

CS243: Introduction to Algorithmic Game Theory

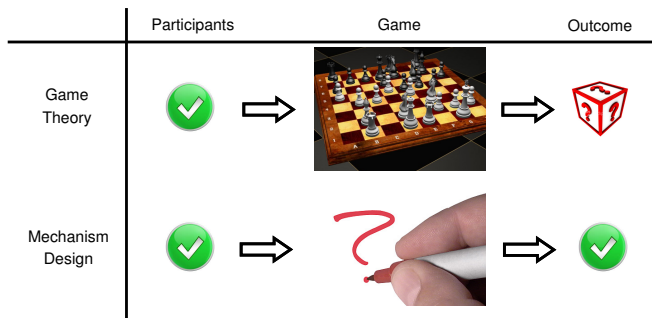
Week 2.1, Dominate Strategy and Truthfulness (Dengji ZHAO)

SIST, ShanghaiTech University, China

Office Hour

- Location: SIST 1A301
- Time Slots:
 - JIA Feiran: Tue, 6pm-7pm.
 - ZHAO Dengji (1A304E): Wed, 4:30pm-5:30pm.
 - ZHANG Wen: Thu, 7pm-8pm.
 - WANG Yao: Thu, 8pm-9pm.

Recap: Game Theory



Recap: (Simultaneous Move) Game Playing

- A set of n players
- Each player i has a set of strategies S_i
- Let $s = (s_1, \dots, s_n)$ be the vector of strategies selected by the n players. Also let $\mathbf{s} = (s_i, \mathbf{s}_{-i})$.
- Let $S = \times_i S_i$ be the strategy vector space of all players.
- Each $s \in S$ determines the outcome for each player, denote $u_i(s)$ the utility of player i under s .

Recap: (Simultaneous Move) Game Playing

Definition

A strategy vector $s \in S$ is a **dominant strategy**, if for each player i , and each alternate strategy vector $s' \in S$, we have that

$$u_i(s_i, s'_{-i}) \geq u_i(s'_i, s'_{-i})$$

Definition

A strategy vector $s \in S$ is said to be a (pure strategy) **Nash equilibrium** if for all players i and each alternate strategy $s'_i \in S_i$, we have that

$$u_i(s_i, s_{-i}) \geq u_i(s'_i, s_{-i})$$

Recap: Games

		P2	
		Confess	Silent
P1	Confess	4, 4	5, 1
	Silent	1, 5	2, 2

Prisoners' Dilemma

		Boy	
		B	S
Girl	B	6, 5	1, 1
	S	2, 2	5, 6

Battle of the Sexes

		2	
		H	T
1	H	-1, 1	1, -1
	T	1, -1	-1, 1

Matching Pennies

How to compute strategies?

Learning in Games: Best Response

Best Response

Definition

We say that a change from strategy s_i to s'_i is an **improving response** for player i if $u_i(s'_i, s_{-i}) > u_i(s)$ and **best response** if s'_i maximizes the players' utility $\max_{s'_i \in S_i} u_i(s'_i, s_{-i})$.

Best Response

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Matching Pennies

Game Design: Mechanism Design

- Auctions (**Second Price Auction**)

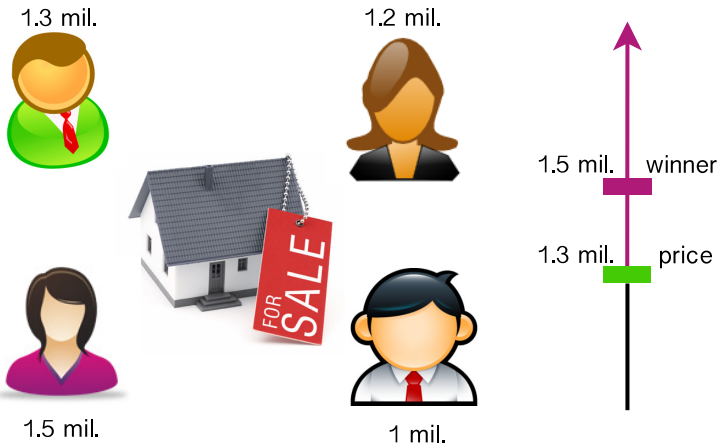
The Setting

- A seller sells an item, e.g. a house.
- A set of n buyers are willing to buy the item, each buyer i has a (**private**) valuation v_i on the item.

Second Price Auction (Vickrey Auction)

- Each buyer reports her valuation to the seller
- The seller sells the item to the buyer with the highest valuation report
- The seller charges the winner the second highest valuation report

Second Price Auction (Vickrey Auction)



Strategies of the Buyers

- Strategy/Action space:

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 - Quiz: answer via [slido.com](https://www.slido.com), event code U562, all possible valuations can be reported, e.g. all real numbers

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- Strategy/Action space:
 - Quiz: answer via [slido.com](https://www.slido.com), event code U562, all possible valuations can be reported, e.g. all real numbers
- What is the best strategy for a buyer?
 - Quiz: answer via [slido.com](https://www.slido.com), event code U562, report his true valuation

Dominant Strategy in Auction Design: Truthfulness

Definition

An auction is **truthful** if reporting valuation truthfully is a **dominant strategy** for all participants/buyers.

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 - Simplify participants' decision making
 - Receive truthful valuation information for other decision making, e.g. maximising social welfare

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Question

Is there any weakness of truthfulness?

- cannot prevent group manipulations

Challenges

Challenge

Is first price auction truthful? No

Challenges

Challenge

Is first price auction truthful? No

Quiz

Is fixed price auction truthful? Yes

- A fixed price is given in advance/public-known.
- All buyers whose reports above the fixed prices will win and pay the fixed price.
- If the number of buyers above the price is more than the number of items to sell, use random tie-breaking.

Advanced Reading

Challenge

How to extend second price auction for single item to multiple items settings? Vickrey-Clarke-Groves (VCG)

- Introduction to Mechanism Design [AGT Chapter 9]

Homework 2.1: Project Proposal

- Each student proposes one project proposal
 - topics can be anything around game theory: design a game, solve an existing game, etc.
- The proposal should specify (in English):
 - What is the problem, why it is interesting?
 - What is the goal?
 - How is it related to algorithmic game theory?
- Evaluation and Credits:
 - Post your proposal on blackboard (by 9th Oct) and also email to wangyao1@shanghaitech.edu.cn
 - Discuss your proposals on blackboard.
 - Choose **top 10 proposals** based on discussions (each receives **1 credit**).
 - Choose **final top 3 proposals** as our project proposals by 31st Oct (each receives **3 credits**).