

# Cryptography: Homework 3

(Deadline: 10am, 2021/10/29)

1. (20 points) Prove that if  $f$  is a one-way function, then the function  $g$  defined by  $g(x_1, x_2) = (f(x_1), x_2)$ , where  $|x_1| = |x_2|$ , is also a one-way function.
2. (30 points) Let  $F$  be a length-preserving pseudorandom function. Let  $F' : \{0, 1\}^n \times \{0, 1\}^{n-1} \rightarrow \{0, 1\}^{2n}$  be a keyed function such that  $F'_k(x) = F_k(0\|x)\|F_k(x\|1)$ . State whether  $F'$  is a pseudorandom function. If yes, prove it; if not, show an attack.