

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB REPORT on

Artificial Intelligence (23CS5PCAIN)

Submitted by

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in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

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CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Anjana Manoj (IBM23CS038)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

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Github Link:

https://github.com/AnjanaManoj-05/AI_LAB



Program 1

Implement Tic – Tac – Toe Game

Algorithm:

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> Lab Programme

1. Tic Tac Toe game

→ Algorithm

1. Start
2. Initialize a 3x3 board with " " (empty)
3. Design
 - Human player = "X"
 - Computer = "O"
4. Display the board
5. Repeat until game ends:
 - Step A: Human's turn
 - 1) Ask user to enter a row (1-3) and column (1-3)
 - 2) If the user chooses empty cell → place "X"
 - 3) Else → display error and ask again
 - 4) Display the board
 - 5) If human wins → print "You win" → stop
 - 6) If board is full → print "Draw" → stop
 - Step B: Computer's turn
 - 1) Call the BestMove() function
 - In BestMove(Board):
 - Initialize best_score = -∞
 - For each empty cell:
 - place "O"
 - Call Minimax(board, depth, isMaximizing = false)
 - undo the move
 - If score > best_score → update best_score
 - Update best_score = update best_score
 - and store the current this move

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Return best move

- 2) Place "O" in the best move cell
- 3) Display board
- 4) If computer wins → print "Computer wins" → stop
- 5) If board is full → print "Draw" → stop
6. Minimax(board, depth, isMaximizing):
 - If "O" wins → return +1
 - If "X" wins → return -1
 - If board is full → return 0
 - isMaximizing = True (Computer's Turn)
 - Set best_score = -∞
 - For each empty cell:
 - place "O"
 - Recursively call Minimax with isMaximizing = False
 - undo move
 - Update best_score = max(best_score, score)
 - Return best_score
 - Else (Human's Turn)
 - For each empty cell:
 - place "X"
 - Recursively call Minimax with isMaximizing = True
 - undo move
 - Set best_score = min(best_score, score)
 - Return best_score

Code:

```
def print_board(board):
    print("\nCurrent Board:")
    for row in board:
        print(row)
    print()

def check_winner(board, player):
    for i in range(3):
        if all(cell == player for cell in board[i]):
            return True
        if all(board[j][i] == player for j in range(3)):
            return True

    if all(board[i][i] == player for i in range(3)):
        return True
    if all(board[i][2 - i] == player for i in range(3)):
        return True

    return False

def is_full(board):
    return all(cell != " " for row in board for cell in row)

def tic_tac_toe():
    board = [[" " for _ in range(3)] for _ in range(3)]
    current_player = "X"
    move_count = 0

    print("Tic-Tac-Toe Game (3x3 Matrix Format)\n")
    print_board(board)

    while True:
        try:
            row = int(input(f"Player {current_player}, enter row (0-2): "))
            col = int(input(f"Player {current_player}, enter col (0-2): "))
        except ValueError:
            print("Please enter integers between 0 and 2.")
            continue

        if not (0 <= row <= 2 and 0 <= col <= 2):
```

```

        print("Invalid position. Try again.")
        continue
    if board[row][col] != " ":
        print("Cell already filled. Choose another.")
        continue

    board[row][col] = current_player
    move_count += 1
    print_board(board)

    if check_winner(board, current_player):
        print(f"Player {current_player} wins!")
        break

    if is_full(board):
        print("Game is a draw.")
        break

    current_player = "O" if current_player == "X" else "X"

    print(f"Total moves (cost): {move_count}")

tic_tac_toe()

```

Output case1:

Tic-Tac-Toe Game (3x3 Matrix Format)

```

Current Board:
[' ', ' ', ' ', ' ', ' ']
[' ', ' ', ' ', ' ', ' ']
[' ', ' ', ' ', ' ', ' ']

```

```

Player X, enter row (0-2): 1
Player X, enter col (0-2): 1

```

```

Current Board:
[' ', ' ', ' ', ' ', ' ']
[' ', ' ', 'X', ' ', ' ']
[' ', ' ', ' ', ' ', ' ']

```

```

Player O, enter row (0-2): 0
Player O, enter col (0-2): 2

```

```

Current Board:
[' ', ' ', ' ', ' ', 'O']
[' ', ' ', 'X', ' ', ' ']
[' ', ' ', ' ', ' ', ' ']

```

```

Player X, enter row (0-2): 1
Player X, enter col (0-2): 0

```

```

Current Board:
[' ', ' ', 'O']
['X', 'X', ' ']
[' ', ' ', ' ']

Player O, enter row (0-2): 2
Player O, enter col (0-2): 1

Current Board:
[' ', ' ', 'O']
['X', 'X', ' ']
[' ', 'O', ' ']

Player X, enter row (0-2): 2
Player X, enter col (0-2): 2

Current Board:
[' ', ' ', 'O']
['X', 'X', ' ']
[' ', 'O', 'X']

Player O, enter row (0-2): 2
Player O, enter col (0-2): 0

Current Board:
[' ', ' ', 'O']
['X', 'X', ' ']
['O', 'O', 'X']

Player X, enter row (0-2): 0
Player X, enter col (0-2): 1

Current Board:
[' ', 'X', 'O']
['X', 'X', ' ']
['O', 'O', 'X']

Player O, enter row (0-2): 1
Player O, enter col (0-2): 2

Current Board:
[' ', 'X', 'O']
['X', 'X', 'O']
['O', 'O', 'X']

Player X, enter row (0-2): 0
Player X, enter col (0-2): 0

Current Board:
['X', 'X', 'O']
['X', 'X', 'O']
['O', 'O', 'X']

Player X wins!
Total moves (cost): 9

```

Output case2:

Tic-Tac-Toe Game (3x3 Matrix Format)

Current Board:

```
[' ', ' ', ' ', ' ', ' ']  
[' ', ' ', ' ', ' ', ' ']  
[' ', ' ', ' ', ' ', ' ']
```

Player X, enter row (0-2): 0

Player X, enter col (0-2): 2

Current Board:

```
[' ', ' ', ' ', 'X', ' ']  
[' ', ' ', ' ', ' ', ' ']  
[' ', ' ', ' ', ' ', ' ']
```

Player O, enter row (0-2): 2

Player O, enter col (0-2): 1

Current Board:

```
[' ', ' ', ' ', 'X', ' ']  
[' ', ' ', ' ', ' ', ' ']  
[' ', ' ', 'O', ' ', ' ']
```

Player X, enter row (0-2): 0

Player X, enter col (0-2): 0

Current Board:

```
['X', ' ', ' ', 'X', ' ']  
[' ', ' ', ' ', ' ', ' ']  
[' ', ' ', 'O', ' ', ' ']
```

Player O, enter row (0-2): 0

Player O, enter col (0-2): 1

Current Board:

```
['X', 'O', 'X', ' ', ' ']  
[' ', ' ', ' ', ' ', ' ']  
[' ', ' ', 'O', ' ', ' ']
```

Player X, enter row (0-2): 2

Player X, enter col (0-2): 0

Current Board:

```
['X', 'O', 'X', ' ', ' ']  
[' ', ' ', ' ', ' ', ' ']  
['X', 'O', ' ', ' ', ' ']
```

Player O, enter row (0-2): 1

Player O, enter col (0-2): 1

Current Board:

```
['X', 'O', 'X', ' ', ' ']  
[' ', ' ', 'O', ' ', ' ']  
['X', 'O', ' ', ' ', ' ']
```



```
['X', 'O', ' ']
```

Player O wins!

Total moves (cost): 6

Output case3:

Tic-Tac-Toe Game (3x3 Matrix Format):

Current Board:

```
[' ', ' ', ' ']  
[' ', ' ', ' ']  
[' ', ' ', ' ']
```

Player X, enter row (0-2): 1

Player X, enter col (0-2): 0

Current Board:

```
[' ', ' ', ' ']  
['X', ' ', ' ']  
[' ', ' ', ' ']
```

Player O, enter row (0-2): 0

Player O, enter col (0-2): 2

Current Board:

```
[' ', ' ', 'O']  
['X', ' ', ' ']  
[' ', ' ', ' ']
```

Player X, enter row (0-2): 2

Player X, enter col (0-2): 0

Current Board:

```
[' ', ' ', 'O']  
['X', ' ', ' ']  
['X', ' ', ' ']
```

Player O, enter row (0-2): 0

Player O, enter col (0-2): 0

Current Board:

```
['O', ' ', 'O']  
['X', ' ', ' ']  
['X', ' ', ' ']
```

Player X, enter row (0-2): 0

Player X, enter col (0-2): 1

Current Board:

```
['O', 'X', 'O']  
['X', ' ', ' ']  
['X', ' ', ' ']
```

Player O, enter row (0-2): 2

Player O, enter col (0-2): 1

```

Current Board:
['O', 'X', 'O']
['X', ' ', ' ']
['X', 'O', ' ']

Player X, enter row (0-2): 2
Player X, enter col (0-2): 2

Current Board:
['O', 'X', 'O']
['X', ' ', ' ']
['X', 'O', 'X']

Player O, enter row (0-2): 1
Player O, enter col (0-2): 1

Current Board:
['O', 'X', 'O']
['X', 'O', ' ']
['X', 'O', 'X']

Player X, enter row (0-2): 1
Player X, enter col (0-2): 2

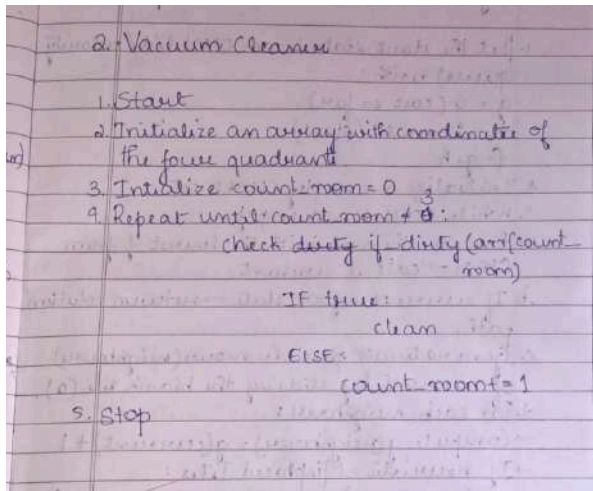
Current Board:
['O', 'X', 'O']
['X', 'O', 'X']
['X', 'O', 'X']

Game is a draw.
Total moves (cost): 9

```

Implement vacuum cleaner agent

Algorithm:



Code:

```
def vacuum_cleaner()
    A = int(input("Enter state of A (0 for clean, 1 for dirty): "))
    B = int(input("Enter state of B (0 for clean, 1 for dirty): "))
    location = input("Enter location (A or B): ").upper()

    cost = 0
    state = {'A': A, 'B': B}

    if location == 'A':
        if state['A'] == 1: # If A is dirty
            print("Cleaned A.")
            state['A'] = 0
            cost += 1
        else:
            print("A is clean")

    if state['B'] == 1: # If B is dirty
        print("Moving vacuum right")
        print("Cleaned B.")
        state['B'] = 0
        cost += 1
        print("Is B clean now? (0 if clean, 1 if dirty):", state['B'])
        print("Is A dirty? (0 if clean, 1 if dirty):", state['A'])
        print("B is clean")
        print("Moving vacuum left")
    else:
        print("Turning vacuum off")

    elif location == 'B':
        if state['B'] == 1: # If B is dirty
            print("Cleaned B.")
```

```

        state['B'] = 0
        cost += 1
    else:
        print("B is clean")

    if state['A'] == 1: # If A is dirty
        print("Moving vacuum left")
        print("Cleaned A.")
        state['A'] = 0
        cost += 1
        print("Is A clean now? (0 if clean, 1 if dirty):", state['A'])
        print("Is B dirty? (0 if clean, 1 if dirty):", state['B'])
        print("A is clean")
        print("Moving vacuum right")
    else:
        print("Turning vacuum off")

    print("Cost:", cost)
    print(state)

vacuum_cleaner()

```

OUTPUT Case1:

```

Enter state of A (0 for clean, 1 for dirty): 1
Enter state of B (0 for clean, 1 for dirty): 1
Enter location (A or B): A
Cleaned A.
Moving vacuum right
Cleaned B.
Is B clean now? (0 if clean, 1 if dirty): 0
Is A dirty? (0 if clean, 1 if dirty): 0
B is clean
Moving vacuum left
Cost: 2
{'A': 0, 'B': 0}

```

OUTPUT Case2:

```

Enter state of A (0 for clean, 1 for dirty): 0
Enter state of B (0 for clean, 1 for dirty): 1
Enter location (A or B): A
A is clean
Moving vacuum right
Cleaned B.
Is B clean now? (0 if clean, 1 if dirty): 0
Is A dirty? (0 if clean, 1 if dirty): 0
B is clean
Moving vacuum left
Cost: 1
{'A': 0, 'B': 0}

```

OUTPUT Case3:

```

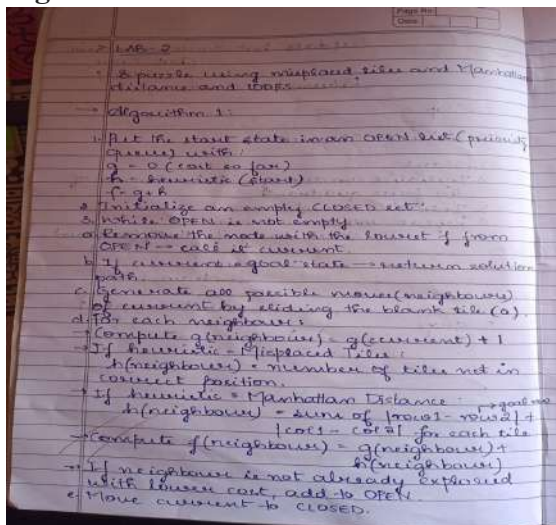
Enter state of A (0 for clean, 1 for dirty): 0
Enter state of B (0 for clean, 1 for dirty): 0
Enter location (A or B): A
A is clean
Turning vacuum off
Cost: 0
{'A': 0, 'B': 0}

```

Program2

Implement 8 puzzle problems using Depth First Search (DFS)

Algorithm:



Code:

```

def get_moves(state):
    idx = state.index("_")
    x, y = divmod(idx, 3)
    moves = []
    for dx, dy in [(-1,0),(1,0),(0,-1),(0,1)]:
        nx, ny = x+dx, y+dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            nidx = nx*3 + ny
            lst = list(state)
            lst[idx], lst[nidx] = lst[nidx], lst[idx]
            moves.append("".join(lst))
    return moves

def dfs(start, goal):
    stack = [(start, 0)]
    parent = {start: None}
    visited = {start}
    order = []

    while stack:
        state, cost = stack.pop()
        order.append(state)
        if state == goal:
            path = []
            while state:
                path.append(state)
                state = parent[state]
            path.reverse()
            return path, cost, order, visited
        for move in reversed(get_moves(state)):
            if move not in visited:
                visited.add(move)
                parent[move] = state
                stack.append((move, cost+1))
    return None, -1, order, visited

start = input("Enter initial state (e.g., 54_618732): ")
goal = input("Enter goal state (e.g., 12345678_): ")
path, cost, visited_order, visited_set = dfs(start, goal)

print("Visited nodes (till goal found):")
for v in visited_order:
    for i in range(0, 9, 3):
        print(v[i:i+3])
    print()
    if v == goal:
        break

print("Steps (solution path):")
for p in path:
    for i in range(0, 9, 3):

```

```

    print(p[i:i+3])
    print()

print("Cost (depth to goal):", cost)
print("Number of nodes visited:", len(visited_set))

```

Output:

```

Steps (solution path):
283
164
7_5

283
1_4
765

2_3
184
765

_23
184
765

123
_84
765

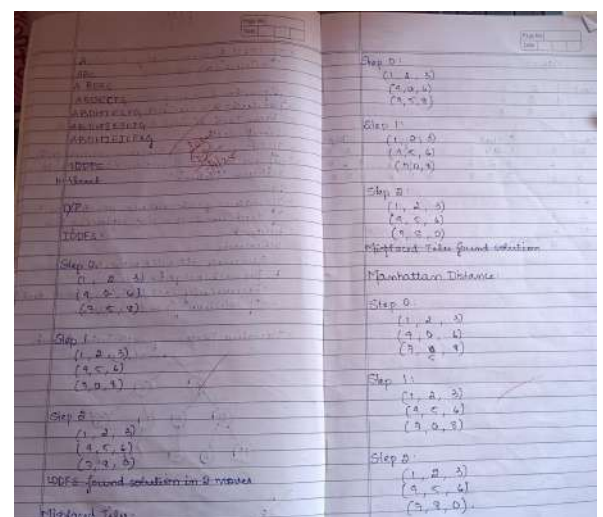
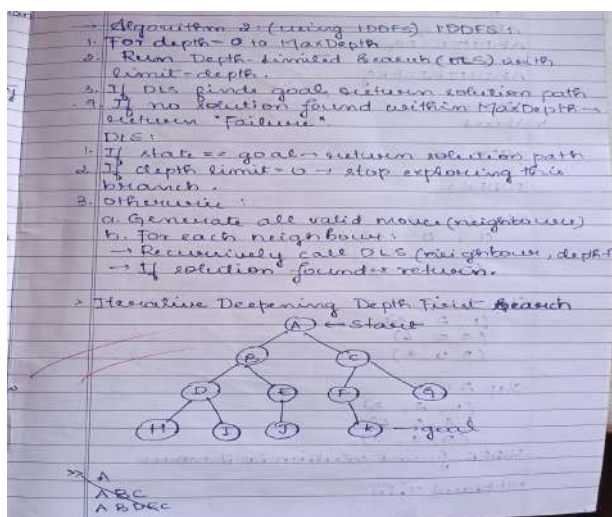
123
8_4
765

Cost (depth to goal): 5
Number of nodes visited: 181440

```

Implement Iterative deepening search algorithm

Algorithm:



Code:

```

def get_neighbors(state):
    neighbors = []
    idx = state.index("0")

```

```

moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]
x, y = divmod(idx, 3)

for dx, dy in moves:
    nx, ny = x + dx, y + dy
    if 0 <= nx < 3 and 0 <= ny < 3:
        new_idx = nx * 3 + ny
        state_list = list(state)
        state_list[idx], state_list[new_idx] = state_list[new_idx], state_list[idx]
        neighbors.append("".join(state_list))
return neighbors

def dfs_limit(start_state, goal_state, limit):
    stack = [(start_state, 0)]
    visited = set()
    parent = {start_state: None}
    path = []

    while stack:
        current_state, depth = stack.pop()

        if current_state == goal_state:
            while current_state:
                path.append(current_state)
                current_state = parent[current_state]
            return path[::-1]

        if depth < limit and current_state not in visited:
            visited.add(current_state)
            neighbors = get_neighbors(current_state)
            neighbors.reverse() # Maintain consistent exploration order
            for neighbor in neighbors:
                if neighbor not in visited:
                    parent[neighbor] = current_state
                    stack.append((neighbor, depth + 1))
    return None

def iddfs(start_state, goal_state, max_depth):
    for limit in range(max_depth + 1):
        print(f'Searching with depth limit: {limit}')
        solution = dfs_limit(start_state, goal_state, limit)
        if solution:
            return solution
    return None

print("Enter the initial state (enter 3 digits per row, separated by spaces, 0 for empty):")
initial_state_rows = []
for i in range(3):
    row = input(f'Row {i+1}: ').split()
    initial_state_rows.extend(row)
initial_state = "".join(initial_state_rows)

```



```

print("\nEnter the goal state (enter 3 digits per row, separated by spaces, 0 for empty):")
goal_state_rows = []
for i in range(3):
    row = input(f"Row {i+1}: ").split()
    goal_state_rows.extend(row)
goal_state = "".join(goal_state_rows)

max_depth = 50

solution = iddfs(initial_state, goal_state, max_depth)

if solution:
    print("\nIDDFS solution path:")
    for s in solution:
        print(s[:3])
        print(s[3:6])
        print(s[6:])
        print()
else:
    print(f"\nNo solution found within the maximum depth of {max_depth}.")

```

Output:

```

Sharada Koundinya 18M23CS310
Enter the initial state (enter 3 digits per row, separated by spaces, 0 for empty):
Row 1: 283
Row 2: 164
Row 3: 705

Enter the goal state (enter 3 digits per row, separated by spaces, 0 for empty):
Row 1: 123
Row 2: 084
Row 3: 765
Searching with depth limit: 0
Searching with depth limit: 1
Searching with depth limit: 2
Searching with depth limit: 3
Searching with depth limit: 4
Searching with depth limit: 5

IDDFS solution path:
283
164
705

283
104
765

203
184
765

023
184
765

123
084
765

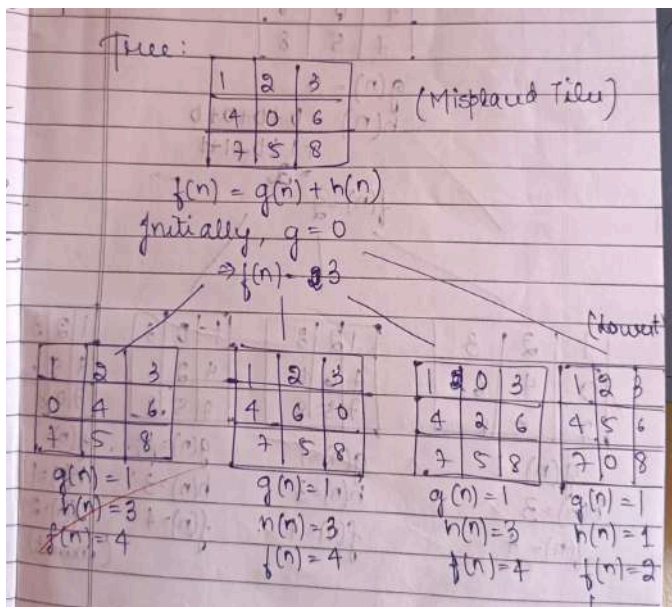
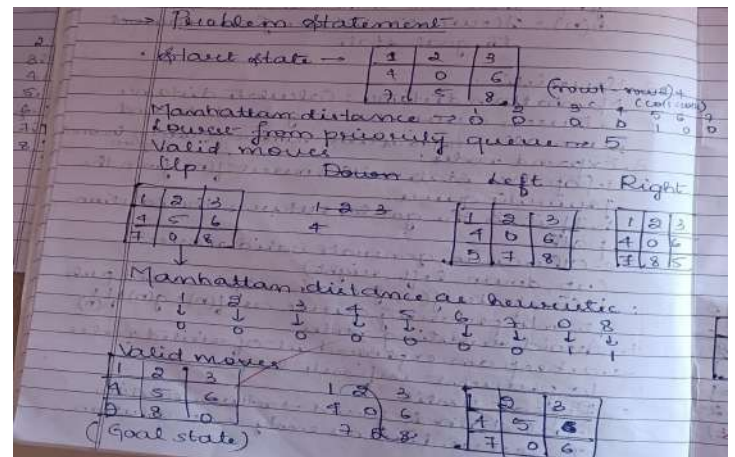
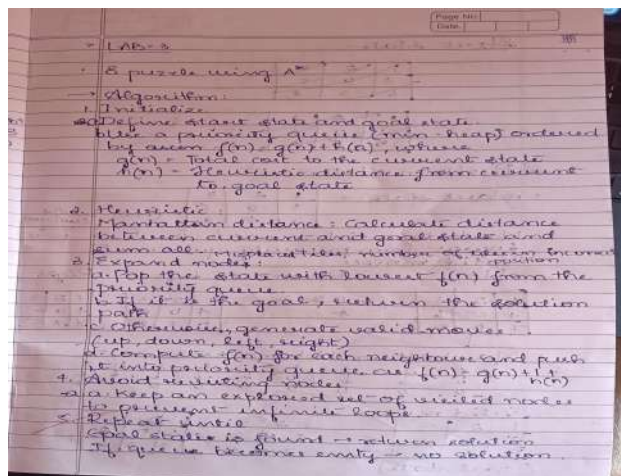
123
804
765

```

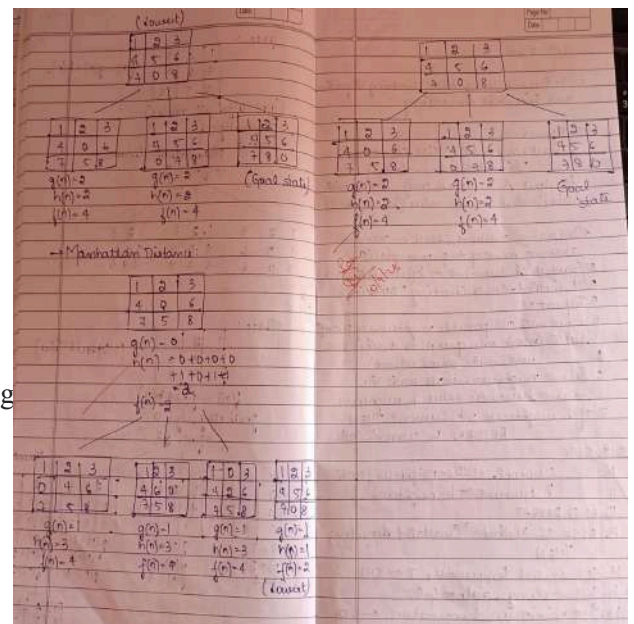
Program3

Implement A* search algorithm

Algorithm:



cluding



return misplaced

```
def find_blank(board):
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] == 0:
                return i, j
    raise ValueError("Board does not contain a blank tile (0)")
```

```
def neighbors(board):
    """Generate neighboring boards by sliding one tile into the blank."""
    n = len(board)
    x, y = find_blank(board)
    dirs = [(0,1),(0,-1),(1,0),(-1,0)]
    res = []
    for dx, dy in dirs:
```

```

        nx, ny = x + dx, y + dy
        if 0 <= nx < n and 0 <= ny < n:
            b = [list(row) for row in board]
            b[x][y], b[nx][ny] = b[nx][ny], b[x][y]
            res.append(tuple(tuple(row) for row in b))
    return res

def flatten(board):
    return [x for row in board for x in row]

def inversion_count(seq):
    arr = [x for x in seq if x != 0]
    inv = 0
    for i in range(len(arr)):
        for j in range(i+1, len(arr)):
            if arr[i] > arr[j]:
                inv += 1
    return inv

def blank_row_from_bottom(board):
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] == 0:
                return n - i
    raise ValueError("Board does not contain a blank tile (0)")

def is_solvable(start, goal):
    """General n-puzzle solvability test (odd/even width)."""
    n = len(start)
    start_flat = flatten(start)
    goal_flat = flatten(goal)

    pos = {val: idx for idx, val in enumerate(goal_flat)}
    start_perm = [pos[val] for val in start_flat]

    inv = inversion_count(start_perm)

    if n % 2 == 1:
        # odd grid: inversions parity must be even
        return inv % 2 == 0
    else:
        # even grid: blank row from bottom parity matters
        blank_row = blank_row_from_bottom(start)
        goal_blank_row = blank_row_from_bottom(goal)
        # When using relative permutation to goal, parity of blank rows must match
        return (inv + blank_row) % 2 == (0 + goal_blank_row) % 2

def reconstruct_path(came_from, current):
    path = [current]
    while current in came_from:
        current = came_from[current]

```

```

    path.append(current)
    path.reverse()
    return path

def a_star_misplaced(start, goal):
    start = tuple(tuple(row) for row in start)
    goal = tuple(tuple(row) for row in goal)

    if len(start) != len(start[0]) or len(goal) != len(goal[0]) or len(start) != len(goal):
        raise ValueError("Initial and goal must be square boards of the same size.")

    start_vals = sorted(flatten(start))
    goal_vals = sorted(flatten(goal))
    if start_vals != goal_vals:
        raise ValueError("Initial and goal must contain the same set of tiles.")

    if not is_solvable(start, goal):
        return None, None, 0, 0 # unsolvable

    counter = count() # tie-breaker

    h0 = misplaced_heuristic(start, goal)
    g_score = {start: 0}
    f0 = h0

    open_heap = [(f0, next(counter), start)]
    open_set = {start: f0}
    closed = set()
    came_from = {}

    expansions = 0

    while open_heap:
        _, _, current = heapq.heappop(open_heap)
        if current in closed:
            continue
        closed.add(current)

        if current == goal:
            path = reconstruct_path(came_from, current)
            return path, g_score[current], expansions, len(closed)

        expansions += 1

    for nb in neighbors(current):
        tentative_g = g_score[current] + 1
        if nb in closed:
            continue
        if nb not in g_score or tentative_g < g_score[nb]:
            came_from[nb] = current
            g_score[nb] = tentative_g
            h = misplaced_heuristic(nb, goal)

```

```

        f = tentative_g + h
        if nb not in open_set or f < open_set[nb]:
            heapq.heappush(open_heap, (f, next(counter), nb))
            open_set[nb] = f

    return None, None, expansions, len(closed)

def read_board(n, prompt):
    print(prompt)
    board = []
    for i in range(n):
        row = list(map(int, input().split()))
        if len(row) != n:
            raise ValueError(f"Row {i+1} must contain exactly {n} integers.")
        board.append(row)
    return board

def print_board(board):
    for row in board:
        print(" ".join(f"{x}" for x in row))

def main():
    try:
        n = int(input("Enter puzzle size n (e.g., 3 for 3x3): ").strip())
        initial = read_board(n, "Enter initial state row by row (use 0 for blank):")
        goal = read_board(n, "Enter goal state row by row (use 0 for blank):")

        result = a_star_misplaced(initial, goal)
        path, cost, expansions, explored = result

        if path is None:
            print("No solution (unsolvable with given start/goal).")
            return

        print("\nSolution path (each state shows g, h, f):\n")
        for idx, state in enumerate(path):
            g = idx # each step costs 1
            h = misplaced_heuristic(state, tuple(tuple(r) for r in goal))
            f = g + h
            print(f"Step {idx}: g={g}, h={h}, f={f}")
            print_board(state)
            print()

        print(f"Total cost (number of moves): {cost}")
        print(f"Nodes expanded: {expansions}")
        print(f"Nodes explored (unique): {explored}")

    except Exception as e:
        print("Error:", e)

if __name__ == "__main__":
    main()

```

Output:

```
Enter puzzle size n (e.g., 3 for 3x3): 3
Enter initial state row by row (use 0 for blank):
2 8 3
1 6 4
7 0 5
Enter goal state row by row (use 0 for blank):
1 2 3
8 0 4
7 6 5

solution path (each state shows g, h, f):

Step 0: g=0, h=4, f=4
2 8 3
1 6 4
7 0 5

Step 1: g=1, h=3, f=4
2 8 3
1 0 4
7 6 5

Step 2: g=2, h=3, f=5
2 0 3
1 8 4
7 6 5

Step 3: g=3, h=2, f=5
0 2 3
1 8 4
7 6 5

Step 4: g=4, h=1, f=5
1 2 3
0 8 4
7 6 5

Step 5: g=5, h=0, f=5
1 2 3
8 0 4
7 6 5

Total cost (number of moves): 5
Nodes expanded: 6
Nodes explored (unique): 7
```

Code:

```
#MANHATTAN DISTANCE
```

```
import heapq
```

```
from itertools import count
```

```
def misplaced_heuristic(board, goal):
    misplaced = 0
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] != 0 and board[i][j] != goal[i][j]:
                misplaced += 1
    return misplaced
```

```
def manhattan_heuristic(board, goal):
    n = len(board)
    # Map goal positions for each tile
    goal_pos = {}
    for i in range(n):
        for j in range(n):
            goal_pos[goal[i][j]] = (i, j)
```

```
    dist = 0
    for i in range(n):
        for j in range(n):
            val = board[i][j]
            if val != 0:
                gi, gj = goal_pos[val]
```

```

        dist += abs(i - gi) + abs(j - gj)
    return dist

def find_blank(board):
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] == 0:
                return i, j
    raise ValueError("Board does not contain a blank tile (0)")

def neighbors(board):
    n = len(board)
    x, y = find_blank(board)
    dirs = [(0,1),(0,-1),(1,0),(-1,0)]
    res = []
    for dx, dy in dirs:
        nx, ny = x + dx, y + dy
        if 0 <= nx < n and 0 <= ny < n:
            b = [list(row) for row in board]
            b[x][y], b[nx][ny] = b[nx][ny], b[x][y]
            res.append(tuple(tuple(row) for row in b))
    return res

def flatten(board):
    return [x for row in board for x in row]

def inversion_count(seq):
    arr = [x for x in seq if x != 0]
    inv = 0
    for i in range(len(arr)):
        for j in range(i+1, len(arr)):
            if arr[i] > arr[j]:
                inv += 1
    return inv

def blank_row_from_bottom(board):
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] == 0:
                return n - i
    raise ValueError("Board does not contain a blank tile (0)")

def is_solvable(start, goal):
    n = len(start)
    start_flat = flatten(start)
    goal_flat = flatten(goal)

    pos = {val: idx for idx, val in enumerate(goal_flat)}
    start_perm = [pos[val] for val in start_flat]

```

```

inv = inversion_count(start_perm)

if n % 2 == 1:
    return inv % 2 == 0
else:
    blank_row = blank_row_from_bottom(start)
    goal_blank_row = blank_row_from_bottom(goal)
    return (inv + blank_row) % 2 == (0 + goal_blank_row) % 2

def reconstruct_path(came_from, current):
    path = [current]
    while current in came_from:
        current = came_from[current]
        path.append(current)
    path.reverse()
    return path

def a_star_manhattan(start, goal):
    start = tuple(tuple(row) for row in start)
    goal = tuple(tuple(row) for row in goal)

    if len(start) != len(start[0]) or len(goal) != len(goal[0]) or len(start) != len(goal):
        raise ValueError("Initial and goal must be square boards of the same size.")

    start_vals = sorted(flatten(start))
    goal_vals = sorted(flatten(goal))
    if start_vals != goal_vals:
        raise ValueError("Initial and goal must contain the same set of tiles.")

    if not is_solvable(start, goal):
        return None, None, 0, 0

    counter = count()
    h0 = manhattan_heuristic(start, goal)
    g_score = {start: 0}
    f0 = h0

    open_heap = [(f0, next(counter), start)]
    open_set = {start: f0}
    closed = set()
    came_from = {}

    expansions = 0

    while open_heap:
        _, _, current = heapq.heappop(open_heap)
        if current in closed:
            continue
        closed.add(current)

        if current == goal:
            path = reconstruct_path(came_from, current)

```



```

        return path, g_score[current], expansions, len(closed)

    expansions += 1

    for nb in neighbors(current):
        tentative_g = g_score[current] + 1
        if nb in closed:
            continue
        if nb not in g_score or tentative_g < g_score[nb]:
            came_from[nb] = current
            g_score[nb] = tentative_g
            h = manhattan_heuristic(nb, goal)
            f = tentative_g + h
            if nb not in open_set or f < open_set[nb]:
                heapq.heappush(open_heap, (f, next(counter), nb))
                open_set[nb] = f

    return None, None, expansions, len(closed)

def read_board(n, prompt):
    print(prompt)
    board = []
    for i in range(n):
        row = list(map(int, input().split()))
        if len(row) != n:
            raise ValueError(f"Row {i+1} must contain exactly {n} integers.")
        board.append(row)
    return board

def print_board(board):
    for row in board:
        print(" ".join(f"{x}" for x in row))

def main():
    try:
        n = int(input("Enter puzzle size n (e.g., 3 for 3x3): ").strip())
        initial = read_board(n, "Enter initial state row by row (use 0 for blank):")
        goal = read_board(n, "Enter goal state row by row (use 0 for blank):")

        result = a_star_manhattan(initial, goal)
        path, cost, expansions, explored = result

        if path is None:
            print("No solution (unsolvable with given start/goal).")
            return

        print("\nSolution path (each state shows g, h, f):\n")
        for idx, state in enumerate(path):
            g = idx
            h = manhattan_heuristic(state, tuple(tuple(r) for r in goal))
            f = g + h
            print(f"Step {idx}: g={g}, h={h}, f={f}")
    
```

```

        print_board(state)
        print()

    print(f"Total cost (number of moves): {cost}")
    print(f"Nodes expanded: {expansions}")
    print(f"Nodes explored (unique): {explored}")

except Exception as e:
    print("Error:", e)

if __name__ == "__main__":
    main()

```

Output:

```

Enter puzzle size n (e.g., 3 for 3x3): 3
Enter initial state row by row (use 0 for blank):
2 8 3
1 6 4
7 0 5
Enter goal state row by row (use 0 for blank):
1 2 3
8 0 4
7 6 5

Solution path (each state shows g, h, f):

Step 0: g=0, h=5, f=5
2 8 3
1 6 4
7 0 5

Step 1: g=1, h=4, f=5
2 8 3
1 0 4
7 6 5

Step 2: g=2, h=3, f=5
2 0 3
1 8 4
7 6 5

Step 3: g=3, h=2, f=5
0 2 3
1 8 4
7 6 5

Step 4: g=4, h=1, f=5
1 2 3
0 0 4
7 6 5

Step 5: g=5, h=0, f=5
1 2 3
8 0 4
7 6 5

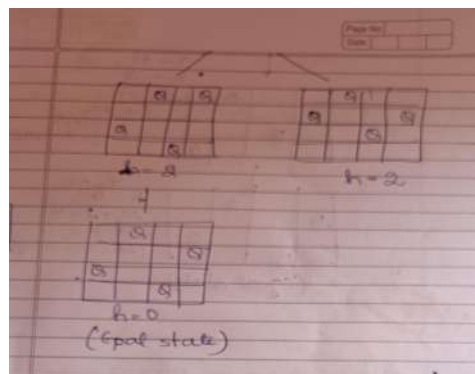
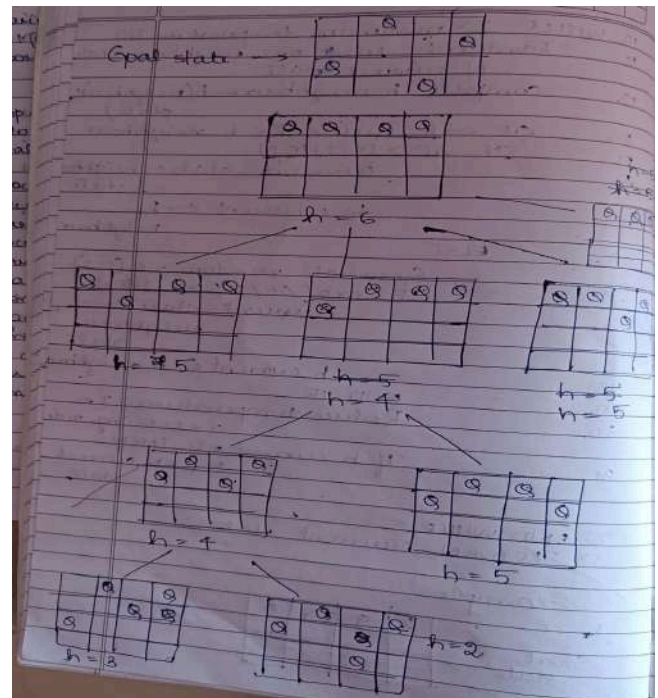
Total cost (number of moves): 5
Nodes expanded: 5
Nodes explored (unique): 6

```

Program4

Implement Hill Climbing search algorithm to solve N-Queens problem

Algorithm:



Code:

```
def calculate_cost(state):
    cost = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                cost += 1
    return cost
```

```
def generate_neighbors(state):
    neighbors = []
    n = len(state)
    for col in range(n):
```

```

        for row in range(n):
            if state[col] != row: # move queen
                new_state = list(state)
                new_state[col] = row
                neighbors.append(new_state)
    return neighbors

def hill_climbing(initial_state):
    current = initial_state
    current_cost = calculate_cost(current)
    step = 0

    print(f"Step {step}: State = {current}, Cost = {current_cost}")

    while True:
        neighbors = generate_neighbors(current)
        neighbor_costs = [(n, calculate_cost(n)) for n in neighbors]

        # Print state space for this step
        print("\nNeighbors and their costs:")
        for n, c in neighbor_costs:
            print(f"    {n} -> Cost = {c}")

        # Pick the best neighbor (lowest cost)
        best_neighbor, best_cost = min(neighbor_costs, key=lambda x: x[1])

        if best_cost >= current_cost:
            break

        step += 1
        current, current_cost = best_neighbor, best_cost
        print(f"\nStep {step}: Move to {current}, Cost = {current_cost}")

        if current_cost == 0:
            print("\nGoal reached! Solution found.")
            break

initial_state = [3, 1, 2, 0]

hill_climbing(initial_state)

]
```

Output:



Week 7

Step 0: State = [3, 1, 2, 0], Cost = 2

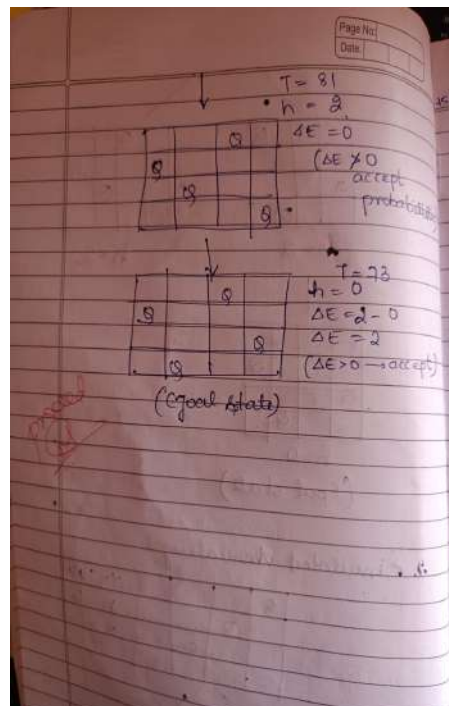
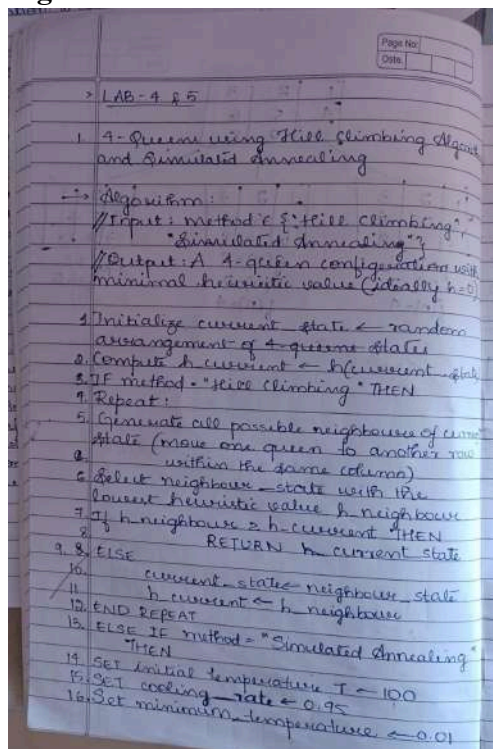
Neighbors and their costs:

[0, 1, 2, 0] → Cost = 4
[1, 1, 2, 0] → Cost = 2
[2, 1, 2, 0] → Cost = 3
[3, 0, 2, 0] → Cost = 2
[3, 2, 2, 0] → Cost = 4
[3, 3, 2, 0] → Cost = 3
[3, 1, 0, 0] → Cost = 3
[3, 1, 1, 0] → Cost = 4
[3, 1, 3, 0] → Cost = 2
[3, 1, 2, 1] → Cost = 3
[3, 1, 2, 2] → Cost = 2
[3, 1, 2, 3] → Cost = 4

Program 5

Simulated Annealing to Solve 8-Queens problem

Algorithm:



Code:

```
import random
import math
```

```

def calculate_cost(state):
    cost = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                cost += 1
    return cost

def get_random_neighbor(state):
    n = len(state)
    new_state = list(state)
    col = random.randint(0, n - 1)
    row = random.randint(0, n - 1)
    new_state[col] = row
    return new_state

def simulated_annealing(n=8, max_iterations=10000, initial_temp=100.0, cooling_rate=0.99):

    current = [random.randint(0, n - 1) for _ in range(n)]
    current_cost = calculate_cost(current)
    best = current
    best_cost = current_cost
    temperature = initial_temp

    for _ in range(max_iterations):
        if current_cost == 0:
            break

        neighbor = get_random_neighbor(current)
        neighbor_cost = calculate_cost(neighbor)
        delta = neighbor_cost - current_cost

        if delta < 0 or random.random() < math.exp(-delta / temperature):
            current, current_cost = neighbor, neighbor_cost

            if current_cost < best_cost:
                best, best_cost = current, current_cost

        temperature *= cooling_rate
        if temperature < 1e-6:
            break

    return best, best_cost

best_state, best_cost = simulated_annealing()

print("The best position found:", best_state)
print("cost =", best_cost)

```

Output:

```

↔ The best position found: [5, 2, 6, 1, 7, 4, 0, 3]
cost = 0

```

Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Algorithm:

LAB 09/08/2020

a. $Q \rightarrow P$
 $P \rightarrow Q$
 $S \vee R$

P	Q	R	$Q \rightarrow P$	$P \rightarrow Q$	$Q \vee R$	KB True
T	T	T	T	T	T	F (False)
T	T	F	T	T	F	F (False)
T	F	T	T	T	T	F
T	F	F	T	T	F	F ($Q \vee R$)
F	T	T	F	T	T	F ($Q \rightarrow P$)
F	T	F	F	T	T	F
F	F	T	T	T	T	T
F	F	F	T	T	F	F ($Q \vee R$)

i) KB is true in the following model:

P	Q	R
T	F	T
F	F	T

Models of KB (where all three sentences are true) are:

- $(P=T, Q=F, R=T)$
- $(P=F, Q=F, R=T)$

ii) $KB \models R$?

From above, both models where KB is

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True have $R=T$ in all models where KB is true.

iii) $KB \models R \rightarrow P$?

P	Q	R	$R \rightarrow P$
T	T	T	T
T	T	F	T
T	F	T	T
T	F	F	T
F	T	T	T
F	T	F	T
F	F	T	T
F	F	F	T

In second model, $R \rightarrow P = F$, while $KB = \text{True}$ so $KB \not\models (R \rightarrow P)$

iv) $KB \models (R \rightarrow P)$? $KB \models (Q \rightarrow R)$?

P	Q	R	$Q \rightarrow R$
T	T	T	T
T	T	F	F
T	F	T	T
T	F	F	T
F	T	T	T
F	T	F	T
F	F	T	T
F	F	F	T

$\Rightarrow Q \rightarrow R$ is true in all models where KB is true.

$\Rightarrow KB \models (Q \rightarrow R)$

Output

Code:

```

import itertools

def eval_expr(expr, model):
    try:
        return eval(expr, {}, model)
    except:
        return False

def tt_entails(KB, query):
    symbols = sorted(set([ch for ch in KB + query if ch.isalpha()])))

    print("\nTruth Table:")
    print(" | ".join(symbols) + " | KB | Query")
    print("-" * (6 * len(symbols) + 20))

    entails = True
    for values in itertools.product([False, True], repeat=len(symbols)):
        model = dict(zip(symbols, values))

```

```

kb_val = eval_expr(KB, model)
query_val = eval_expr(query, model)

row = " | ".join(["T" if model[s] else "F" for s in symbols])
print(f"{row} | {kb_val} | {query_val}")

if kb_val and not query_val:
    entails = False

return entails

KB = input("Enter Knowledge Base (use &, |, ~ for AND, OR, NOT): ")
query = input("Enter Query: ")

result = tt_entails(KB, query)

print("\nResult:")
if result:
    print("KB entails Query (True in all cases).")
else:
    print("KB does NOT entail Query.")

```

Output:

```

Enter Knowledge Base (use &, |, ~ for AND, OR, NOT): (A|C)&(B|~C)
Enter Query: A|B

Truth Table:
A | B | C | KB | Query
-----
F | F | F | 0 | False
F | F | T | 0 | False
F | T | F | 0 | True
F | T | T | 1 | True
T | F | F | 1 | True
T | F | T | 0 | True
T | T | F | 1 | True
T | T | T | 1 | True

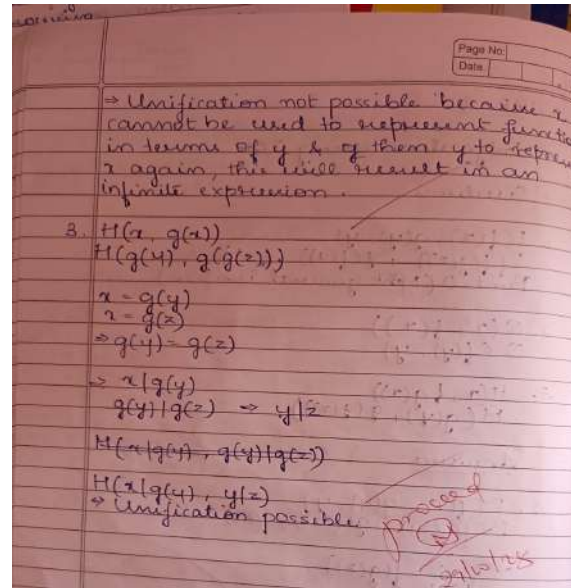
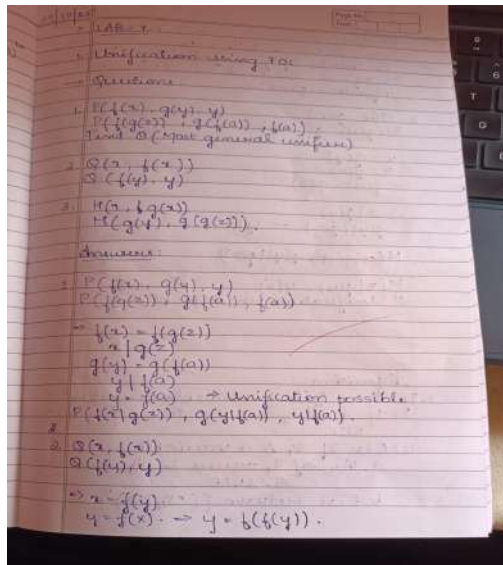
Result:
KB entails Query (True in all cases).

```


Program 7

Implement unification in first order logic

Algorithm:



Code:

```
def occurs_check(var, term, subst):
    if var == term:
        return True
    elif isinstance(term, tuple):
        return any(occurs_check(var, t, subst) for t in term)
    elif term in subst:
        return occurs_check(var, subst[term], subst)
    return False

def unify(x, y, subst):
    if subst is None:
        return None
    elif x == y:
        return subst
    elif isinstance(x, str) and x.isupper():
        return unify_var(x, y, subst)
    elif isinstance(y, str) and y.isupper():
        return unify_var(y, x, subst)
    elif isinstance(x, tuple) and isinstance(y, tuple):
        if x[0] != y[0] or len(x) != len(y):
            return None
        for a, b in zip(x[1:], y[1:]):
            subst = unify(a, b, subst)
            if subst is None:
                return None
        return subst
```

```

else:
    return None

def unify_var(var, x, subst):
    if var in subst:
        return unify(subst[var], x, subst)
    elif x in subst:
        return unify(var, subst[x], subst)
    elif occurs_check(var, x, subst):
        return None
    else:
        subst[var] = x
        return subst

def parse_expr(s):
    s = s.replace(" ", "")
    if '(' not in s:
        return s
    name_end = s.index('(')
    name = s[:name_end]
    args = []
    depth = 0
    current = ""
    for c in s[name_end+1:-1]:
        if c == ',' and depth == 0:
            args.append(parse_expr(current))
            current = ""
        else:
            if c == '(':
                depth += 1
            elif c == ')':
                depth -= 1
            current += c
    if current:
        args.append(parse_expr(current))
    return tuple([name] + args)

def expr_to_str(expr):
    if isinstance(expr, tuple):
        return expr[0] + "(" + ",".join(expr_to_str(e) for e in expr[1:]) + ")"
    else:
        return expr

expr1_input = input("Enter first expression: ")
expr2_input = input("Enter second expression: ")

expr1 = parse_expr(expr1_input)
expr2 = parse_expr(expr2_input)

subst = unify(expr1, expr2, {})

if subst:

```

```

    formatted_subst = {var: expr_to_str(val) for var, val in subst.items()}
else:
    formatted_subst = None

print("Most General Unifier (MGU):", formatted_subst)

```

Output:

```

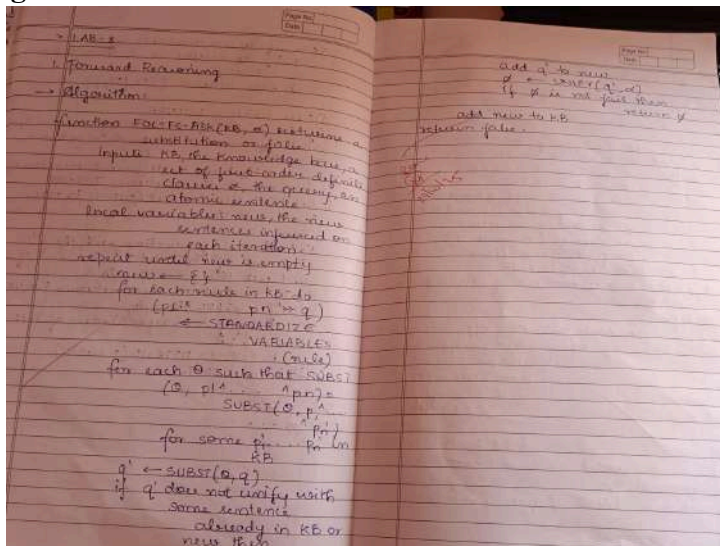
➡ Enter first expression: p(b,X,f(g(Z)))
Enter second expression: p(Z,f(Y),f(Y))
Most General Unifier (MGU): {'Z': 'b', 'X': 'f(Y)', 'Y': 'g(Z)'}

```

Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

Algorithm:



Code:

```

facts = {
    'American(Robert)': True,
    'Hostile(A)': True,
    'Sells_Weapons(Robert, A)': True
}

```

If American(X) and Hostile(Y) and Sells_Weapons(X, Y), then Crime(X)
def forward_reasoning(facts):

```

If American(X) and Hostile(Y) and Sells_Weapons(X, Y), then Crime(X)
    if facts.get('American(Robert)', False) and facts.get('Hostile(A)', False) and
facts.get('Sells_Weapons(Robert, A)', False):
    facts['Crime(Robert)'] = True

```

```

forward_reasoning(facts)

```

```

if facts.get('Crime(Robert)', False):
    print("Robert is a criminal.")
else:
    print("Robert is not a criminal.")

```

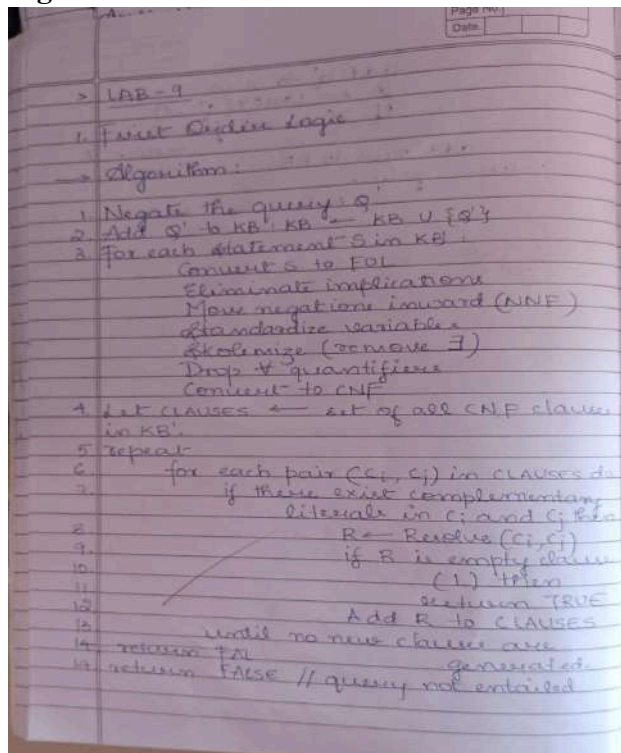
Output:

Robert is a criminal.

Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using resolution.

Algorithm:



Code:

```

from itertools import combinations

```

```

def get_literals(clause):

```

```

"""Split a clause into literals (handles OR operator)."""
return [literal.strip() for literal in clause.split("OR")]

def negate_literal(literal):
    """Return the negation of a literal."""
    literal = literal.strip()
    if literal.startswith("~"):
        return literal[1:]
    else:
        return "~" + literal

def resolve(ci, cj):
    """Try to resolve two clauses and return resolvents."""
    resolvents = set()
    lits_i = get_literals(ci)
    lits_j = get_literals(cj)

    for li in lits_i:
        for lj in lits_j:
            if li == negate_literal(lj):
                new_clause = set(lits_i + lits_j)
                new_clause.discard(li)
                new_clause.discard(lj)
                if not new_clause:
                    resolvents.add("NIL")
                else:
                    resolvents.add(" OR ".join(sorted(new_clause)))
    return resolvents

def resolution_algorithm(kb, query):
    print("\n===== RESOLUTION IN FIRST ORDER LOGIC =====\n")

    # Negate the query and add it to KB
    negated_query = negate_literal(query)
    print(f"Original Query    : {query}")
    print(f"Negated Query     : {negated_query}")
    clauses = kb + [negated_query]
    print("\nInitial Knowledge Base:")
    for i, c in enumerate(clauses, 1):
        print(f" Clause {i}: {c}")

    print("\n===== Resolution Steps =====\n")
    new = set()
    step = 1
    while True:
        pairs = list(combinations(clauses, 2))

```

```

    for (ci, cj) in pairs:
        resolvents = resolve(ci, cj)
        for res in resolvents:
            if res == "NIL":
                print(f'Step {step}: Resolving [{ci}] and [{cj}] gives NIL  $\Rightarrow$  Contradiction found!')
                print("\n✅ Query is PROVED by Resolution.\n")
                return True
            if res not in clauses and res not in new:
                print(f'Step {step}: Resolving [{ci}] and [{cj}]  $\Rightarrow$  New clause: {res}')
                new.add(res)
                step += 1
            if new.issubset(set(clauses)):
                print("\n❌ No new clauses can be generated.")
                print("Query CANNOT be proved by Resolution.\n")
                return False
        for c in new:
            if c not in clauses:
                clauses.append(c)

# -----
# Main Program (User Input)
# -----

if __name__ == "__main__":
    print("=== Resolution in First Order Logic (Simplified) ===")
    n = int(input("Enter number of clauses in Knowledge Base: "))
    kb = []
    for i in range(n):
        clause = input(f"Enter clause {i+1}: ").strip()
        kb.append(clause)

    query = input("Enter the query to prove: ").strip()

    # Run Resolution Algorithm
    resolution_algorithm(kb, query)

```

Output:

```

===== RESTART: C:/Users/BMSCESE/Desktop/Lab-9.py =====
--- Resolution in First Order Logic (Simplified) ---
Enter number of clauses in Knowledge Base: 4
Enter clause 1: P OR Q
Enter clause 2: ~Q OR R
Enter clause 3: ~R
Enter clause 4: ~P
Enter the query to prove: R
===== RESOLUTION IN FIRST ORDER LOGIC =====
Original Query      : R
Negated Query       : ~R

Initial Knowledge Base:
  Clause 1: P OR Q
  Clause 2: ~Q OR R
  Clause 3: ~R
  Clause 4: ~P
  Clause 5: ~R

===== Resolution Steps =====
Step 1: Resolving [P OR Q] and [~Q OR R]  $\Rightarrow$  New clause: P OR R
Step 2: Resolving [P OR R] and [~R]  $\Rightarrow$  New clause: P
Step 3: Resolving [~Q OR R] and [~R]  $\Rightarrow$  New clause: ~Q
Step 4: Resolving [P OR Q] and [~Q]  $\Rightarrow$  New clause: P
Step 5: Resolving [~Q OR R] and [Q]  $\Rightarrow$  New clause: R
Step 6: Resolving [Q] and [~Q] gives NIL  $\Rightarrow$  Contradiction Found!
✅ Query is PROVED by Resolution.

```

Program 10

Implement Alpha-Beta Pruning

Algorithm:

Handwritten pseudocode for the Alpha-Beta Pruning algorithm:

```

> LAB-10
1. Alpha-Beta Pruning algorithm
2. Pseudocode
Function ALPHA-BETA-SEARCH(state)
    return an action
    v ← MAX-VALUE(state, -∞, ∞)
    return the action in
    ACTIONS(state) with
    value v
Function MAX-VALUE(state, α, β) return
    a utility value
    if TERMINAL-TEST(state) then
        return
        UTILITY(state)
    v ← -∞
    for each a in ACTIONS(state) do
        v ← max(v, MIN-VALUE
        (RESULT(s, a),
        α, β))
        if v ≥ β then return v
        α ← MAX(α, v)
    return v
Function MIN-VALUE(state, α, β) return
    a utility value
    if TERMINAL-TEST(state) then
        return UTILITY(state)
    v ← +∞

```

Handwritten output and leaf node values:

Output:

- Enter number of leaf nodes: 8
- Enter values for leaf nodes[0] : 3
- Enter values for leaf nodes[1] : 5
- Enter values for leaf nodes[2] : 6
- Enter values for leaf nodes[3] : 9
- Enter values for leaf nodes[4] : 1
- Enter values for leaf nodes[5] : 2
- Enter values for leaf nodes[6] : 10
- Enter values for leaf nodes[7] : 1

Leaf nodes: (3, 5, 6, 9, 1, 2, 10, 1)

Optimal value (Best for Maximizer): 5

Leaf node (3) is selected.

Code:

```
import math
```

Recursive function for Alpha-Beta Pruning

```
def alpha_beta_pruning(depth, node_index, is_maximizing, values, alpha, beta, max_depth):
```

```
    indent = " " * depth # for visual indentation
```

```
    if depth == max_depth:
```

```
        print(f'{indent}Reached leaf node[{node_index}] = {values[node_index]}')
```

```
        return values[node_index]
```

```
    if is_maximizing:
```

```
        best = -math.inf
```

```
        print(f'{indent}Maximizer at depth {depth}, Alpha={alpha}, Beta={beta}')
```

```
        for i in range(2): # each node has 2 children
```

```
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, False, values, alpha, beta,
```

```
max_depth)
```

```
            best = max(best, val)
```

```
            alpha = max(alpha, best)
```

```
            print(f'{indent}Max node[{node_index}] updated Best={best}, Alpha={alpha},
```

```
Beta={beta}')
```

```
            if beta <= alpha:
```

```
                print(f'{indent}-- Pruning remaining branches at Max node[{node_index}] (Beta <=
```

```
Alpha) --')
```

```
                break
```

```
            return best
```

```
    else: # Minimizer's turn
```

```

        best = math.inf
        print(f' {indent}Minimizer at depth {depth}, Alpha={alpha}, Beta={beta}')
        for i in range(2):
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, True, values, alpha, beta,
max_depth)
            best = min(best, val)
            beta = min(beta, best)
            print(f' {indent}Min node[{node_index}] updated Best={best}, Alpha={alpha},
Beta={beta}')
            if beta <= alpha:
                print(f' {indent}-- Pruning remaining branches at Min node[{node_index}] (Beta <=
Alpha) --")
                break
        return best

# -----
# Main Program
# -----
if __name__ == "__main__":
    print("=== Alpha-Beta Pruning (Cutoff) Search Algorithm ===\n")

    # Input: leaf node values
    n = int(input("Enter number of leaf nodes (power of 2): "))
    values = []
    for i in range(n):
        val = int(input(f"Enter value for leaf node[{i}]: "))
        values.append(val)

    print("\nLeaf Nodes (Terminal Values):", values)
    max_depth = int(math.log2(n)) # since binary tree

    print("\n===== Search Trace =====\n")
    best_value = alpha_beta_pruning(0, 0, True, values, -math.inf, math.inf, max_depth)

    print("\n===== RESULT =====")
    print(f"Optimal Value (Best for Maximizer): {best_value}")

```

Output:


```

===== RESULT: C:/Users/ANUSCORN/Desktop/lab-10.py =====
--- Alpha-Beta Pruning (Cutoff) Search Algorithm ---

Enter number of leaf nodes (power of 2): 8
Enter value for leaf node[0]: 3
Enter value for leaf node[1]: 5
Enter value for leaf node[2]: 4
Enter value for leaf node[3]: 9
Enter value for leaf node[4]: 1
Enter value for leaf node[5]: 2
Enter value for leaf node[6]: 0
Enter value for leaf node[7]: -1

Leaf Nodes (Terminal Values): [3, 5, 4, 9, 1, 2, 0, -1]

===== Search Trace =====

Maximizer at depth 0, Alpha=-inf, Beta=inf
Minimizer at depth 1, Alpha=-inf, Beta=inf
Maximizer at depth 2, Alpha=-inf, Beta=inf
  Reached leaf node[0] = 3
  Max node[0] updated Best=3, Alpha=3, Beta=inf
  Reached leaf node[1] = 5
  Max node[0] updated Best=5, Alpha=5, Beta=inf
  Min node[0] updated Best=0, Alpha=-inf, Beta=0
  Minimizer at depth 2, Alpha=-inf, Beta=0
  Reached leaf node[2] = 4
  Max node[1] updated Best=4, Alpha=4, Beta=0
  -- Pruning remaining branches at Max node[1] (Beta <= Alpha) --
  Min node[0] updated Best=5, Alpha=5, Beta=0
Max node[0] updated Best=5, Alpha=5, Beta=inf
Minimizer at depth 1, Alpha=5, Beta=inf
Maximizer at depth 2, Alpha=5, Beta=inf
  Reached leaf node[3] = 9
  Max node[1] updated Best=9, Alpha=9, Beta=inf
  Reached leaf node[4] = 1
  Max node[2] updated Best=2, Alpha=5, Beta=inf
  Min node[1] updated Best=1, Alpha=5, Beta=1
  -- Pruning remaining branches at Min node[1] (Beta <= Alpha) --
  Max node[0] updated Best=9, Alpha=9, Beta=inf

===== RESULT =====
Optimal Value (Best for Maximizer): 9
>>>

```