EXTENDS Naturals, Sequences, Integers

Variables state, roundKey, round, Nr, encrypt

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 \begin{array}{rl} IP & \triangleq \ \langle 58,\, 50,\, 42,\, 34,\, 26,\, 18,\, 10,\, 2,\\ & 60,\, 52,\, 44,\, 36,\, 28,\, 20,\, 12,\, 4,\\ & 62,\, 54,\, 46,\, 38,\, 30,\, 22,\, 14,\, 6,\\ & 64,\, 56,\, 48,\, 40,\, 32,\, 24,\, 16,\, 8,\\ & 57,\, 49,\, 41,\, 33,\, 25,\, 17,\, 9,\, 1,\\ & 59,\, 51,\, 43,\, 35,\, 27,\, 19,\, 11,\, 3,\\ & 61,\, 53,\, 45,\, 37,\, 29,\, 21,\, 13,\, 5,\\ & 63,\, 55,\, 47,\, 39,\, 31,\, 23,\, 15,\, 7 \rangle \end{array}
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 $FP \triangleq \langle 40, 8, 48, 16, 56, 24, 64, 32, \\ 39, 7, 47, 15, 55, 23, 63, 31, \\ 38, 6, 46, 14, 54, 22, 62, 30, \\ 37, 5, 45, 13, 53, 21, 61, 29, \\ 36, 4, 44, 12, 52, 20, 60, 28, \\ 35, 3, 43, 11, 51, 19, 59, 27, \\ 34, 2, 42, 10, 50, 18, 58, 26, \\ 33, 1, 41, 9, 49, 17, 57, 25 \rangle$

 $E \triangleq \langle 32, 1, 2, 3, 4, 5, \\ 4, 5, 6, 7, 8, 9, \\ 8, 9, 10, 11, 12, 13, \\ 12, 13, 14, 15, 16, 17, \\ 16, 17, 18, 19, 20, 21, \\ 20, 21, 22, 23, 24, 25, \\ 24, 25, 26, 27, 28, 29, \\ 28, 29, 30, 31, 32, 1 \rangle$

 $P \triangleq \langle 16, 7, 20, 21, 29, 12, 28, 17, 1, 15, 23, 26, 5, 18, 31, 10, 2, 8, 24, 14, 32, 27, 3, 9, 19, 13, 30, 6, 22, 11, 4, 25 \rangle$

 $SBox1 \triangleq \langle \langle 14, 4, 13, 1, 2, 15, 11, 8, 3, 10, 6, 12, 5, 9, 0, 7 \rangle, \\ \langle 0, 15, 7, 4, 14, 2, 13, 1, 10, 6, 12, 11, 9, 5, 3, 8 \rangle, \\ \langle 4, 1, 14, 8, 13, 6, 2, 11, 15, 12, 9, 7, 3, 10, 5, 0 \rangle, \\ \langle 15, 12, 8, 2, 4, 9, 1, 7, 5, 11, 3, 14, 10, 0, 6, 13 \rangle \rangle$

 $SBox2 \triangleq \langle \langle 15, 1, 8, 14, 6, 11, 3, 4, 9, 7, 2, 13, 12, 0, 5, 10 \rangle, \\ \langle 3, 13, 4, 7, 15, 2, 8, 14, 12, 0, 1, 10, 6, 9, 11, 5 \rangle, \\ \langle 0, 14, 7, 11, 10, 4, 13, 1, 5, 8, 12, 6, 9, 3, 2, 15 \rangle, \\ \langle 13, 8, 10, 1, 3, 15, 4, 2, 11, 6, 7, 12, 0, 5, 14, 9 \rangle \rangle$

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SBox4 \triangleq \langle \langle 7, 13, 14, 3, 0, 6, 9, 10, 1, 2, 8, 5, 11, 12, 4, 15 \rangle,
                                                \langle 13, 8, 11, 5, 6, 15, 0, 3, 4, 7, 2, 12, 1, 10, 14, 9 \rangle
                                               \langle 10, 6, 9, 0, 12, 11, 7, 13, 15, 1, 3, 14, 5, 2, 8, 4 \rangle
                                               \langle 3, 15, 0, 6, 10, 1, 13, 8, 9, 4, 5, 11, 12, 7, 2, 14 \rangle \rangle
SBox5 \stackrel{\triangle}{=} \langle \langle 2, 12, 4, 1, 7, 10, 11, 6, 8, 5, 3, 15, 13, 0, 14, 9 \rangle,
                                                \langle 14, 11, 2, 12, 4, 7, 13, 1, 5, 0, 15, 10, 3, 9, 8, 6 \rangle
                                               \langle 4, 2, 1, 11, 10, 13, 7, 8, 15, 9, 12, 5, 6, 3, 0, 14 \rangle
                                               \langle 11, 8, 12, 7, 1, 14, 2, 13, 6, 15, 0, 9, 10, 4, 5, 3 \rangle \rangle
SBox6 \stackrel{\triangle}{=} \langle \langle 12, 1, 10, 15, 9, 2, 6, 8, 0, 13, 3, 4, 14, 7, 5, 11 \rangle,
                                                \langle 10, 15, 4, 2, 7, 12, 9, 5, 6, 1, 13, 14, 0, 11, 3, 8 \rangle
                                               \langle 9, 14, 15, 5, 2, 8, 12, 3, 7, 0, 4, 10, 1, 13, 11, 6 \rangle
                                               \langle 4, 3, 2, 12, 9, 5, 15, 10, 11, 14, 1, 7, 6, 0, 8, 13 \rangle \rangle
SBox7 \stackrel{\triangle}{=} \langle \langle 4, 11, 2, 14, 15, 0, 8, 13, 3, 12, 9, 7, 5, 10, 6, 1 \rangle,
                                                \langle 13, 0, 11, 7, 4, 9, 1, 10, 14, 3, 5, 12, 2, 15, 8, 6 \rangle
                                               \langle 1, 4, 11, 13, 12, 3, 7, 14, 10, 15, 6, 8, 0, 5, 9, 2 \rangle
                                               \langle 6, 11, 13, 8, 1, 4, 10, 7, 9, 5, 0, 15, 14, 2, 3, 12 \rangle \rangle
SBox8 \triangleq \langle \langle 13, 2, 8, 4, 6, 15, 11, 1, 10, 9, 3, 14, 5, 0, 12, 7 \rangle,
                                                \langle 1, 15, 13, 8, 10, 3, 7, 4, 12, 5, 6, 11, 0, 14, 9, 2 \rangle
                                               \langle 7, 11, 4, 1, 9, 12, 14, 2, 0, 6, 10, 13, 15, 3, 5, 8 \rangle
                                               \langle 2, 1, 14, 7, 4, 10, 8, 13, 15, 12, 9, 0, 3, 5, 6, 11 \rangle \rangle
Permute(bitSeq, perm) \stackrel{\Delta}{=}
              [i \in 1 .. Len(perm) \mapsto bitSeq[perm[i]]]
GenerateRoundKey(k, r) \triangleq
              [i \in 1 ... Len(k) \mapsto k[((i+r-1)\%Len(k))+1]]
AccessSBox(SBox, Row, Col) \triangleq
                                                   If Row \in 1...4 \land Col \in 1...16 then SBox[Row][Col] else 0
F(R, K) \triangleq
                    LET
                                  E_{-}R \stackrel{\triangle}{=} Permute(R, E)
                                  XOR\_Result \triangleq [i \in 1 ... 48 \mapsto (E\_R[i] + K[i])\%2]
                                  SBox\_Output1 \stackrel{\triangle}{=} AccessSBox(SBox1, (XOR\_Result[1]*2) + XOR\_Result[6] + 1, ((XOR\_Result[1]*2) + XOR\_Result[6] + 1)
                                  SBox\_Output2 \triangleq AccessSBox(SBox2, (XOR\_Result[7]*2) + XOR\_Result[12] + 1, ((XOR\_Result[7]*2) + XOR\_Result[7]*2) 
                                  SBox\_Output3 \triangleq AccessSBox(SBox3, (XOR\_Result[13]*2) + XOR\_Result[18] + 1, ((XOR\_Result[13]*2) + XOR\_Result[18] + 1)
                                  SBox\_Output4 \triangleq AccessSBox(SBox4, (XOR\_Result[19]*2) + XOR\_Result[24] + 1, ((XOR\_Result[24]*2) + (XOR\_Result[24]*2) + (XOR\_Result[24]*
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 $SBox3 \stackrel{\triangle}{=} \langle \langle 10, 0, 9, 14, 6, 3, 15, 5, 1, 13, 12, 7, 11, 4, 2, 8 \rangle,$

 $\langle 13, 7, 0, 9, 3, 4, 6, 10, 2, 8, 5, 14, 12, 11, 15, 1 \rangle, \langle 13, 6, 4, 9, 8, 15, 3, 0, 11, 1, 2, 12, 5, 10, 14, 7 \rangle, \langle 1, 10, 13, 0, 6, 9, 8, 7, 4, 15, 14, 3, 11, 5, 2, 12 \rangle \rangle$

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SBox\_Output5 \stackrel{\triangle}{=} AccessSBox(SBox5, (XOR\_Result[25]*2) + XOR\_Result[30] + 1, ((XOR\_Result[25]*2) + XOR\_Result[30] + 1)
                                                       SBox\_Output6 \triangleq AccessSBox(SBox6, (XOR\_Result[31]*2) + XOR\_Result[36] + 1, ((XOR\_Result[30]*2) + XOR\_Result[30]*2)
                                                        SBox\_Output7 \triangleq AccessSBox(SBox7, (XOR\_Result[37]*2) + XOR\_Result[42] + 1, ((XOR\_Result[42]*2) + (XOR\_Result[42]*2) + ((XOR\_Result[42]*2) + ((XOR\_Result[
                                                        SBox\_Output8 \triangleq AccessSBox(SBox8, (XOR\_Result[43]*2) + XOR\_Result[48] + 1, ((XOR\_Result[43]*2) + XOR\_Result[48] + 1)
                                                        ToBits4(n) \stackrel{\triangle}{=} \langle (n \div 8)\%2, (n \div 4)\%2, (n \div 2)\%2, n\%2 \rangle
                                                        P\_Input \triangleq ToBits4(SBox\_Output1) \circ ToBits4(SBox\_Output2) \circ ToBits4(SBox\_Output3) \circ ToBits4(SBox\_Outpu
                                                                                                            ToBits4(SBox\_Output5) \circ ToBits4(SBox\_Output6) \circ ToBits4(SBox\_Output7) \circ ToBits4(SBox\_Output7) \circ ToBits4(SBox\_Output8) \circ ToBi
                                                        P\_Output \triangleq Permute(P\_Input, P)
                                IN
                                                        P_-Output
 Round(L, R, K) \triangleq
                      LET newR \stackrel{\triangle}{=} [i \in 1 ... 32 \mapsto (L[i] + F(R, K)[i])\%2]
                                                    newL \triangleq R
                                                  \langle newL, newR \rangle
                      IN
 EncryptRound(L, R, K) \triangleq
                       LET result \stackrel{\triangle}{=} Round(L, R, K)IN
 DecryptRound(L, R, K) \triangleq
                       LET result \stackrel{\triangle}{=} Round(R, L, K)IN result
DESProcess(e, s, k, r) \stackrel{\Delta}{=}
                       IF e THEN EncryptRound(s[1], s[2], GenerateRoundKey(k, r))
                            ELSE DecryptRound(s[1], s[2], GenerateRoundKey(k, Nr - r + 1))
 NextRound \triangleq
                           \land round < Nr
                           \land state' = DESProcess(encrypt, state, roundKey, round)
                          \land \mathit{roundKey'} = \mathit{roundKey}
                          \wedge Nr' = Nr
                          \land round' = round + 1
                          \land encrypt' = encrypt
Init \triangleq
                          \land \, state = \langle [i \qquad \in 1 \mathinner{\ldotp\ldotp} 32 \mapsto 0], \, [i \in 1 \mathinner{\ldotp\ldotp} 32 \mapsto 1] \rangle
                          \land roundKey = [i \in 1 ... 48 \mapsto 1]
                          \wedge round = 0
                          \wedge Nr = 16
                          \land encrypt = \text{true}
Spec \triangleq
                       Init \land \Box [NextRound]_{\langle state, \, round, \, roundKey, \, Nr, \, encrypt \rangle}
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