ ))
            g  $\triangleq$  IF i  $\in 0 \dots 15$  THEN i
              ELSE IF i  $\in 16 \dots 31$  THEN (5 * i + 1) % 16
              ELSE IF i  $\in 32 \dots 47$  THEN (3 * i + 5) % 16
              ELSE (7 * i) % 16
          IN
             $\wedge F' = F + A + K[i] + P[g]$ 
             $\wedge A' = D$ 
             $\wedge D' = C$ 
             $\wedge C' = B$ 
             $\wedge B' = B + \text{LeftRotate}(F', S[i])$ 
         $\wedge A' = A + AA$ 
         $\wedge B' = B + BB$ 
         $\wedge C' = C + CC$ 
         $\wedge D' = D + DD$ 
    digest  $\triangleq \langle A, B, C, D \rangle$ 
  IN
    digest

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$$\begin{aligned}
ExtendedKey &\triangleq \text{IF } Len(key) > BLOCK_SIZE \text{ THEN } MD5(key) \text{ ELSE } Append(key, \langle 0 \rangle^{(BLOCK_SIZE - Len(key))}) \\
ipad &\triangleq [i \in 1 \dots Len(ExtendedKey) \mapsto ExtendedKey[i]^{54}] \\
opad &\triangleq [i \in 1 \dots Len(ExtendedKey) \mapsto ExtendedKey[i]^{92}] \\
HashFunction(m, k) &\triangleq \\
&\quad \text{LET} \\
&\quad \quad innerHash \triangleq MD5(ipad \circ m) \\
&\quad \quad resultHash \triangleq MD5(opad \circ innerHash) \\
&\quad \text{IN} \\
&\quad \quad resultHash \\
SendHash &\triangleq \\
&\quad \wedge sentHash' = HashFunction(message, ExtendedKey) \\
&\quad \wedge \text{UNCHANGED } \langle message, key, processedHash, equalityCheck, A, B, C, D, AA, BB, CC, DD, K, S, M \rangle \\
ProcessHash &\triangleq \\
&\quad \wedge processedHash' = HashFunction(message, ExtendedKey) \\
&\quad \wedge \text{UNCHANGED } \langle message, key, sentHash, equalityCheck, A, B, C, D, AA, BB, CC, DD, K, S, M \rangle \\
CompareHashes &\triangleq \\
&\quad \wedge equalityCheck' = (sentHash = processedHash) \\
&\quad \wedge \text{UNCHANGED } \langle message, key, sentHash, processedHash, A, B, C, D, AA, BB, CC, DD, K, S, M \rangle \\
Init &\triangleq \\
&\quad \wedge message = GenS(18) \\
&\quad \wedge key = GenK(18) \\
&\quad \wedge sentHash = \langle \rangle \\
&\quad \wedge processedHash = \langle \rangle \\
&\quad \wedge equalityCheck = \text{FALSE} \\
&\quad \wedge A \in Prime \\
&\quad \wedge B \in Prime \\
&\quad \wedge C \in Prime \\
&\quad \wedge D \in Prime \\
&\quad \wedge K = GenK(18) \\
&\quad \wedge S = GenS(18) \\
&\quad \wedge AA = A \\
&\quad \wedge BB = B \\
&\quad \wedge CC = C \\
&\quad \wedge DD = D \\
&\quad \wedge M = \langle \rangle \\
Next &\triangleq \\
&\quad \vee SendHash \\
&\quad \vee ProcessHash \\
&\quad \vee CompareHashes
\end{aligned}$$

$$Spec \stackrel{\Delta}{=} Init \wedge \square [Next]_{\langle message, key, sentHash, processedHash, equalityCheck, A, B, C, D, AA, BB, CC, DD, M, K, S \rangle}$$
