

| Price (x) | Normalization | (Price - μ) ² | Standardization | Max Absolute Scaled |
|-----------|---------------------------------|-------------------------------|------------------------------------|--------------------------|
| 110 | $\frac{110-100}{150-100} = 0.2$ | $(110-116.11)^2 = 37.33$ | $\frac{110-116.11}{14.68} = -0.42$ | $\frac{110}{150} = 0.73$ |
| 105 | $\frac{105-100}{150-100} = 0.1$ | $(105-116.11)^2 = 123.43$ | $\frac{105-116.11}{14.68} = -0.76$ | $\frac{105}{150} = 0.70$ |
| 115 | $\frac{115-100}{150-100} = 0.3$ | $(115-116.11)^2 = 1.23$ | $\frac{115-116.11}{14.68} = -0.08$ | $\frac{115}{150} = 0.77$ |
| 120 | $\frac{120-100}{150-100} = 0.4$ | $(120-116.11)^2 = 15.13$ | $\frac{120-116.11}{14.68} = 0.26$ | $\frac{120}{150} = 0.80$ |
| 110 | $\frac{110-100}{150-100} = 0.2$ | $(110-116.11)^2 = 37.33$ | $\frac{110-116.11}{14.68} = -0.42$ | $\frac{110}{150} = 0.73$ |
| 130 | $\frac{130-100}{150-100} = 0.6$ | $(130-116.11)^2 = 192.93$ | $\frac{130-116.11}{14.68} = 0.95$ | $\frac{130}{150} = 0.87$ |
| 150 | $\frac{150-100}{150-100} = 1$ | $(150-116.11)^2 = 1148.53$ | $\frac{150-116.11}{14.68} = 2.30$ | $\frac{150}{150} = 1$ |
| 100 | $\frac{100-100}{150-100} = 0$ | $(100-116.11)^2 = 259.53$ | $\frac{100-116.11}{14.68} = -1.10$ | $\frac{100}{150} = 0.67$ |
| 105 | $\frac{105-100}{150-100} = 0.1$ | $(105-116.11)^2 = 123.43$ | $\frac{105-116.11}{14.68} = -0.76$ | $\frac{105}{150} = 0.7$ |
| | | $\Sigma = 1938.87$ | | |

Standardization

$$X_{\text{new}} = \frac{X_i - X_{\text{mean}}}{\text{Standard deviation}}$$

$$\sigma = \sqrt{\frac{\Sigma (X_i - \mu)^2}{N}}$$

Normalization

$$X_{\text{new}} = \frac{X_i - \min(X)}{\max(X) - \min(X)}$$

$$\mu = X_{\text{mean}} = \frac{110 + 105 + 115 + 120 + 110 + 130 + 150 + 100 + 105}{9} = 116.11$$

Let, $x = \text{Price}$

$$\min(x) = 100$$

$$\max(x) = 150$$

$$N = 9$$

Max Absolute Scaled

$$x_{\text{scaled}} = \frac{x}{\max(x)}$$

| Price (x) | Log transform | Robust Sealing |
|-----------|-------------------|-----------------------------------|
| 110 | $\ln(110) = 4.70$ | $\frac{110-110}{120-105} = 0$ |
| 105 | $\ln(105) = 4.65$ | $\frac{105-110}{120-105} = -0.33$ |
| 115 | $\ln(115) = 4.74$ | $\frac{115-110}{120-105} = 0.33$ |
| 120 | $\ln(120) = 4.7$ | $\frac{120-110}{120-105} = 0.67$ |
| 110 | $\ln(110) = 4.70$ | $\frac{110-110}{120-105} = 0$ |
| 130 | $\ln(130) = 4.87$ | $\frac{130-110}{120-105} = 1.33$ |
| 150 | $\ln(150) = 5.01$ | $\frac{150-110}{120-105} = 2.67$ |
| 100 | $\ln(100) = 4.61$ | $\frac{100-110}{120-105} = -0.67$ |
| 105 | $\ln(105) = 4.65$ | $\frac{105-110}{120-105} = -0.33$ |

100 105 105 110 110 115 120 130 150
 25th percentile 75th percentile

$$9 \times \frac{75}{100} = 6.75 \approx 7$$

25th percentile

Robust Sealing

$$9 \times \frac{25}{100} = 2.25 \approx 3$$

$$X_i - X_{\text{median}}$$

IQR

$$\{75^{\text{th}} \text{ percentile} - 25^{\text{th}} \text{ percentile}\}$$