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Assignment-1

Ansi) Asymptotic notation are material tools to represent the time complexity of algorithms for asymptotic analysis.

The main idea of asymptotic analysis is to have a measure of the efficiency of algorithms that don't depends on machines. Specific constants and doesn't require algorithm to be implemented and time taken by the program to be compared.

Following are the asymptotic notations that are mostly used:

- I O Notation: The theta notation bounds a Junction from above and below, so it defines exact asymptotic behaviour.
- 2] Big O Notation: It defines an upper bound of an algorithm, it bounds a Junction only from above
- 3] 12 Notation: 12 Notation provides an asymptotic Lower bound

For eg consider Insertion sort

It takes linear time en best case and quardatic time in worst case.

We can say that Insertion sort have $O(n^2)$ for worst case O(n) for best case I(n)

Ans 2] O(logn)

Ans 3] T(n) = 5 3T(n-1), if n > 01 otherwise

T(n) = 3T(n-1) 3(3T(n-2)) $3^{2}T(n-2)$ $3^{3}T(n-3)$ $3^{n}T(n-n)$ $= 3^{n}$

Ans 4) $T(n) = \begin{cases} 2T(n-1)-1, & i \\ 1 & n > 0 \end{cases}$ T(n) = 2T(n-1)-1 = 2(2T(n-2)-1)-1

$$= 2^{2}(T(n-2))-2-1$$

$$= 2^{2}(2T(n-3)-1)-2-1$$

$$= 2^{3}T(n-3)-2^{2}-2^{1}-20$$

$$= 2^{n}T(n-n)-2^{n-1}-2^{n-2}-2^{n-3}-2^{2}-2^{1}-2^{0}$$

$$= 2^{n} \pm -(2^{n}-1)$$

$$= 2^{n}-2^{n}+1=1$$

$$T(n)=1$$

Anss] Si= Si-1+i

: K= O(1n)

Ans 6] 0 (10)

Ans 7] j'es loop executing log n times K''' V''' V'''' log n times V''' V'''' V'''' V'''' V''' V''' V''' V''' V''' V''' V''' V'' V

Time complexity= 0 (n lg2n)

Ana] 0 (n3)

Ans
$$9/15$$
] Inner loop will execute $\left(n+\frac{n}{2}+\frac{n}{3}+-\frac{n}{n}\right)^{\frac{n}{4}}$
 $n\left(1+\frac{1}{2}+\frac{1}{3}+--\frac{1}{n}\right)$

It is equal to 0 -(nlogn)

Ans 10] · $n^{\frac{n}{4}}$ an

 $k>=1$ a>1

Taking $k=a=2$
 $n^{\frac{n}{4}}$ 2^n

We can say $n^2=0(2^k)$
 $n^{\frac{n}{4}}=0(a^n)$

Ans 11] $0(\sqrt{n})$ Same logic given in Ques 5

Ans 12] Recurrence Relation

 $T(n)=T(n-1)+T(n-2)+1$

Making Recurrence Tree

 $n-1$
 $n-2$
 $n-2$
 $n-3$
 $n-3$
 $n-4$
 $n-4$
 $n-1$
 $n-2$
 $n-3$
 $n-4$
 $n-4$
 $n-1$
 $n-2$
 $n-3$
 $n-4$
 $n-3$
 $n-4$
 $n-1$
 $n-2$
 $n-3$
 $n-4$
 $n-$

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$$\frac{1(a2^{n+1}-1)}{2^{n-1}} = 2^{n+1}-1$$

$$O(2^{n+1}) = O(2+2^n) = O(2^n)$$

Space complexity = O(n)

This is because maximum Stack frame is some equal to n only as function is called like this

$$g(n-1) + g(n-2)$$

g(n-2) is called when we get the return value from g(n-1)

.. It is equal to O(n)

Ans 13] n logn

 n^3

log log n

int Jun (intn)

if
$$(n \le 2)$$
 $fetival;$

else

retwon (Jun (Jloor(squt(n)))+n);

Ans 14) $Ta = T(n/4) + T(n/2) + cn^2$

We can assume

 $T(n/2) >= T(n/4)$
 $T(n) = 2T(n/2) + cn^2$

Applying masters method

 $a = 2$, $b = 2$
 $k = log_b a = log_2 = 1$
 $n = n$
 $f(n) = n^2$

It is $o(n^2)$

But as $T(n) = o(n^2)$
 $f(n) = o(n^2)$

4

Ans 16] if k is a constant greater Han 1
Then T. C = O (log logn)

$$\frac{99 \text{ n}}{100} \quad \frac{99 \text{ n}}{100} \quad \frac{99 \text{ n}}{100^2} \quad \frac{99 \text{ n}}{100^2} \quad \frac{99 \text{ n}}{100^2}$$

If we take longer branch i.e $\frac{990}{100}$ T.C + log $\frac{100}{990}$

We can say that the base of log does not matter as it only a matter of constant.

- Ans 18] a) 100 Log logn In n logn! n logn n2 2n 2n/4n n!
 - b] I Log logn Trogn Logn 2 Logn Log 2nn 2n4n Logn! nlogn no 2(2n) n!
 - C] 96 Logen 5n logn! n logen n logen 8n2 7n3

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Ans 19] linear search (array, key)

for i in array

if value = = key

returni
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Ans 20] Iterative Insertion Sort

insertion sort (arr,n)

loop from i=1 to i=n-1

Pick element arr[i] and insert

it into sorted sequence arr[o--i-i]

Recursive Insertion Sort insertion Sort (arr, n) { if & n <=1 return

insertion sort (arr, n-1)

Pick Last element arr[i] and insert It into sorted sequence arr[o---i-i]

?

Insertion sort considers, one input element per iteration and produces a partial solution without considering Juture elements.

It is called online sorting algorithm
Ans 20/21/22]

Considering only 3 sorting Algo. till now as we get the Lectures of these 3 only.

Algo. Best Case Aug. case Worst case S.C Stable Intace on Bubble Och O(n2) O(n2) O(1) O(0) ×

Selection $O(n^2)$ fo (n^2) $O(n^2)$ $O(i) \times V \times SOHE$

Insertion O(n) $O(n^2)$ $fo(n^2)$ O(1) V V Sort

Ans 23) Binary Search

A ← Sorted array

∩ ← Size of array

× ← value to be sorted

while × not found

if upper bound Lower bound
EXIT: x does not exist

Set mid point = lower bound + (upper bound -Lower bound)/2

ig A [mid point] < x

Lowerbound = midpoint +1

BA [mid point]>x

Upperbound = midpoint-1

if A [midpoint]=x

EXIT = X gound at mid point

Time Complexity

Space Complexity

Linear

O(n)

0(1)

Bineary Search

O(logn)

O(logn)

(Recursive)

Bineary Search (Itorative) O(Logn)

0(1)

Ans 24) T(n) = T(n/2)+c