

MODULE <i>pbkdf2</i>
EXTENDS <i>Integers, Sequences, TLC, Bitwise</i>
$  \begin{aligned}  Password &\triangleq \langle 32, 12, 45, 67, 78, 43, 21, 19 \rangle \\  Salt &\triangleq \langle 16, 12, 34, 45 \rangle \\  Iterations &\triangleq 5 \\  OutputLength &\triangleq 16 \\  BlockIndex &\triangleq \langle 4, 2, 1, 0 \rangle  \end{aligned}  $
VARIABLES $U, F, DerivedKey$
$HMAC(password, data) \triangleq data \circ Password$
$U1 \triangleq HMAC(Password, Append(Salt, BlockIndex))$
$  \begin{aligned}  ModAdd(x, y) &\triangleq ((x + y) \% (2^8)) \\  ModSub(x, y) &\triangleq ((x - y) \% (2^8)) \\  ModMul(x, y) &\triangleq ((x * y) \% (2^8))  \end{aligned}  $
$  \begin{aligned}  Init &\triangleq \\  &\wedge U = [i \in 1 \dots Iterations \mapsto \text{IF } i = 1 \text{ THEN } U1 \text{ ELSE } \langle \rangle] \\  &\wedge F = U1 \\  &\wedge DerivedKey = \langle \rangle  \end{aligned}  $
$GenNextU(i) \triangleq U[i] = HMAC(Password, U[i - 1])$
$UpdateF(i) \triangleq F' = F \hat{\wedge} U[i]$
$  \begin{aligned}  FinalizeDerivedKey &\triangleq \\  &\wedge DerivedKey' = Append(DerivedKey, F) \\  &\wedge \text{UNCHANGED } \langle U, F \rangle  \end{aligned}  $
$  \begin{aligned}  Next &\triangleq \\  &\vee \exists i \in 2 \dots Iterations : \\  &\quad \wedge GenNextU(i) \\  &\quad \wedge UpdateF(i) \\  &\quad \wedge \text{UNCHANGED } \langle DerivedKey \rangle \\  &\vee FinalizeDerivedKey  \end{aligned}  $
$  \begin{aligned}  Spec &\triangleq \\  &\wedge Init \\  &\wedge \Box [Next]_{\langle U, F, DerivedKey \rangle}  \end{aligned}  $