Signals and Systems Homework 11 Due Time: 23:59 June 1^{st} , 2018 Submitted in-class on Thu (May 31), or to the box in front of SIST 1C 403E (the instructor's office).

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- 1. (5) Consider the signal $x[n] = (\frac{1}{5})^n u[n-3]$ and evaluate the z-transform of this signal, then specify the region of convergence.
- 2. (10) A cuasal LTI system is described by the difference equation.

$$y[n] = y[n-1] + y[n-2] + x[n-1]$$

- (a) Find the system function $H(z) = \frac{Y(z)}{X(z)}$ for the system. Plot the ploes and zeros of H(z) and indicate the region of convergence.
- (b) Find the unit sample response of the system.
- (c) You should have found the system to be unstable. Find a stable(noncausal) unit sample response that satisfies the difference equation.
- 3. (5) Consider the linear discrete, shift-invariant system with input x[n] and output y[n] for which

$$y[n-1] - \frac{10}{3}y[n] + y[n+1] = x[n]$$

The system is stable. Determine the unit sample response.

4. (20) A causal LTI system with input x[n] and output y[n] has the following block-diagram representation

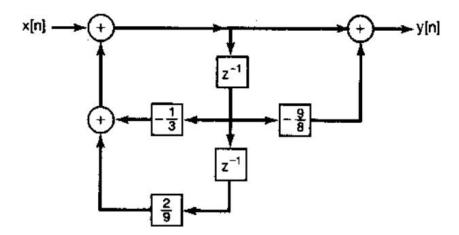


Figure 1: Block-diagram

- (a) Determine a difference equation relating y[n] and x[n].
- (b) Is the system stable?
- 5. (20) The following is known about a discrete-time system with input x[n] and output y[n]: a. If $x[n] = (-2)^n$ for all n, then y[n] = 0 for all n;
 - b. If $x[n] = (\frac{1}{2})^n u[n]$ for all n, then y[n] for all n is of the form:

$$y[n] = \delta[n] + a(\frac{1}{4})^n u[n]$$

a is a constant.

- (a) Determine the value of the constant a.
- (b) Determine the response y[n] if the input x[n] is

$$x[n] = 1$$

for all n

6. (20) By using the power-series expansion:

$$log(1-w) = -\sum_{i=1}^{\infty} \frac{w^i}{i}$$

and |w| < 1 determin the inverse of each of the following two z-transform:

- (a) $X(z) = log(1-2z), |z| < \frac{1}{2}$
- (b) $X(z) = log(1 \frac{1}{2}z^{-1}), |z| > \frac{1}{2}$
- 7. (20) Use the unilateral z-transform

$$F(z) = \sum_{n=0}^{\infty} f[n]z^{-n}$$

to compute the value of the n-th term of the Fibonacci sequence:

$$f(n+2) = f(n+1) + f(n), \quad n \ge 0$$

with f(0) = 1, f(1) = 1. (Hint: Be careful about using the properties of ZT since the above equality just holds for $n \ge 0$.)