§3 The Stack ADT

1. ADT

A stack is a Last-In-First-Out (LIFO) list, that is, an ordered list in which insertions and deletions are made at the top only.

Objects: A finite ordered list with zero or more elements.

Operations:

- Int IsEmpty(Stack S);
- Stack CreateStack();
- DisposeStack(Stack S);
- MakeEmpty(Stack S);
- Push(ElementType X, Stack S);
- ElementType Top(Stack S);
- Pop(Stack S);



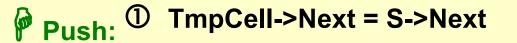


Note: A Pop (or Top) on an empty stack is an error in the stack ADT.

Push on a full stack is an implementation error but not an ADT error.

2. Implementations

Linked List Implementation (with a header node)



② S->Next = TmpCell

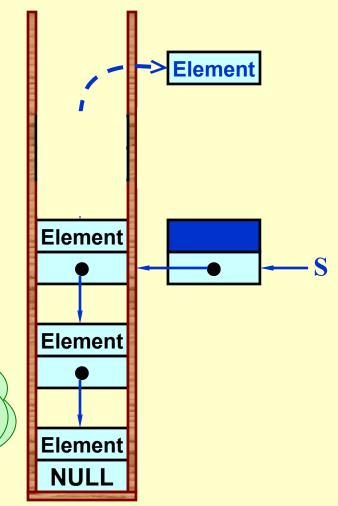
Top: return S->Next->Element

Pop: ① FirstCell = S->Next

② S->Next = S->Next->Next

③ free (FirstCell)





> Array Implementation

Note: ① The stack model must be well encapsulated. That is, no part of your code, except for the stack routines, can attempt to access the Array or TopOfStack variable. ② Error check must be done before Push or Pop (Top).

Read Figures 3.38-3.52 for detailed implementations of stack operations.

3. Applications

***** Balancing Symbols

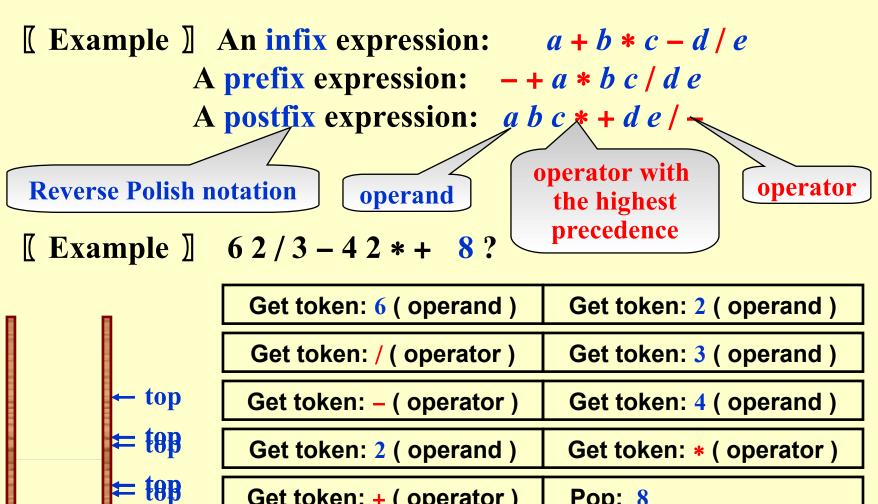


Check if parenthesis (), brackets [], and braces {} are balanced.

```
Algorithm {
  Make an empty stack S;
                                               T(N) = O(N)
  while (read in a character c) {
                                            where N is the length
    if (c is an opening symbol)
                                              of the expression.
       Push(c, S);
                                                  This is an
    else if (c is a closing symbol) {
                                              on-line algorithm.
       if (S is empty) { ERROR; exit; }
       else { /* stack is okay */
         if (Top(S) doesn't match c) { ERROR, exit; }
         else Pop(S);
       } /* end else-stack is okay */
    } /* end else-if-closing symbol */
  } /* end while-loop */
  if (S is not empty) ERROR;
```

*** Postfix Evaluation**

= top



Get token: + (operator)

T(N) = O(N). No need to know precedence rules.

Pop: 8

* Infix to Postfix Conversion

[Example]
$$a + b * c - d$$
 $a b c * + d -$

Note:

> The order of operands is the same in infix and postfix.

higher precedence appear before those lence.

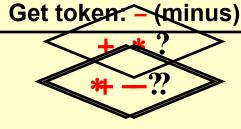
simple?



Wait till

Get token: c (operand)

Get token: d (operand)





Solutions:

- ① Never pop a (from the stack except when processing a).
- ② Observe that when (is not in the stack, its precedence is the highest; but when it is in the stack, its precedence is the lowest. Define in-stack precedence and incoming precedence for symbols, and each time use the corresponding precedence for comparison.

Note: a-b-c will be converted to ab-c. However, 2^2^3 (2^2^3) must be converted to 223^4 , not 22^3 since exponentiation associates right to left.

...e.

nents

fp

```
Recursion can always be completely removed.

Non recursive programs are generally faster than equivalent recursive programs.

However, recursive programs are in general much simpler and easier to understand.
```

```
void PrintList ( List L )
{
top: if ( L != NULL ) {
    PrintElement ( L->Element );
    L = L->next;
    goto top; /* do NOT do this */
    }
} /* compiler removes recursion */
```

§4 The Queue ADT

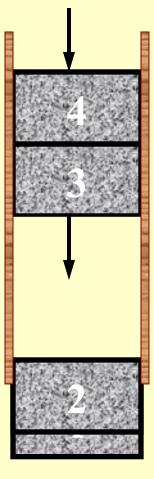
1. ADT

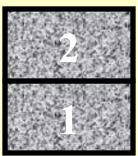
A queue is a First-In-First-Out (FIFO) list, that is, an ordered list in which insertions take place at one end and deletions take place at the opposite end.

Objects: A finite ordered list with zero or more elements.

Operations:

- int IsEmpty(Queue Q);
- **Queue CreateQueue()**;
- DisposeQueue(Queue Q);
- MakeEmpty(Queue Q);
- Enqueue(ElementType X, Queue Q);
- FlementType Front(Queue Q);
- Dequeue(Queue Q);



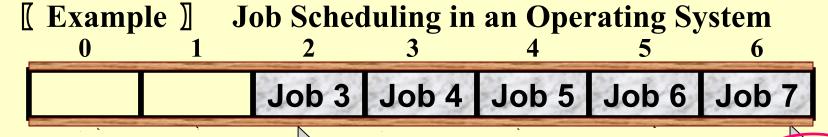


Rear

2. Array Implementation of Queues

```
(Linked list implementation is trivial)
```

```
struct QueueRecord {
    int Capacity; /* max size of queue */
    int Front; /* the front pointer */
    int Rear; /* the rear pointer */
    int Size; /* Optional - the current size of queue */
    ElementType *Array; /* array for queue elements */
};
```

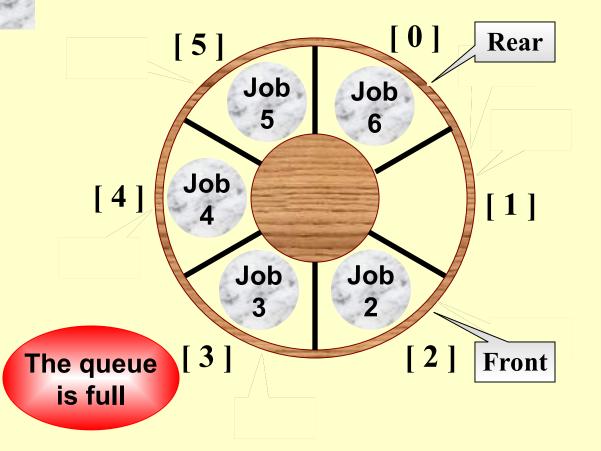


Front

Enqueue Job 1 Enqueue Job 2 Enqueue Job 3 Dequeue Job 1
Enqueue Job 4 Enqueue Job 5 Enqueue Job 6 Dequeue Job 2
Enqueue Job 7 Enqueue Job 8

Circular Queue:

Question:
Why is the queue announced full while there is still a free space left?



Note: Adding a **Size** field can avoid wasting one empty space to distinguish "full" from "empty". Do you have any other ideas?