Random Stuff 3

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Q) A number n in base 10 when written in base b is 503 ond when written in 6+2 is 305. Find the product of

$$Aw! N = 3x(b+2)^{2} + 0 \times (b+2)^{1} + 5 \times (b+2)^{0}$$
 $N = 5 \times b^{2} + 0 \times b^{1} + 3 \times b^{0}$

$$\Rightarrow 3(b+2)^{2}+5 = 5-b^{2}+3$$

$$\Rightarrow 3b^{2}+12b+12+5-5-b^{2}+3 \Rightarrow 2b^{2}-12b-14=0$$

$$\Rightarrow b^{2}-6b-7=0$$

$$\Rightarrow b^{2}-6b-7$$

$$\langle S \rangle$$
 x>0 and $[x] + [\frac{1}{x}] = 2$. Find range of 2e.

Aw;
$$-2+\frac{1}{2}-\frac{1}{2}=2$$
 $x+\frac{1}{2}-\frac{1}{2}=2$
 $x+\frac{1}{2}-\frac{1}{$

$$x \in (2-\sqrt{3}, 2+\sqrt{3})$$
 $x \in (2-\sqrt{3}, 2+\sqrt{3})$
 $x \neq (2-\sqrt{3}, 2+\sqrt{3})$
 $x \neq$

$$\Rightarrow [n] + [n] = 2 \Rightarrow 0 + [n] = 2 \Rightarrow 2 \le \frac{1}{6} \le 3$$

$$\Rightarrow \frac{1}{2} > \epsilon > \frac{1}{3}$$

$$\Rightarrow \boxed{\pi \in \left(\frac{1}{3}, \frac{1}{2}\right]}$$

$$(an)^{\frac{1}{2}}$$

$$(an)$$

Care 3:
$$-\infty = 2+\varepsilon$$
, $-\infty = 2+\varepsilon$ $-\infty = 2+\varepsilon$

$$\underbrace{(ax 4:-)}_{n=3+\epsilon} = 3+0=3+2\times$$

So we get the final rouge as ac (3/1] U [13 U [2/3)

a) Let nyz be positive red numbers. Show that x4+y4+22 > 18 xy2

Ans:
$$\frac{2^4+y^4+\frac{2^2}{2}+\frac{2^2}{2}}{4} > \frac{4\sqrt{x^2y^2z^4}}{4} > x^4+y^6+z^2 > \frac{4}{\sqrt{2}}xy^2 = \sqrt{8}xy^2$$

 Δ For any rul number 2, y > 1 prove that $\frac{2^2}{4-1} + \frac{y^2}{2-1} > 8$.

$$Aw:-\frac{2^{2}}{4-1}+\frac{4^{2}}{n-1}>2\frac{n}{\sqrt{(n-1)(4-1)}}\Rightarrow 2\frac{n}{\sqrt{n-1}}\frac{4}{\sqrt{n-1}}>2.2.2.2>8$$

Aus:
$$\frac{x^2}{4-1} + \frac{y^2}{n-1} > 2 \xrightarrow{ny} \xrightarrow{y} \Rightarrow 2 \xrightarrow{n} \frac{y}{\sqrt{n-1}} > 2 \cdot 2 \cdot 2 \Rightarrow 8$$

$$(n-2)^2 = x^2 - 4n + 4 > 0$$

$$\Rightarrow x^2 > 4 (n-1)$$

$$\Rightarrow x > 2 \sqrt{n}$$

a> Let a, b $\in \mathbb{R}$, $a \neq 0$. Show that, $a^2 + b^2 + \frac{1}{a^2} + \frac{b}{a} > \sqrt{3}$

Ans:
$$a^{2} + (b + \frac{1}{2a})^{2} + \frac{3}{4a^{2}}$$

$$(1 + 1)^{2}, \quad a^{2} + \frac{3}{4a^{2}} = (b + \frac{1}{2})^{2} + (a - (\frac{3}{4})a^{2})^{2} + 2(\frac{3}{4})a^{2}$$

Ans:
$$a^{2} + (b + \frac{1}{2a}) + \frac{7}{4a^{2}}$$

$$= (b + \frac{1}{2a})^{2} + a^{2} + \frac{3}{4a^{2}} = (b + \frac{1}{2a})^{2} + (a - (\frac{3}{4})a^{2}) + 2(\frac{3}{4})a^{2}(a)$$

$$= (b + \frac{1}{2a})^{2} + (a - (\frac{3}{4})a^{2}) + \sqrt{3} > \sqrt{3}$$

$$= (b + \frac{1}{2a})^{2} + (a - (\frac{3}{4})a^{2}) + \sqrt{3} > \sqrt{3}$$
which were