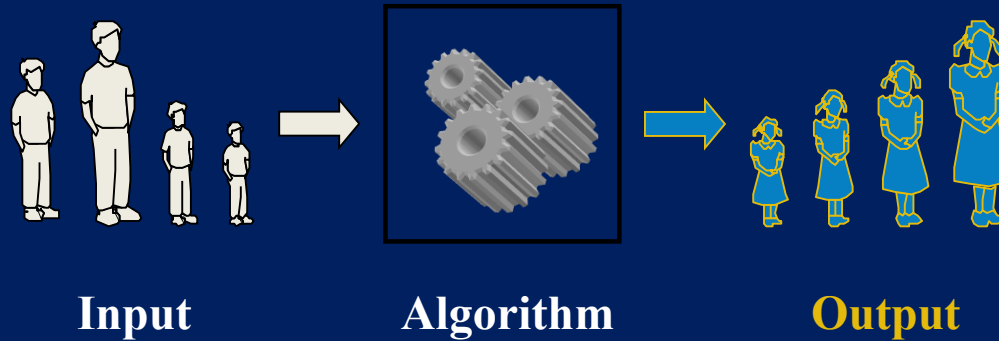


DESIGN & ANALYSIS OF ALGORITHM (BCSC0012)

Chapter 4: Sorting Shell Sort



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Shell Sort

- Invented by Donald Shell in 1959.
- 1st algorithm to break the quadratic time barrier but few years later, a sub quadratic time bound was proven
- Shell sort works by comparing elements that are **distant** rather than adjacent elements in an array.
- Shell sort uses a sequence h_1, h_2, \dots, h_t called the **increment sequence**. Any increment sequence is fine as long as $h_1 = 1$ and some other choices are better than others.

Shell Sort

- Shell sort makes multiple passes through a list and sorts a number of equally sized sets using the insertion sort.
- Shell sort improves on the efficiency of insertion sort by shifting values to their destination.

Shell sort is also known as ***diminishing increment sort***.

The distance between comparisons decreases as the sorting algorithm runs until the last phase in which adjacent elements are compared

Empirical Analysis of Shell sort (Advantage)

- Advantage of Shell sort is that its only efficient for medium size lists. For bigger lists, the algorithm is not the best choice. Fastest of all $O(N^2)$ sorting algorithms.
- 5 times faster than the bubble sort and a little over twice as fast as the Insertion sort, its closest competitor.

Empirical Analysis of Shell sort (Disadvantage)

- Disadvantage of Shell sort is that it is a complex algorithm and its not nearly as efficient as the **merge**, **heap**, and **quick sorts**.
- The shell sort is still significantly slower than the merge, heap, and quick sorts, but its relatively simple algorithm makes it a good choice for sorting lists of less than 5000 items unless speed important. It's also an excellent choice for repetitive sorting of smaller lists.

Shell Sort

- Comparison based sorting technique.
- Starts with gap = $\lfloor n/2 \rfloor$, where n = no. of elements.
- One by one select elements to the right of the gap and place them at their appropriate position.

Time Complexity

Best $O(n \log n)$

Worst $O(n^2)$

Average $O(n \log n)$

Space Complexity $O(1)$

Shell Sort: Example

| | | | | | | | | | |
|----|----|---|---|---|----|----|----|---|---|
| 19 | 63 | 2 | 6 | 7 | 18 | 60 | 16 | 9 | 4 |
|----|----|---|---|---|----|----|----|---|---|

Solution:

N=10 ; gap = $\lfloor n/2 \rfloor = 5$

PASS I:

| | | | | | | | | | |
|----|----|---|---|---|----|----|----|---|---|
| 19 | 63 | 2 | 6 | 7 | 18 | 60 | 16 | 9 | 4 |
|----|----|---|---|---|----|----|----|---|---|



| | | | | | | | | | |
|----|----|---|---|---|----|----|----|---|---|
| 18 | 63 | 2 | 6 | 7 | 19 | 60 | 16 | 9 | 4 |
|----|----|---|---|---|----|----|----|---|---|



| | | | | | | | | | |
|----|----|---|---|---|----|----|----|---|---|
| 18 | 60 | 2 | 6 | 4 | 19 | 63 | 16 | 9 | 7 |
|----|----|---|---|---|----|----|----|---|---|



| | | | | | | | | | |
|----|----|---|---|---|----|----|----|---|---|
| 18 | 60 | 2 | 6 | 4 | 19 | 63 | 16 | 9 | 7 |
|----|----|---|---|---|----|----|----|---|---|

Shell Sort: Example ...

Pass II:

$$\text{gap} = \lfloor 5/2 \rfloor = 2$$

| | | | | | | | | | |
|----|----|---|---|---|----|----|----|---|---|
| 18 | 60 | 2 | 6 | 4 | 19 | 63 | 16 | 9 | 7 |
|----|----|---|---|---|----|----|----|---|---|



| | | | | | | | | | |
|----|----|---|---|---|----|----|----|---|---|
| 18 | 60 | 2 | 6 | 4 | 19 | 63 | 16 | 9 | 7 |
|----|----|---|---|---|----|----|----|---|---|



| | | | | | | | | | |
|---|---|---|---|---|----|----|----|----|----|
| 2 | 6 | 4 | 7 | 9 | 16 | 18 | 19 | 63 | 60 |
|---|---|---|---|---|----|----|----|----|----|



| | | | | | | | | | |
|---|---|---|---|---|----|----|----|----|----|
| 2 | 6 | 4 | 7 | 9 | 16 | 18 | 19 | 63 | 60 |
|---|---|---|---|---|----|----|----|----|----|

Shell Sort: Example ...

Pass III:

$$\text{gap} = \lfloor 2/2 \rfloor = 1$$

| | | | | | | | | | |
|---|---|---|---|---|----|----|----|----|----|
| 2 | 6 | 4 | 7 | 9 | 16 | 18 | 19 | 63 | 60 |
| ↓ | | | | | | | | | |
| 2 | 6 | 4 | 7 | 9 | 16 | 18 | 19 | 63 | 60 |
| ↓ | | | | | | | | | |
| 2 | 4 | 6 | 7 | 9 | 16 | 18 | 19 | 60 | 63 |

Shell Sort: Example 2

EXAMPLE 2:

| | | | | | | | |
|----|----|----|---|----|----|----|---|
| 18 | 32 | 12 | 5 | 38 | 33 | 16 | 2 |
|----|----|----|---|----|----|----|---|

Shell Sort: Example 2 ...

EXAMPLE 2:

| | | | | | | | |
|----|----|----|---|----|----|----|---|
| 18 | 32 | 12 | 5 | 38 | 33 | 16 | 2 |
|----|----|----|---|----|----|----|---|

Solution:

N=8 ; gap = $\lfloor n/2 \rfloor = 4$

PASS I:

| | | | | | | | |
|----|----|----|---|----|----|----|---|
| 18 | 32 | 12 | 5 | 38 | 33 | 16 | 2 |
|----|----|----|---|----|----|----|---|



| | | | | | | | |
|----|----|----|---|----|----|----|---|
| 18 | 32 | 12 | 5 | 38 | 33 | 16 | 2 |
|----|----|----|---|----|----|----|---|



| | | | | | | | |
|----|----|----|---|----|----|----|---|
| 18 | 32 | 12 | 2 | 38 | 33 | 16 | 5 |
|----|----|----|---|----|----|----|---|

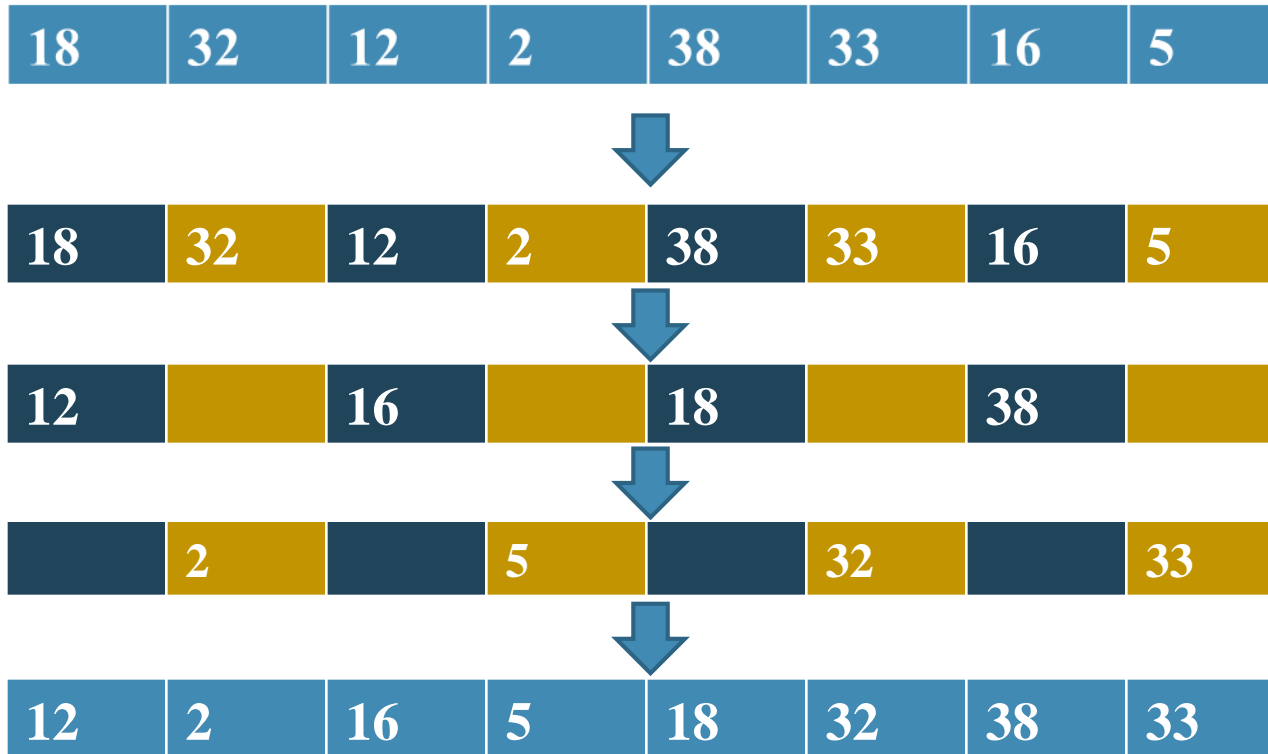


| | | | | | | | |
|----|----|----|---|----|----|----|---|
| 18 | 32 | 12 | 2 | 38 | 33 | 16 | 5 |
|----|----|----|---|----|----|----|---|

Shell Sort: Example 2 ...

PASS II:

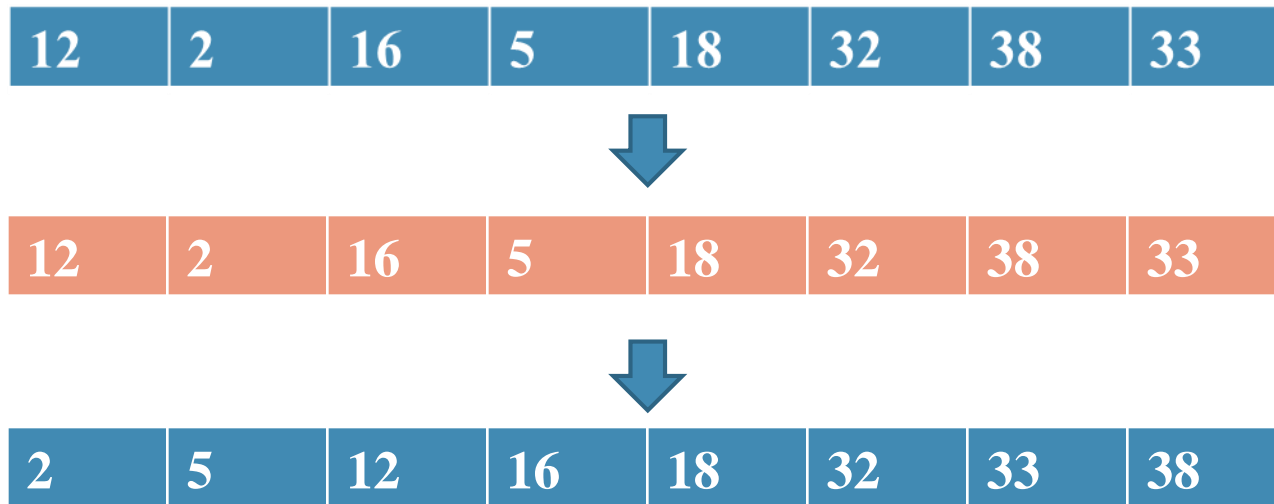
$$\text{gap} = \lfloor 4/2 \rfloor = 2$$



Shell Sort: Example 2 ...

PASS III:

$$\text{gap} = \lfloor 2/2 \rfloor = 1$$



Shell Sort: Algorithm

Shell Sort(A, n)

```
for( gap = n/2; gap>0; gap = gap/2)
```

```
{
```

```
    for(i = gap; i < n; i++)
```

```
    {
```

```
        temp=A[i];
```

```
        for(j=i; j>=gap && A[j-gap]>temp; j=j-gap)
```

```
        {
```

```
            A[j]= A[j-gap]
```

```
        }
```

```
        A[j]=temp;
```

```
    }
```

```
}
```

| | | | | |
|----|----|----|---|---|
| 12 | 34 | 54 | 2 | 3 |
|----|----|----|---|---|

$N=5$, $gap = \lfloor 5/2 \rfloor = 2$

“Thank you”

Any Questions ?



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