**INFO6205**

**Program Structures & Algorithms**

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**Virus transmission simulation**

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1. **Introduction**

Coronaviruses are a wide group of viruses that typically cause mild to moderate upper respiratory tract infections. Over the past two decades, three new coronaviruses have emerged from the animal reservoirs causing serious widespread illness and death.

* SARS-CoV (SARS - Severe Acute Respiratory Syndrome)
* MERS-CoV (MERS - Middle East respiratory syndrome)
* SARS-CoV-2 (COVID-19 - Coronavirus disease)

The COVID-19 is a communicable disease and was first reported in Wuhan, China in December 2019 and since then it has spread around the world. It has been declared a global pandemic by World Health Organization.

* **R- naught**

For communicable diseases in a population with no immunity, the basic reproduction parameter (R-naught or ) is the estimated average number of infections produced by a single infectious person. values indicate how rapidly transmission will occur and if a disease will spread or decline within a community.

If the value of is >1 an outbreak will continue and will come to an end for <1. The values are established using mathematical models and are dependent on the parameters and the model hence it varies hugely depending on the country, culture, calculation, stages of the outbreak, etc. Any mitigation or containment strategy will aid in reducing the reproduction number, either by decreasing the transmission rate or the time before infectious individuals are isolated.

* **Dispersion parameter(*k*)**

The dispersion parameter (*k*) plays an important role in explaining the overdispersion and super-spreading of the SARS-CoV-2 virus, it is the measure of the virus’s dispersion. As every infected person does not pass on the virus to the same number of people, this parameter helps in determining if the virus spreads by one person infecting many (big bursts) people or in a steady manner.

If the value of k is small, it means that one infected person can trigger many new cases in a very short time i.e., lower values of *k* corresponding to broader distribution. Several studies suggest that the dispersion parameter *k* for SARS-CoV-2 is on the order of 0.1 [5], approximately 10% of infected people will result in 80% of new infections. The estimated values of R-naught and dispersion parameter for both SARS-CoV and SARS-CoV-2 viruses are given below:

SARS-CoV

* *k* for SARS-CoV is 0.16 with the negative binomial model (Singapore)[8]
* is of the range 0.43–2.41 [9]

SARS-CoV-2

* *k* for SARS-CoV-2 is on the order of 0.1 [5]
* is of the range 2-3 [6][7]

1. **Aim of the project**

The aim of the project is to simulate a SARS-CoV-2 virus and analyze the effectiveness of various preventive measures. The following constraints/factors are taken into consideration for the simulation:

* The R-naught and k factor of the disease
* The usage and effectiveness of masks and social distancing
* The prevalence of testing and contact tracing
* The availability and efficacy of the vaccine
* Remote work and schools
* Quarantine
* Group event

1. **Implementation**
   1. **Algorithm Flow Chart**



Figure 1: Flow Chart

* 1. **Data Structure**

The data structures used for the project are:

1. Array: We store the entire population as an array, we loop through each person, and based on their position and interaction with other nearby populations we update their health conditions.
2. Directed graph: In this project directed graph is implemented to check contact tracing. We can get information on the people infected by a person. The directional graph is represented using an adjacency list. The unique id of people is represented as vertices and once they collide, in the direction of collision the edges are stored. A HashSet is used to store the vertices and the edges of each vertex are saved in the LinkedList.
3. HashMap: All the constraints/ factors required for the simulation are stored and retrieved from the HashMap.
   1. **Simulation**

The project is developed using Java and the simulation is implemented using Java swing graphical user interface (GUI), JFree chart, and Graphics 2D. It is implemented based on a desktop display resolution of 1920x1080 with a scaling of 150%. The simulation is modeled for both SARS-CoV-2 and SARS-CoV. The screenshot of the dashboard is shown in Figure 2.

The simulation is based on various assumptions and study reports. It does not reflect the real-world scenario of SARS-CoV-2 or SARS-CoV, as it would include several other factors. This simulation helps us in getting an understanding of the importance of each factor that we have considered and the effect they have on the transmission of the virus.

In the simulation, each person is represented as a ball, the user can choose the total number of populations from the slider within a range of 50 to 1000. When we start the simulation, initially each person will be given a position, the position of the people keeps changing, and based on their collision with other people we update the health status of the person.

The health conditions of the population are represented by various colors as shown in the legend. The factors/constraints can be selected and the equivalent simulation incorporating the factors/constraints will be generated.

The value of R naught can be defined by the user, the simulation will consider it and during the simulation, each person can only infect that many numbers of people. In case if the R naught value is not specified the simulation transmits on a general scenario where a person can infect a random number of people.

The real-time display of the number of healthy, infected, severe, recovered, and dead people are provided for both the viruses.

The log pane displays the result obtained for each run of the application – Figure 19. The contact tracing details are displayed on the console of the IDE – Figure 13.



Figure 2: Dashboard

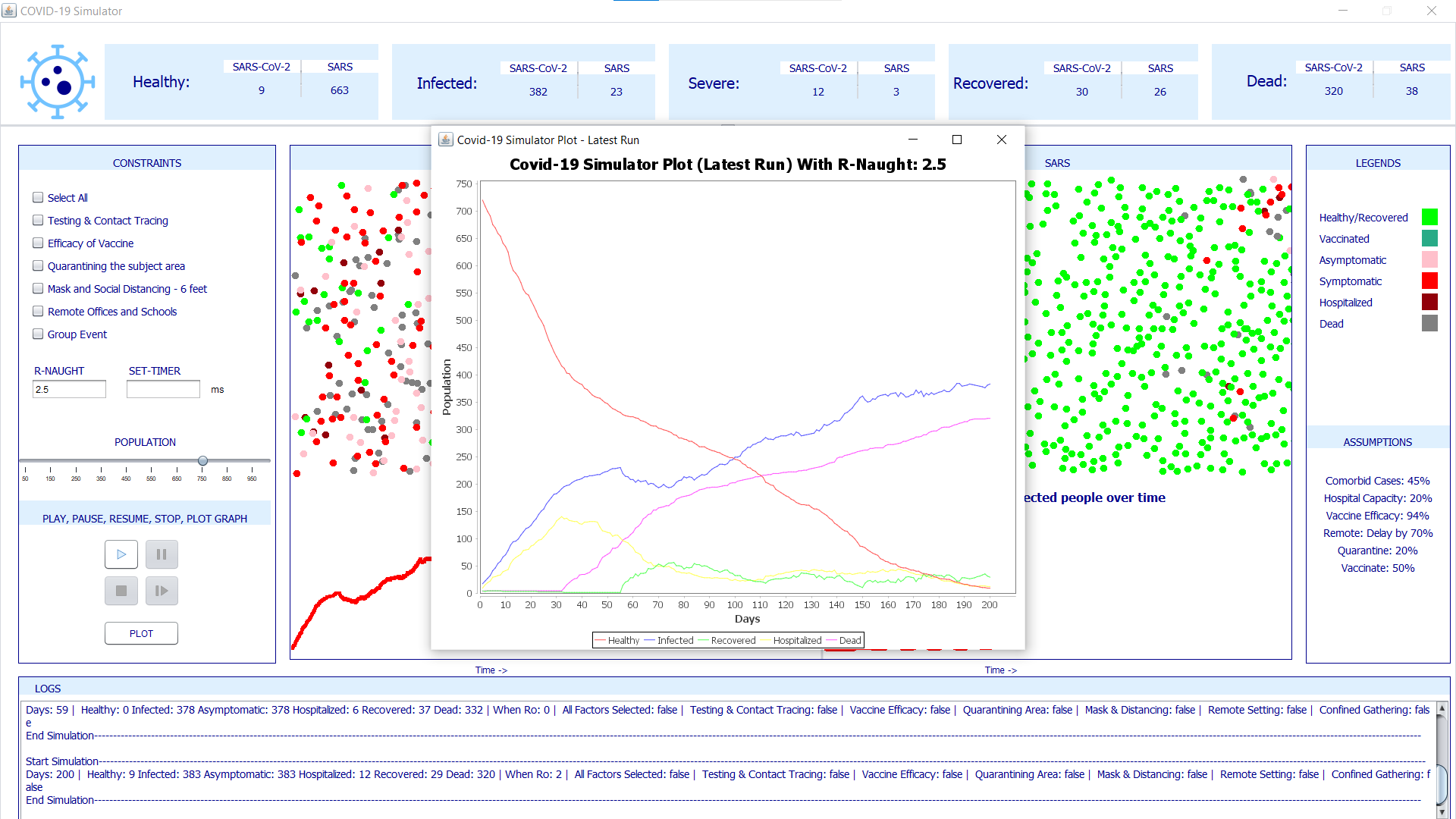


Figure : Growth of infection over the time (in days) with Ro 2.5 without any constraints in the Dashboard

A plot of the number of infections over time can be displayed by clicking on the Plot button. This plot depicts how the infection has grown over time as well as how the healthy part of the population has constantly decreased. This graph can be plotted at any point of time during the simulation run or after the simulation play is stopped. This plot contains the number of healthy, infected, hospitalized, and dead over the number of days the simulation was run as shown in Figure 3. Detailed results for different R-naught values, constraints at various intervals of days are in Figures 14 - 18.

* 1. **SARS-CoV (Compared Virus)**

When simulating the SARS-CoV (SARS) virus, we take into account the incubation period of 3-5 days that is mapped to 3ms before it starts infecting healthy people. Due to the incubation period and recovery time for the virus, the transmission is comparably lower than the SARS-CoV-2 which results in a lower dispersion parameter. When the vaccination constraint is selected, it will not be considered for SARS-CoV simulation as the vaccine is still not developed in the real world for this virus.

1. **Project Details**
   1. **Assumptions** 
      1. **Population types**
2. Healthy (Light Green): Susceptible to the virus. They include people with the comorbid condition. This also includes recovered individuals.
3. Vaccinated (Dark Green): 94% of the population are protected from the virus.
4. Infected – Symptomatic (Bright Red): Primary transmitter of the virus until tested and quarantined.
5. Infected – Asymptomatic (Pink): Undetected transmitter until tested and quarantined.
6. Hospitalized/Severe (Dark Red): If hospitalized they are immobile, and the comorbid condition is checked.
7. Dead (Grey): Immobile and will not further transmit the virus.
   * 1. **Factors considered for simulation**
8. R-naught value:
   1. The R-naught parameter is user-defined, the transmission changes depending on the R-naught value.
   2. The infected population will further transmit the virus only to a number of people defined in R-naught.
   3. For example, if R-naught is 2, an infected person will transmit it only to the first two healthy people that they interact with.
9. Vaccine:
10. 50% of the population is vaccinated.
11. The vaccine efficiency is considered to be 94% [11].
12. Individuals with comorbid conditions will be vaccinated first.
13. There is no vaccine currently available for SARS-CoV, hence it is not considered for the comparison.
14. Testing and Contact Tracing:
15. Testing will detect all the infected populations including symptomatic and asymptomatic. So once testing is considered, the entire simulation will reveal all infected individuals.
16. Quarantine constraint is also taken into account if infected.
17. For contact tracing, the part of the population that comes in contact with the infected person is traced using a directed graph.
18. Quarantining the subject area:
19. 20% of the population will be quarantined.
20. This will include healthy people who have recently traveled, people with health issues, people practicing self-isolation, and infected people.
21. The quarantined healthy population will not be infected by the virus.
22. Infected people who quarantine will not be transmitting the virus to nearby healthy people.
23. Mask and Social Distancing – 6ft:
24. Population displacement will reduce when social distancing is practiced.
25. In this case, the collision(interaction) becomes lesser resulting in less transmission of the virus.
26. Remote Offices and Schools:
27. Population movement is delayed by 70%.
28. Due to the delay, the spreading reduces, as the recovery time elapses.
29. Group Events:
30. A closed confined massive gathering event is attended by a part of the population.
31. A single infected person can infect the entire attending population.
32. When a group event is considered along with R naught value (i.e, R naught > 0), the infected person will transmit only to a certain number of people depending on the R naught value. But even then, since the event has close interaction, the virus still spreads rapidly among the attending population.
    * 1. **General**
33. The recovery time:
    1. Considering the population relative to the size of the panel, we have factored the recovery time of 15 days to 5ms.
    2. After recovery, they are considered as a healthy population and become susceptible to the virus.
34. Death Rate:
35. Both infected people with and without comorbidities get hospitalized based on hospital bed availability.
36. From the hospitalized patients, patients with comorbid conditions are generally considered to die.
37. Asymptomatic Population:
38. We have considered one out of every 3 infected persons to be asymptomatic.
39. Hospitalizing severe population:
40. Severe patients would be hospitalized up to the hospital bed capacity.
41. The hospital capacity is considered to accommodate 20% of the population (This percentage could be changed in the config file).
42. SARS-CoV incubation period:
43. We have factored the incubation period of 5 - 7 days to 3ms.
44. After the incubation period, it gets transmitted to others.
    1. **Config.ini**

Below are the parameters we have taken and that can be modified in the Config.ini file:

1. Infection Parameters:
2. infectionRate: This is the percentage of the population initially infected. We have taken it as 0.1, which means 10% of the population would be infected at the start of the simulation.
3. asymptoticFraction: Fraction of asymptomatic infected people. We have taken 3, i.e, 1 out of 3 infected people is asymptomatic.
4. comorbidPercentage: Percentage of population that are comorbid. Currently considered as 45%.
5. infectedQuarantinePercentage: When quarantine constraint is selected, this is the percentage of the infected population that quarantine. Taken as 20%.
6. Vaccine Parameters:
7. vaccinatedPercentage: This is the percentage of the population that is vaccinated when we consider the efficacy of vaccine constraint. Currently considered as 50%.
8. vaccineEffectiveness: Percentage of vaccinating population that does not get infected. Effectiveness is considered as 94%.
9. Population Ball Parameters:
10. populationBallHeight: Height of the 2D Graphics ball shape components that we have considered for displaying population.
11. populationBallWidth: Width of the 2D Graphics ball shape components that we have considered for displaying population.
12. Other Conditions:
13. hospitalCapacity: The capacity of the hospital is considered based on the percentage of the population. i.e, if hospitalCapacity is 0.2 then the hospital capacity is 20% of the total population.
14. **Outputs**

The following are the results observed for the simulation for various constraints/factors.

1. **Comparison plot for social distancing and mask condition**

|  |  |  |
| --- | --- | --- |
| Time(ms) | With Social Distancing and Mask | Without Social Distancing and Mask |
| 1 | 20 | 33 |
| 2 | 34 | 43 |
| 3 | 69 | 87 |
| 4 | 101 | 104 |
| 5 | 189 | 322 |
| 6 | 254 | 273 |
| 7 | 229 | 325 |

****

Figure :Comparison plot for social distancing and mask condition

When people follow social distancing and mask, the simulation shows that the displacement of the population is less. Due to this, there is lesser collision resulting in reduced transmission of the virus.

We observed that when social distancing is not followed the mean infected count is 169 and when social distancing is considered the mean infection count is 128. There is a 24% reduction of infection if we follow social distancing and use masks.

1. **Comparison plot for quarantine condition**

|  |  |  |
| --- | --- | --- |
| Time(ms) | With Quarantine | Without Quarantine |
| 1 | 22 | 49 |
| 2 | 29 | 79 |
| 3 | 20 | 166 |
| 4 | 62 | 161 |
| 5 | 65 | 302 |
| 6 | 94 | 226 |
| 7 | 94 | 474 |



Figure : Comparison plot for quarantine condition

On considering quarantine condition, many infected and a few healthy people stay immobile in the simulation. The infected people that quarantine does not infect healthy population and the healthy people who follow quarantine do not get infected. This causes a reduction in virus transmission.

We observed that when quarantine is not considered the mean infected count is 208 and when quarantine is considered it is 55. There is a 73% reduction of infection if we follow quarantine.

1. **Comparison Plot for Remote Work/School condition**

|  |  |  |
| --- | --- | --- |
| Time(ms) | Remote | Not Remote |
| 1 | 20 | 78 |
| 2 | 42 | 69 |
| 3 | 14 | 202 |
| 4 | 18 | 258 |
| 5 | 21 | 165 |
| 6 | 30 | 436 |
| 7 | 27 | 476 |



Figure : Comparison Plot for Remote Work/School condition

When the population considers remote work and schools, the simulation shows a delay of movement. Due to this delay, the infected people are seen to recover much before spreading to the healthy group. This way remote condition reduces virus transmission.

We observed that when all offices and schools are open the mean infected count is 240 whereas the mean count is 24 when offices and schools go remote. There is a 90% reduction of infection.

1. **Comparison plot considering vaccination parameter**

|  |  |  |
| --- | --- | --- |
| Time (ms) | Vaccinated | Not Vaccinated |
| 1 | 19 | 56 |
| 2 | 29 | 84 |
| 3 | 54 | 202 |
| 4 | 67 | 257 |
| 5 | 69 | 310 |
| 6 | 98 | 373 |
| 7 | 194 | 427 |



Figure :Comparison plot for vaccination

When the vaccine constraint is considered, 50% of the population is vaccinated Out of the vaccinated population, 94% of them do not get infected.

We observed that when in a group without any vaccination the mean infected count is 244 and when a group with vaccination is considered, the mean infection count is 75. There is a 69% reduction of infection.

All the above graphs depicted the impact of each factor on the SARS-CoV-2 virus transmission.

1. **Comparison by considering all factors and without any factors**

In the simulation when all factors are considered, we could see that the population moves around slowly. This is due to remote work, some components are immobile as they get tested and follow quarantining, social distancing, wearing masks and some groups have been vaccinated. All these factors help in reducing the virus spread.

|  |  |  |
| --- | --- | --- |
| Time(ms) | All Factors | No Factors |
| 1 | 36 | 5 |
| 2 | 57 | 7 |
| 3 | 74 | 8 |
| 4 | 145 | 8 |
| 5 | 265 | 9 |
| 6 | 341 | 9 |

Figure :Comparison by considering all factors and no factors.

From this graph, it can be observed when no factors are considered the number of infected people increases exponentially over time whereas when all factors are considered the growth is logarithmic. This graph shows the importance of following all the factors/constraints to reduce the spread of the virus.

1. **Comparison between different R-naught values**

|  |  |  |
| --- | --- | --- |
| R0 | No factors | All factors |
| 1 | 25 | 25 |
| 2 | 184 | 5 |
| 3 | 418 | 7 |
| 4 | 463 | 11 |
| 5 | 470 | 6 |
| 6 | 494 | 5 |
| 7 | 500 | 6 |

Figure :Comparison between different R-naught values.

This graph depicts the relation of the basic reproduction parameter with virus transmission for a constant time(5ms). The population was taken as 500 for this simulation and we can observe that by R0 = 7 all people were infected within this time frame. This shows that as the R naught value increases the transmission of the virus is faster.

1. **Comparison between SARS-CoV-2 and SARS-CoV without considering any constraints.**

|  |  |  |
| --- | --- | --- |
| Time(ms) | SARS-CoV-2 | SARS-CoV |
| 1 | 52 | 20 |
| 2 | 96 | 17 |
| 3 | 136 | 18 |
| 4 | 188 | 24 |
| 5 | 187 | 23 |
| 6 | 235 | 30 |

Figure :Comparison between SARS-CoV-2 and SARS-CoV

It can be analyzed that the number of infected people increases exponentially over time for SARS-CoV-2 whereas for SARS-CoV it increases only by a small fraction when no constraints are considered.

1. **Comparison between R0=0 value vs R0=1 and R0=2.5 over time.**

|  |  |  |  |
| --- | --- | --- | --- |
| Time(ms) | R0 =0 | R0=1 | R0=2.5 |
| 1 | 39 | 21 | 19 |
| 2 | 25 | 32 | 54 |
| 3 | 40 | 39 | 35 |
| 4 | 62 | 30 | 40 |
| 5 | 115 | 32 | 43 |
| 6 | 81 | 26 | 58 |
| 7 | 153 | 26 | 55 |



Figure :Comparison between no R0 value vs R0=1 and R0=2.5

When R0 is not considered, the spreading is very high compared to R0=1 and R0=2.5. This implies that R0 alone is not efficient enough to analyze the virus transmission.

1. **Comparison plot for infection based on group event over time with and without factors.**

|  |  |  |
| --- | --- | --- |
| Time (ms) | No factors | All factors |
| 1 | 43 | 6 |
| 2 | 109 | 7 |
| 3 | 181 | 13 |
| 4 | 299 | 8 |
| 5 | 401 | 13 |
| 6 | 105 | 7 |

Figure :Comparison plot for a group event

It can be observed from the graph that if at least one infected person is present inside the group it can infect everyone, and the result is a drastic spike if no factors/constraints are considered.

Based on our analysis of the R naught comparison plots in Figures 9 and 11, we can infer the relationship between R naught and the number of infections. As the value of R naught increases the transmission of the virus is faster.

For the SARS-CoV-2 simulation, R naught was considered as 2.5, it was observed that when an infected person who has previously infected 2 people comes to attend a closed group event, there are no more people infected by this person. But this is not the real scenario, if an infected person is attending a closed group event it is possible for the person to infect all the people attending the event as shown in the simulation. This brings the dispersion constant *k* into the picture and shows that the basic reproductive parameter alone is not efficient enough to determine the virus transmission. In cases like a group event, a single person can transmit the virus to multiple people whereas in other scenarios a person may not even transmit it to another person.

1. **Contact Tracing**



Figure : Contact tracing screenshot with all constraints.

On the IDE console after each run, the contact tracing for each person is displayed. It shows that person A234795 has infected person A309125. The contract tracing is checked only when an infected person comes in contact with a healthy person. The number of infected people when all factors/constraints are selected is small.

1. **Result Plots**

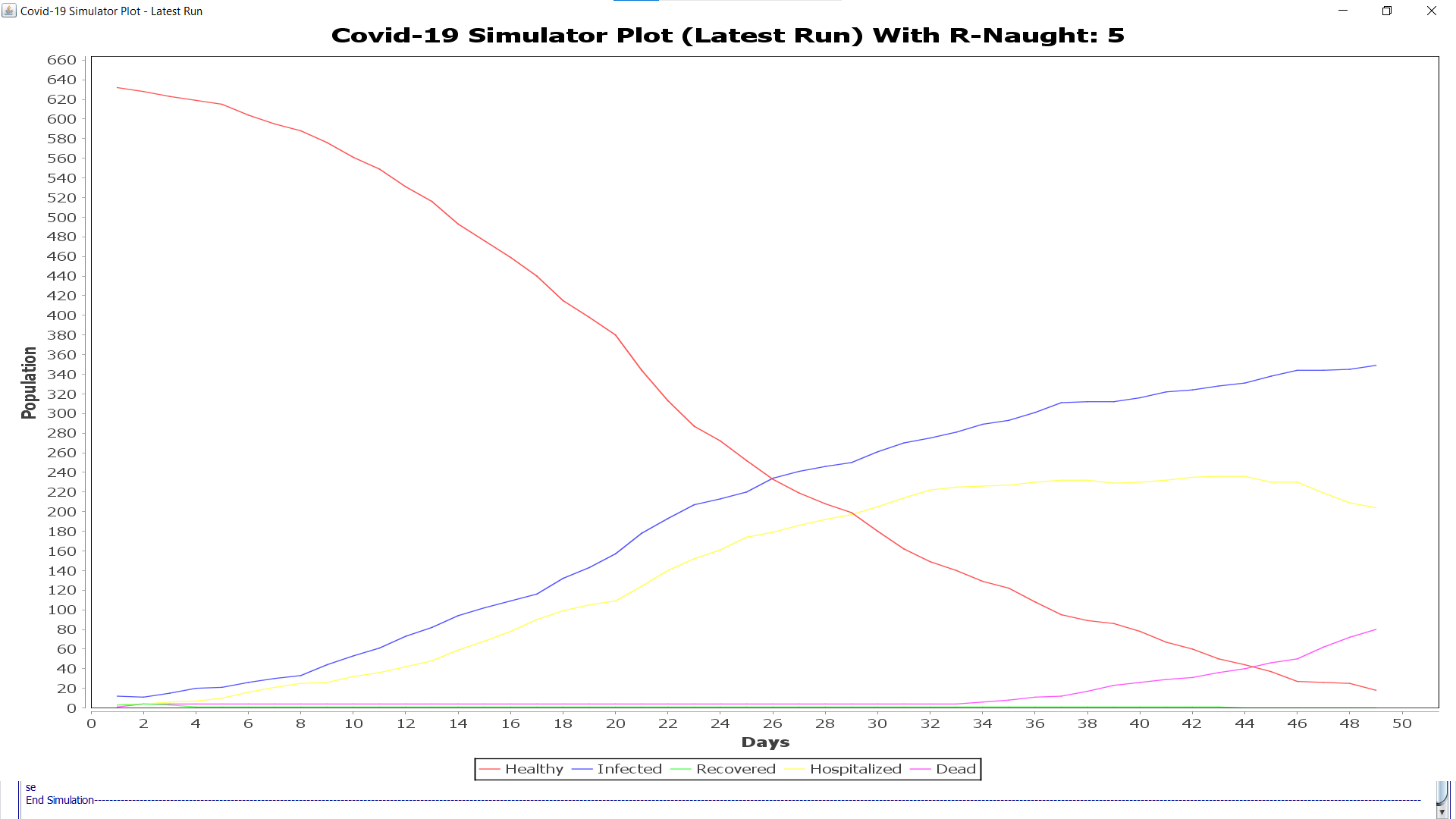
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Figure : Simulator Plot with R-Naught=5 and without any constraints for a population of 640 over 50 days.

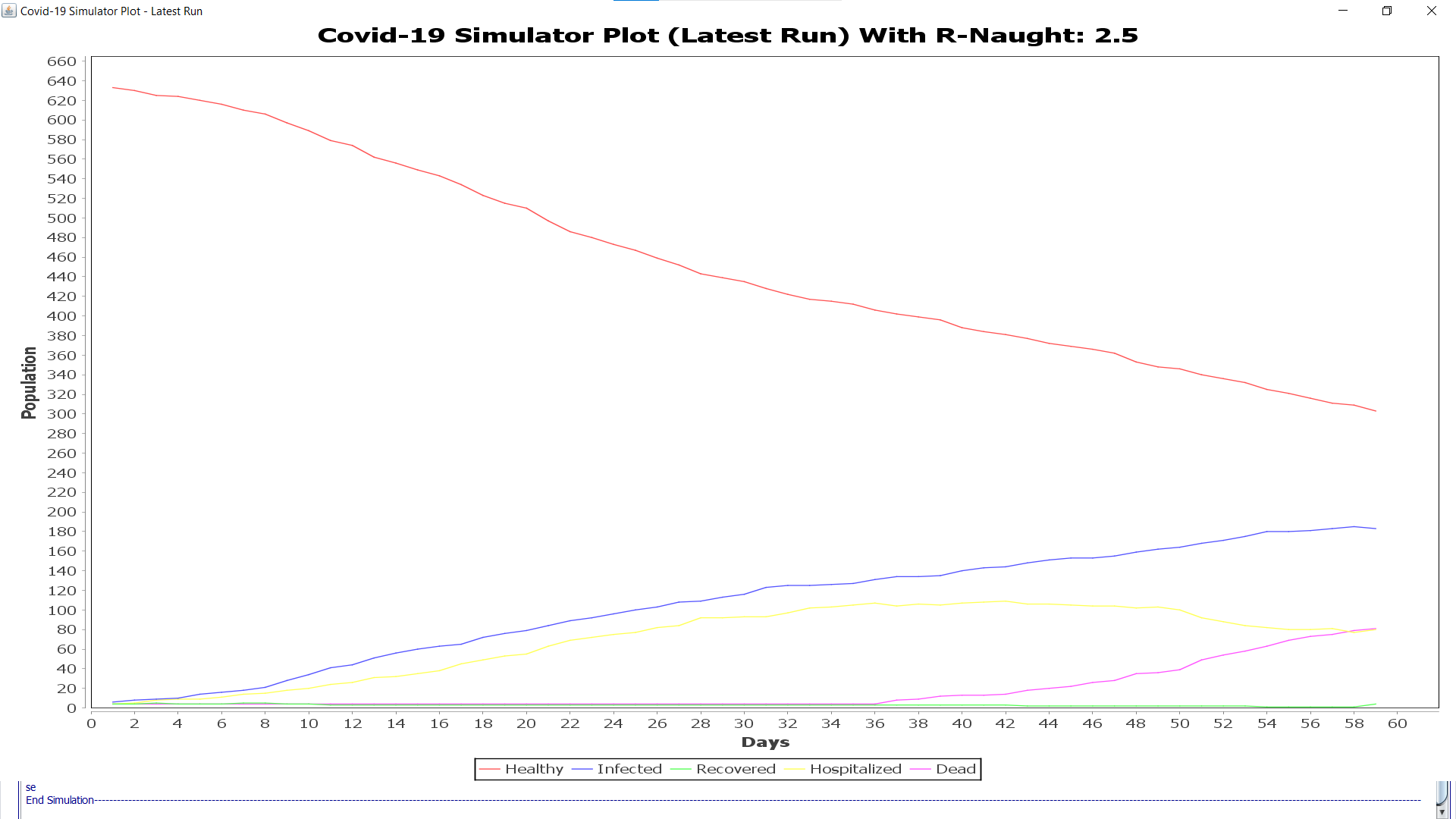


Figure : Simulator Plot with R-Naught=2.5 and without any constraints for a population of 640 over 50 days

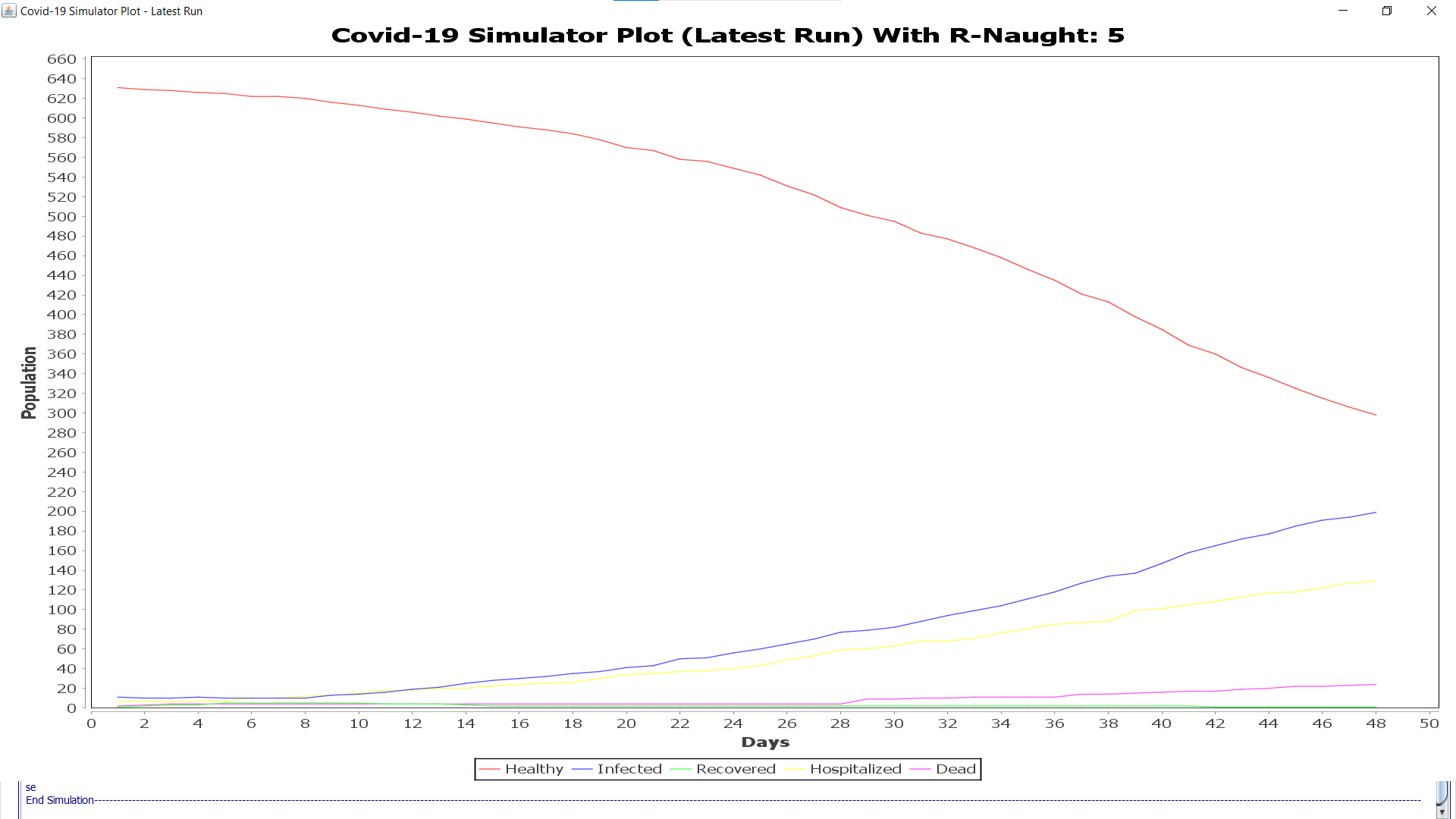
****

Figure : Simulator Plot with R-Naught=5 and with testing, contact tracing, mask mandate & social distancing in effect for a population of 640 over 50 days

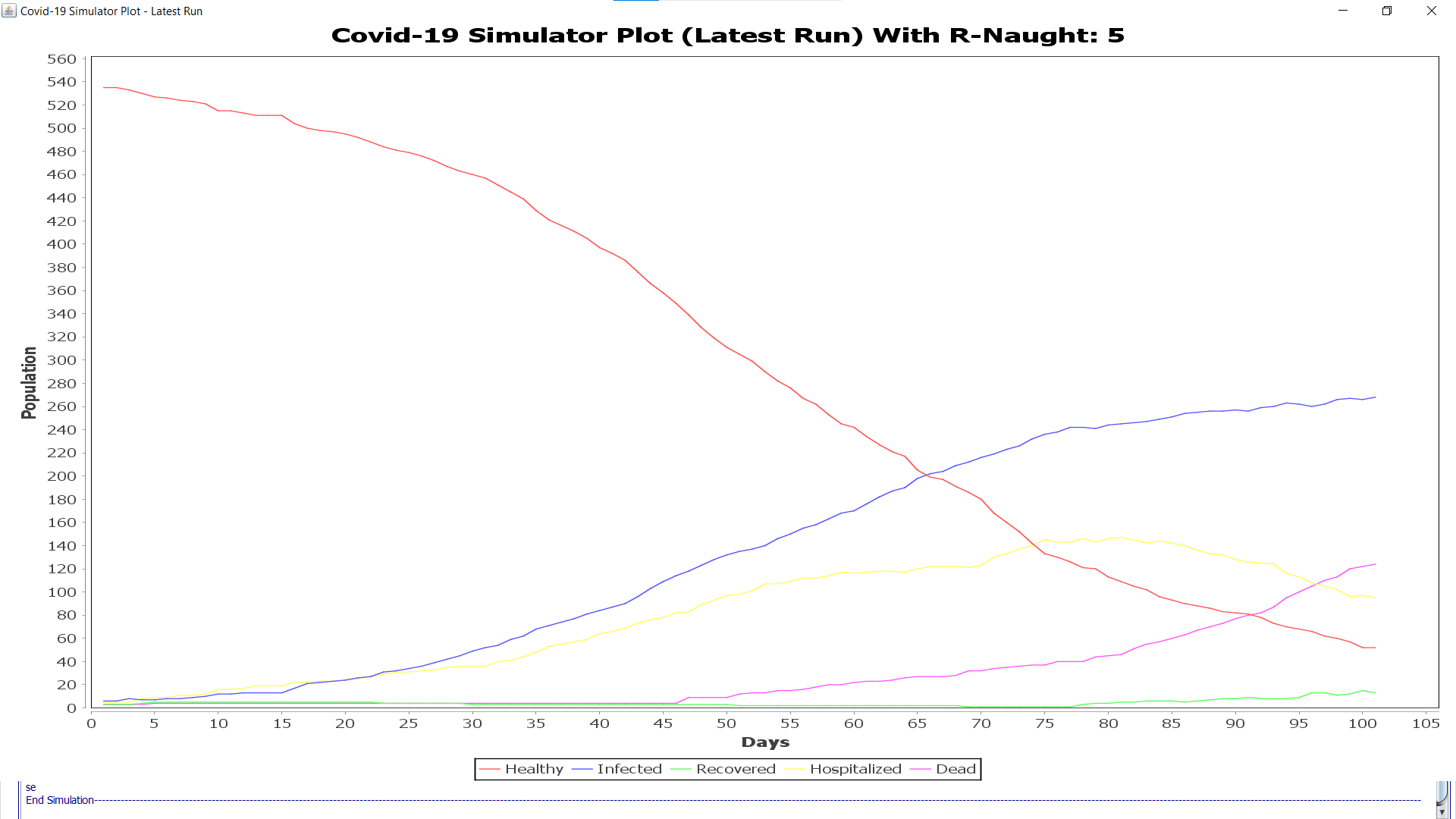
****

Figure : Simulator Plot with R-Naught=5 and with testing, contact tracing, mask mandate & social distancing in effect for a population of 540 over 105 days

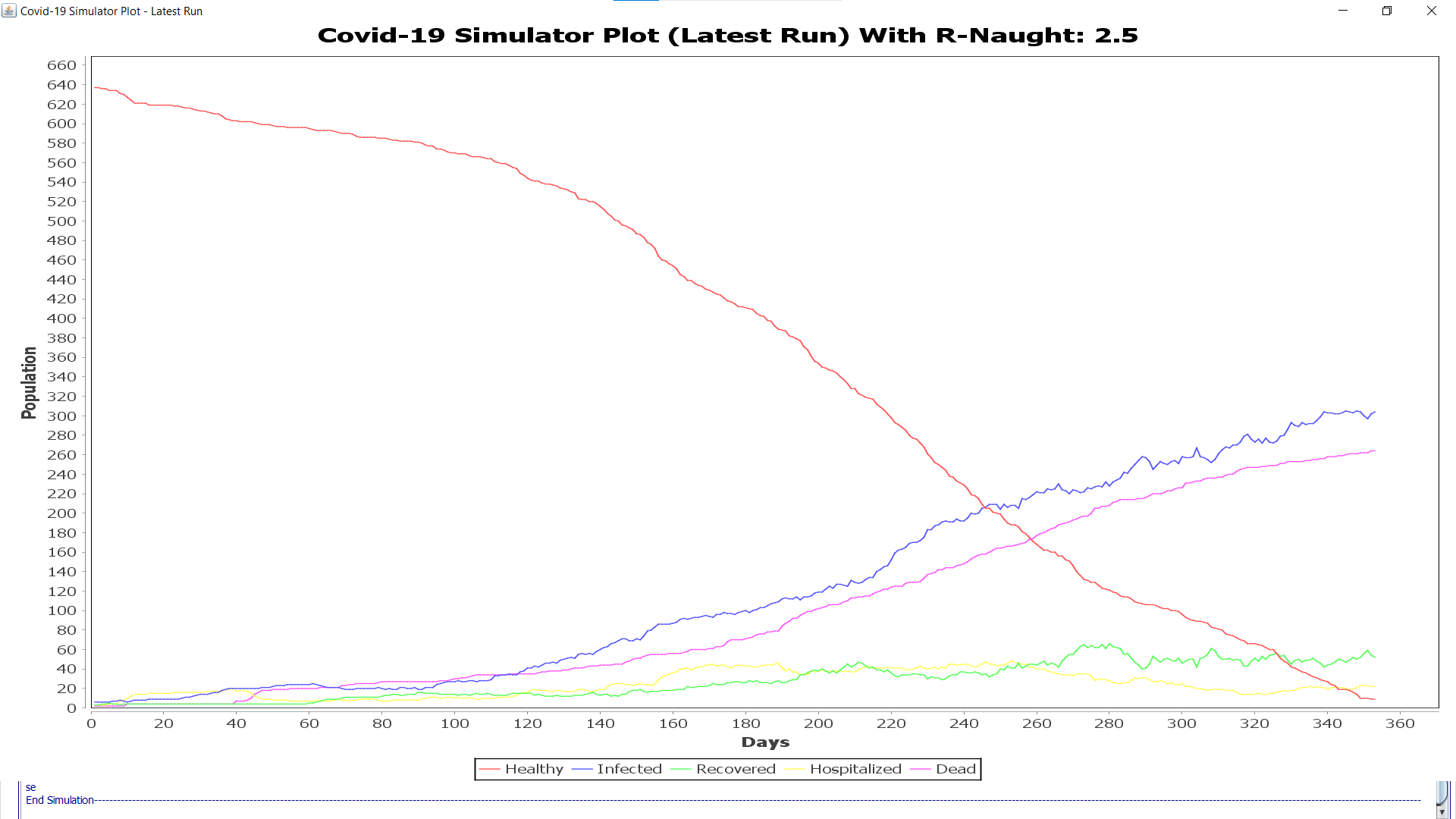
****

Figure : Simulator Plot with R-Naught=2.5 and with testing, contact tracing, mask mandate & social distancing in effect for a population of 640 over 360 days.

1. **Log pane**

*Figure 19: Log pane*

1. **Mathematical Analysis/Evidence**
3. 1. **Big O**

It can be observed from Figure 7 that for the scenario when no factors/constraints are selected or followed by the people, the transmission increases, and the growth is exponential – O (**. By incorporating the algorithm that includes all factors/constraints the growth** was improved to logarithmic time **- O(log(n)).**

* 1. **Entropy**

At the beginning of the simulation, the available data is minimum, this is when the entropy is at the highest. With time, we analyze the effect of factors/constraints on the transmission of the virus. This results in a lower entropy.

* 1. **Invariant**

1. Array:
   1. For the population stored in an array, whenever a person collides with another person the position will change, and the status will be updated accordingly.
2. Directed Graph:
   1. When an infected person collides with a healthy person, the direction of the edge is only from the infected person to a healthy person.
   2. There will not be any duplicated vertices(person).
3. **Unit tests and code coverage result:**

The unit test coverage for the project is 80.5%. The snapshots of unit test and code coverage results:

1. Solution:

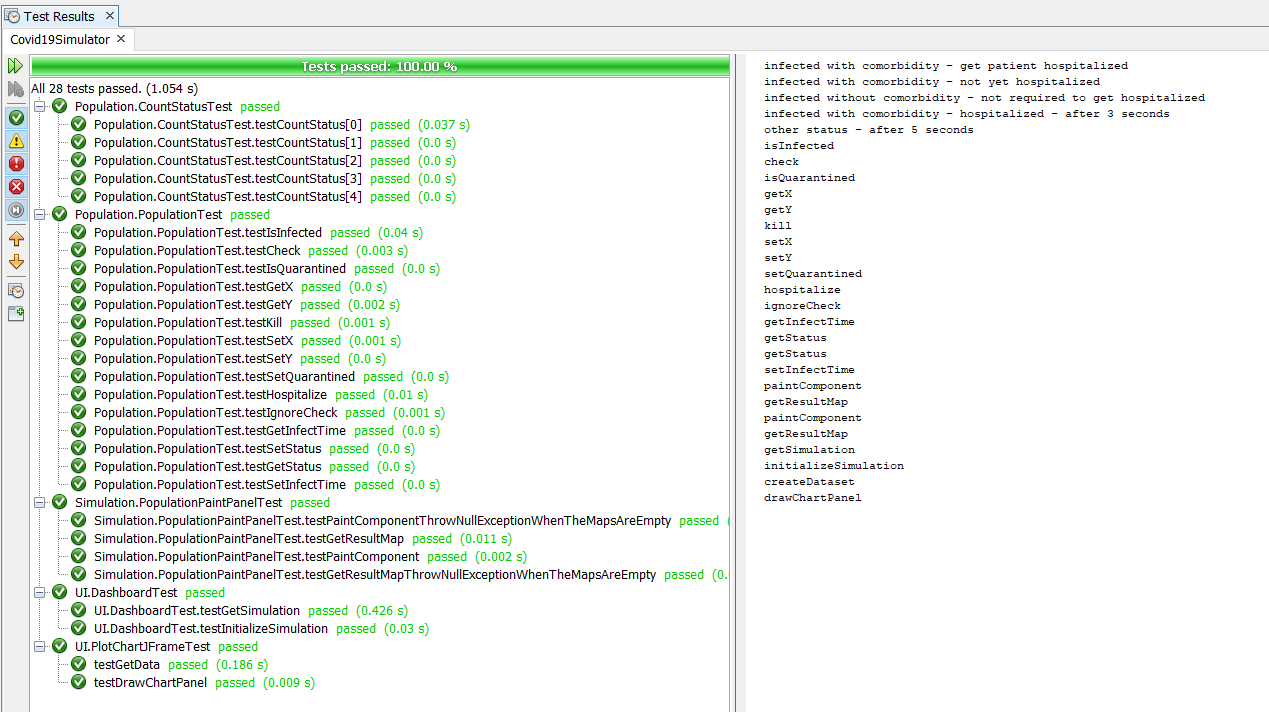


Figure : All tests execution.

1. Unit test for Population package:
2. CountStatusTest.java



Figure : Unit test for CountStatusTest.java

1. PopulationTest.java



Figure : Unit test for PopulationTest.java

1. Unit test for Simulation package:
2. PopulationPaintPanelTest.java



Figure : Unit test for PopulationPaintPanelTest.java

1. Unit test for UI package:
2. DashboardTest.java



Figure : Unit test for DashboardTest.java

1. PlotChartJFrameTest.java



Figure 25: Unit test for PlotChartJFrame

1. Code coverage:

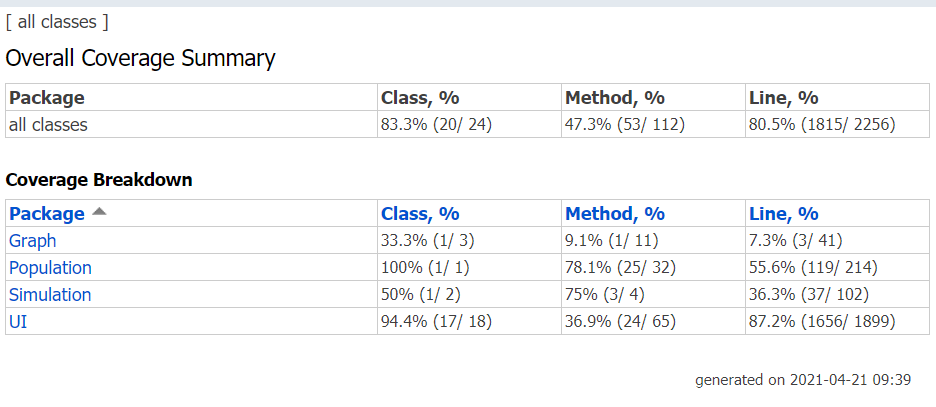


Figure 26: Code coverage result.

1. **Conclusion**

The spread of SARS-CoV-2 and SARS-CoV virus was simulated and analyzed. When two viruses - SARS-CoV-2 and SARS-CoV of different k/R factors were compared, the spreading was relatively smaller for the SARS-CoV virus.

The R naught value that estimates the average number of transmissions by a single infectious person does not give us the actual virus transmission rate when compared to real-life scenarios where one person can transmit the infection to a random number of people based on the dispersion parameter(*k*) in case of events or gatherings.

It can be concluded from the results that when no precautions(factors/constraints) are considered the transmission growth rate is exponential, this transmission growth rate was improved to logarithmic time when all precautions (factors/constraints) were incorporated.

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