

(1) (8 Points) Here is a sorting algorithm in the following. (The array starts at index 1)

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Procedure Sort(A):  
  for i = 1 to A.length - 1:  
    for j = A.length downto i + 1:  
      if A[j] < A[j - 1]  
        key = A[j]  
        A[j] = A[j - 1]  
        A[j - 1] = key  
    // Mark
```

- (3 Points) Which sorting algorithm does it describe?
- (5 Points) Given a list as [31, 4, 59, 26, 41, 58], we use the above procedure to sort it. Write down what will the list be like each time when the procedure meets the **Mark**.

- (2) (7 Points) Suppose that we have a hash table with n slots, with collisions resolved by chaining, and suppose that n keys are inserted into the table. Each key is equally likely to be hashed to each slot. Let M be the maximum number of keys in any slot after all keys have been inserted.
- (3 Points) Calculate the probability Q_k that exactly k keys hash to a particular slot.
 - (4 Points) Let P_k be the probability that $M = k$, that is, the probability that the slot containing the most keys contains k keys. Show that $P_k \leq nQ_k$.