

→ Fractional Knapsack Problem:

Objects (o)	1	2	3	4	5	6	7
Profit (P)	5	10	15	7	8	9	4
Weight (w)	1	3	5	4	1	3	2

$W = 15$
$n = 7$

→ Max Profit = ?

Approach 1 Profit	47.25
Approach 2 Profit	46
Approach 3 Profit	51

Approach-1 To Choose objects in random manner.

Approach-2 To choose objects in minimum weight first.

Approach-3 To choose  $\frac{P_i}{W_i}$  based in decreasing order.

Objects (o)	1	2	3	4	5	6	7
Profit (P)	5	10	15	7	8	9	4
Weight (w)	1	3	5	4	1	3	2
$\frac{P_i}{W_i}$	5	3.3	3	1.75	8	3	2

Max  $\frac{P_i}{W_i}$  Ratio

Objects	Profit	Weight	Remaining weight
5	8	1	$15 - 1 = 14$
1	5	1	$14 - 1 = 13$
2	10	3	$13 - 3 = 10$
3	15	5	$10 - 5 = 5$
6	9	3	$5 - 3 = 2$
7	4	2	$2 - 2 = 0$
	51		



Greedy Knapsack ( )

②

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for  $i = 1$  to  $n$

Compute  $P_i/W_i \Rightarrow O(n)$

Sort objects in non increasing order.  $\Rightarrow O(n \log n)$

For  $i = 1$  to  $n$  from sorted list.

if ( $m > 0$  &  $w_i \leq m$ )

$m = m - w_i$   
 $P = P + P_i$  }  $O(n)$

Else

Break;

if ( $m > 0$ )

$P = P + P_i \left( \frac{m}{w_i} \right) \Rightarrow O(1)$

}

$TC = O(n) + O(n \log n) + O(n) + O(1)$

$\Rightarrow O(n \log n)$

→ Applications

- ① Portfolio optimization.
- ② Power allocation management.
- ③ Resource management in S/w industry.
- ④ Home energy management.