O) If in DABC, AC=15 and BC=13 and IG||AB where I's
the incentre and G's the centroid of DABC. Find the area
of DABC.

Aw:- Area of DABC =  $\frac{1}{2}v(AB+BC+CA)$ =  $\frac{1}{2}h(AB)$  (his beight of C from AB) As IG[|AB|, h = 3(GX)]

GX = IY as  $IGI|AB \Rightarrow N=3(IY) = 3v$ 

$$\frac{1}{2} + (AB + 1S + 13) = \frac{1}{2} \frac{3}{4} (AB)$$

$$\Rightarrow 3AB = AB + 1S + 13 \Rightarrow AB = 14$$
Ana of  $ABC = \sqrt{S(S-C)(S-C)}$ 

B) Let ABCD be a cyclic quadrilateral. Let I, and I\_2 be the Incurred of AABC and ADBC respectively. Prove that I\_I\_2\_BC is also cyclic.

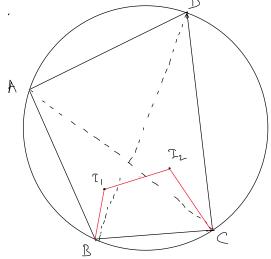
Aw: - We med to show, LBIC = LBI2C

$$\angle BT_{,C} = 180^{\circ} - (\angle T_{,B}C - \angle T_{,CB})$$

$$= 180^{\circ} - \frac{1}{2}(\angle ABC + \angle ACB)$$

$$= 180^{\circ} - \frac{1}{2}(180^{\circ} - \angle BAC)$$

$$= 90^{\circ} + \frac{1}{2}\angle BAC$$



Similarly, LBI\_C = 90°+1 LBDC

Also, LBAC = LBDC as BC is common chand. -> LBI( = LBI2C

B) Given a pair of concentric circles chord AB, BC, CD.... of the outer circle are drawn such that they all touch the inner circle. If LABC = 75° how many chards can be drawn before returning to the starting point.

Ani- LAOB = 105°

105 K = 360 M

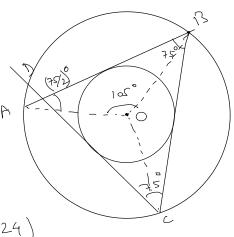
Some web to find smellest

such KEN

=> 102 k = 0 (mag 360)

 $\Rightarrow 2|k = 72m$   $\Rightarrow 7k = 24m \Rightarrow 7k = 0 \pmod{24}$ 

=> swallest [x = 24]



O> The sides x and y of a scalean triangle satisfy  $x+2\Delta = y+2\Delta$  where  $\Delta$  is the area of the triangle. If x=60 and y=63, what is the length of the largest side of the triangle

Au: - Apply, S = x + y + z = 123 + z and  $x + \frac{2}{x} \sqrt{s(s-x)(s-y)(s-z)}$   $y = 4 + \frac{2}{y} \sqrt{s(s-x)(s-y)(s-z)}$  y = 63y = 63

A rectorque piece of paper has integer side bugths. The paper is folded so that a pair of diagonally opposite vertices coincide and it is found that the crease is of bugth 65. Find a possible value of the perimeter of the paper.

A paper.

Au'-BX=BY=a-c

Ausi- 
$$BX = DY = a - c$$
  
 $XY = 65$   
 $MY = a - 2c$   
 $(a - 2c)^2 + b^2 = 65^2$   
 $c^2 + b^2 = (a - c)^2$   
 $a - 2c = 16$ ,  
 $b = 63$ 

