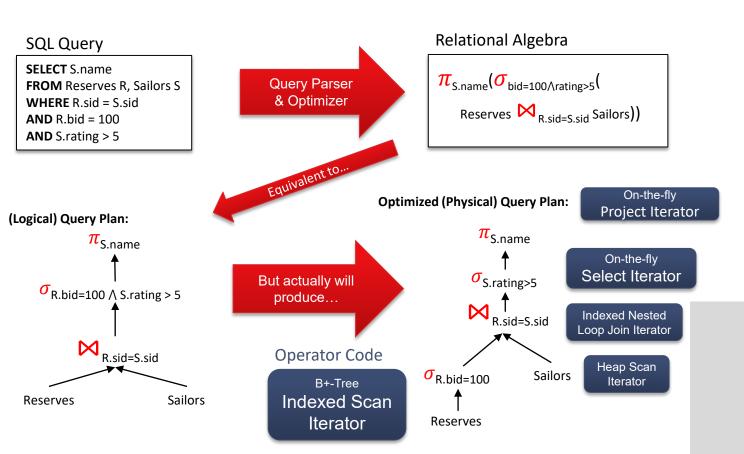
Iterators, Relational Operators and Joins

R&G Chapters 12 & 14





Recall from Last Lecture

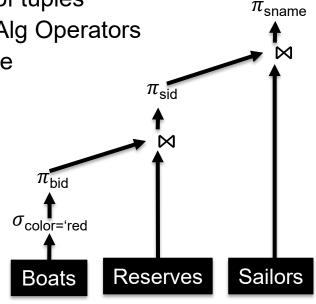




Relational Operators and Query Plans

$$\pi_{\text{sname}}(\pi_{\text{sid}}(\pi_{\text{bid}}(\sigma_{\text{color='red'}}(\text{Boats})) \bowtie \text{Res}) \bowtie \text{Sailors})$$

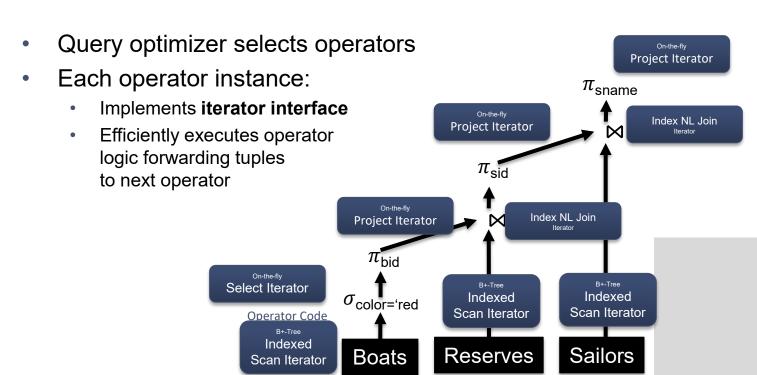
- Query plan
 - Edges encode "flow" of tuples
 - Vertices = Relational Alg Operators
 - Source vertices = table access operators ...
- Also called dataflow graph





Query Executor Instantiates Operators

 $\pi_{\text{sname}}(\pi_{\text{sid}}(\pi_{\text{bid}}(\sigma_{\text{color='red'}}(\text{Boats})) \bowtie \text{Res}) \bowtie \text{Sailors})$





Iterator Interface

The relational operators implemented as subclasses of the class Iterator:

```
abstract class iterator {
     void setup(List<Iterator> inputs);
     void init(args);
     tuple next();
     void close();
}
```

Notes:

- Pull-based computation model
 - e.g., Console calls init and next which propagates down graph
 - init/next can result in either streaming ("on-the-fly") or blocking ("batch") algorithm:
 - streaming: small, constant amount of work per call
 - blocking: does not produce output until it consumes its entire input!
- Encapsulation: any iterator can be input to any other!
- State: iterators may maintain substantial "internal" state
 - e.g., hash tables, running counts, large sorted files ...



Example: Select (on-the-fly)

```
init(predicate):
 child.init()
 pred = predicate;
 current = NULL;
next():
 while (current != EOF && !pred(current))
    current = child.next();
 return current;
close():
 child.close()
```



Example: Heap Scan

```
init(relation):
  heap = open heap file for this relation;
  cur page = heap.first page(); // first page
  cur slot = cur page.first slot(); // first slot on that page
next():
  if (cur page == NULL) return EOF; // End Of Fun
  current = [cur page, cur slot]; // we will return this recordld
  // advance the slot
  cur slot = cur slot.next();
  if (cur slot == NULL) {
   // advance to next page, first slot
   cur page = cur page.next();
   if (cur page != NULL)
     cur slot = cur page.first slot();
  return current:
close():
  heap.close()
```



Example: Sort (2-pass)

```
    init(keys):  // all of pass 0 in init, a blocking call child.init()
    repeatedly call child.next() and generate the sorted runs on disk, until child gives EOF
    // set up for pass 1, assumes enough buffers to merge
    open each sorted run file and load into input buffer for pass 1
    next():  // pass 1 (assumes enough buffers to merge)
    output = min tuple across all buffers
    if min tuple was last one in its buffer, fetch next page from that run into buffer
    return output (or EOF -- "End of Fun" -- if no tuples remain)
```

 close(): deallocate the runs files child.close()



Example: Group By on Sorted input

```
GroupBy
```

```
    init(group_keys, aggs):
        child.init()
        cur_group = NULL;
    next():
        result = NULL
        do {
```

```
do {
    tup = child.next();
    if (group(tup) != cur_group) { // New group!
        if (cur_group != NULL) // Form a result for current group
            result = [cur_group, final() of all aggs]
            cur_group = group(tup);
            call init() on all the aggs
        }
        call merge(tup) on all the aggs
} while (!result);
return result:
```

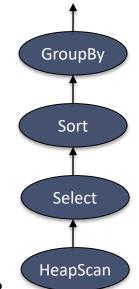
close(): child.close()

agg_type	state	init	merge(x)	final
COUNT	count	0	count ++	count
SUM	sum	0	sum += x	sum
AVG	[count, sum]	[0, 0]	[count++, sum+=x]	sum / count
MIN	min	+infinity	min > x ? x : min	min



A Full Query Plan

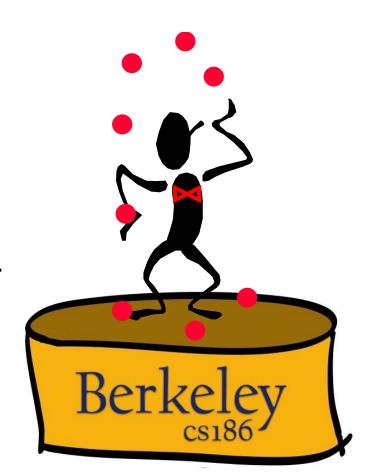
- A Query Plan is Single-threaded!
- Trace the calls:
 - Call init() on the root GroupBy
 - How does init() recurse down the chain and return?
 - call next() on root
 - How does next() recurse down the chain and return a tuple?
- Note how the blocking operator (sort) interacts with the other, streaming operators
- Note how we don't store operator output on disk; tuples stream through the plan's call stack
 - Some operators like Sort use disk internally





Join Operators

R&G 14.4





Schema for Examples



- Cost Notation
 - [R] : the number of pages to store R
 - p_R: number of records per page of R
 - |R|: the cardinality (number of records) of R
 - $|R| = p_R^*[R]$
- Reserves (sid: int, bid: int, day: date, rname: string)
 - [R]=1000, p_R=100, |R| = 100,000
- Sailors (sid: int, sname: string, rating: int, age: real)
 - [S]=500, p_S =80, |S| = 40,000



Simple Nested Loops Join

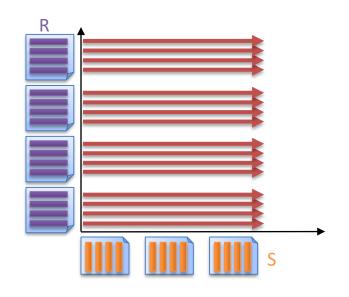


foreach **record** r in R do

foreach record s in S do

if θ(ri, sj) then add <ri, sj> to result buffer

Note: for simplicity we do not present iterator implementations for the join algorithms.



[R]=1000,
$$p_R$$
=100, $|R|$ = 100,000
[S]=500, p_S =80, $|S|$ = 40,000

Cost:



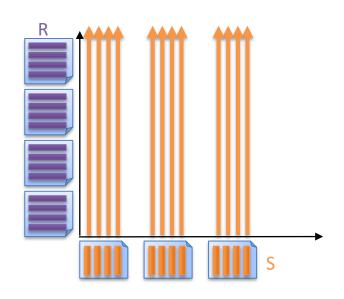
Changing the Join Order



foreach record s in S do

foreach **record** r in R do

if θ(ri, sj) then add <ri, sj> to result buffer



```
[R]=1000, p_R=100, |R| = 100,000
[S]=500, p_S=80, |S| = 40,000
```

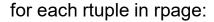
Cost:



Page Nested Loop Join

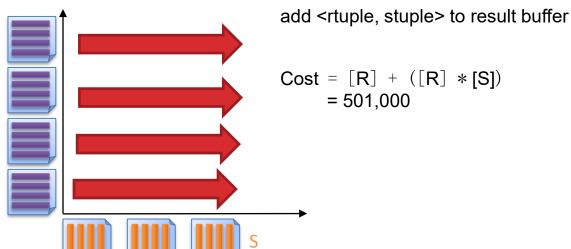


for each rpage in R: for each spage in S:



for each stuple in spage:

if join condition(rtuple, stuple):







"Block" Nested Loop Join



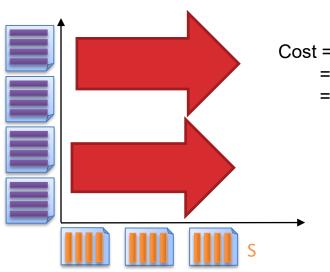


for each rchunk of B-2 pages of R:

for each spage of S:

for all matching tuples in spage and rchunk:

add <rtuple, stuple> to result buffer



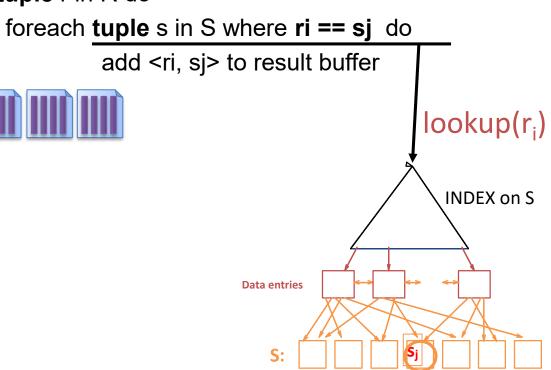
```
Cost = [R] + [ [R]/(B-2) ] * [S]
= 1000 + [ 1000/(B-2) ] * 500
= 6,000 for B=102 (~100x better than Page NL!)
```



Index Nested Loops Join



foreach **tuple** r in R do



Data Records



Index Nested Loops Join Cost



foreach **tuple** r in R do

foreach **tuple** s in S where **ri == sj** do add <ri, sj> to result

Cost = [R] + |R| * cost to find matching S tuples

- If index uses Alt. 1 → cost to traverse tree from root to leaf. (e.g., 2-4 IOs)
- For Alt. 2 or 3:
 - Cost to lookup RID(s); typically 2-4 IOs for B+Tree.
 - Cost to retrieve records from RID(s)
 - Clustered index: 1 I/O per page of matching S tuples.
 - Unclustered: up to 1 I/O per matching S tuple



Index Nested Loops Join Cost, Part 2



- Reserves (<u>sid</u>: int, <u>bid</u>: int, <u>day</u>: date, <u>rname</u>: string)
 - [R]=1000, p_R =100, |R| = 100,000
- Sailors (<u>sid</u>: int, sname: string, rating: int, age: real)
 - [S]=500, p_S =80, |S| = 40,000
 - Index on sid



Index Nested Loops Join Cost, Part 3



- Unclustered Cost(R,S) = [R] + |R| * (Search + # matching tuples)
- Clustered Cost(R,S): [R] + |R| * (Search + # of matching pages)
- Here, sid is the primary key for Sailors, so there is exactly one matching sailor for each tuple in R
- Unclustered B+-Tree height 2 (3 I/Os from root to leaf):
 - $\mathbb{R} \times \mathbb{S}$: 1000 + (100,000)*(3 + 1) = 401,000
- Clustered B+-tree height 2 (3 I/Os from root to leaf)
 - $R \bowtie S: 1000 + (100,000)*(3 + 1) = 401,000$



Sort-Merge Join



- Requires equality predicate:
 - Equi-Joins & Natural Joins
- Two Stages:
 - Sort tuples in R and S by join key
 - All tuples with same key in consecutive order
 - Input might already be sorted ... why?
 - Join Pass: Merge-scan the sorted partitions and emit tuples that match



```
do {
  if (!mark) {
    while (r < s) { advance r }
   while (r > s) { advance s }
   // mark start of "block" of S
   mark = s
  if (r == s) {
    result = <r, s>
    advance s
    return result
  else {
    reset s to mark
    advance r
    mark = NULL
```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

si	id	bid
2	8	103
2	8	104
3	1	101
3	1	102
4	2	142
5	8	107





```
do {
  if (!mark) {
    while (r < s) { advance r }
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   // mark start of "block" of S
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    result = <r, s>
    advance s
    return result
  else {
    reset s to mark
    advance r
    mark = NULL
```

	sid	sname
>	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid
28	103
28	104
31	101
31	102
42	142
58	107





```
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sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

	sid	bid
-	28	103
	28	104
	31	101
	31	102
	42	142
	58	107





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    advance s
    return result
  else {
    reset s to mark
    advance r
    mark = NULL
```

	sid	sname
	22	dustin
\Rightarrow	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
	·	





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```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

_		
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	





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sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	





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sid	sname	
22	dustin	
28	уирру	
31	lubber	
31	lubber2	
44	guppy	
58	rusty	

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	





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    return result
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```



sid	sname	bid
28	уирру	103

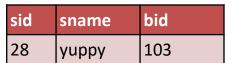




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```

sid	sname		sid	bid
22	dustin		28	103
28	уирру	\Rightarrow	28	104
31	lubber		31	101
31	lubber2		31	102
44	guppy		42	142
58	rusty		58	107

Siu	biu	
28	103	
28	104	
31	101	
31	102	
42	142	
го	107	







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    advance s
    return result
  else {
    reset s to mark
    advance r
    mark = NULL
```

sid	sname	•
22	dustin	
28	уирру	
31	lubber	
31	lubber2	
44	guppy	
58	rusty	

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
		-

		_
Berl	cs186	y

sid	sname	bid
28	yuppy	103



```
do {
  if (!mark) {
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sid	sname		sid	bid
22	dustin		28	103
28	yuppy	\Rightarrow	28	104
31	lubber		31	101
31	lubber2		31	102
44	guppy		42	142
58	rusty		58	107

sid	sname	bid
28	уирру	103





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sid	sname	
22	dustin	
28	уирру	
31	lubber	\Rightarrow
31	lubber2	
44	guppy	
58	rusty	

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103





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sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104





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sid	sname
22	dustin
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sid	bid	
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28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104





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sid	sname
22	dustin
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		_
sid	bid	
28	103	
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42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	уирру	104





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```

sid	sname	
22	dustin	•
28	уирру	
31	lubber	
31	lubber2	
44	guppy	
58	rusty	

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
		•



S	sid	sname	bid
2	28	yuppy	103
2	28	уирру	104



```
do {
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```

sid	sname
22	dustin
28	уирру
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31	lubber2
44	guppy
58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
		1



sid	sname	bid
28	yuppy	103
28	уирру	104



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sid	sname
22	dustin
28	уирру
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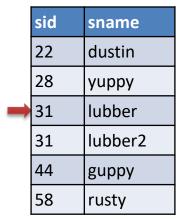
sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

sid	sname	bid
28	yuppy	103
28	yuppy	104





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do {
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    reset s to mark
    advance r
    mark = NULL
```



sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

sid	sname	bid
28	yuppy	103
28	yuppy	104



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```

	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

sid	sname	bid
28	yuppy	103
28	уирру	104





```
do {
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	sid	sname
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sid	bid
28	103
28	104
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31	102
42	142
58	107

sid	sname	bid
28	yuppy	103
28	yuppy	104





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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
	·	

sid	sname	bid
28	yuppy	103
28	уирру	104





```
do {
  if (!mark) {
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    advance s
    return result
  else {
    reset s to mark
    advance r
    mark = NULL
```

	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104





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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

		1
sid	bid	
28	103	
28	104	
31	101	1
31	102	

sid	sname	bid
28	yuppy	103
28	уирру	104





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do {
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```

	sid	sname
→	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	уирру	103
28	yuppy	104





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	sid	sname
→	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
42	142	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101





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do {
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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

Ве

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101



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do {
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```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101





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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
		-

sid	bid	
28	103	
28	104	
31	101	1
31	102	
42	142	

Berkelev

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101



```
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```
}
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  advance r
  mark = NULL
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```

	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

			_
	sid	bid	
	28	103	
	28	104	
	31	101	
	31	102	
>	42	142	
	58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101





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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

			_
	sid	bid	
	28	103	
	28	104	
	31	101	
	31	102	
>	42	142	
	58	107	

sid	sname	bid
28	уирру	103
28	уирру	104
31	lubber	101
31	lubber	102



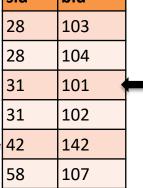


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1	sid	sname	
	22	dustin	
	28	уирру	
	31	lubber	
	31	lubber2	
	44	guppy	
	58	rusty	

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	bid	
28	103	
28	104	
31	101	
31	102	





sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102



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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

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sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102



```
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```

	sid	sname	
	22	dustin	
	28	yuppy	
	31	lubber	
	31	lubber2	
	44	guppy	
	58	rusty	

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102





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```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102





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```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

	sid	bid
	28	103
	28	104
>	31	101
	31	102
	42	142
	58	107

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102





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```

sid	sname
22	dustin
28	уирру
31	lubber
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44	guppy
58	rusty

	sid	bid
	28	103
	28	104
	31	101
	31	102
	42	142
	58	107

	<u> </u>	
sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102





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```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty
	22 28 31 31 44

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	уирру	103
28	уирру	104
31	lubber	101
31	lubber	102





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sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
	28 28 31 31 42	28 103 28 104 31 101 31 102 42 142

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102



```
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•	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
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sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102



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     result = <r, s>
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```

```
return result
```

```
}
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```

sid	sname
22	dustin
28	уирру
31	lubber
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58	rusty

	sid	bid
	28	103
	28	104
	31	101
>	31	102
	42	142
	58	107

Berkeley

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102

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•	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101





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sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101

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```

•	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
	58	rusty

bid	
103	
104	
101	
102	
142	
107	
	103 104 101 102 142

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101





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sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

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sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101



```
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sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

	sid	bid	
	28	103	
	28	104	
	31	101	
	31	102	
-	42	142	
	58	107	

sid	bid	
28	103	
28	104	
31	101	_
31	102	
42	142	

Berkelev

sid	sname	bid
28	уирру	103
28	уирру	104
31	lubber	101
31	lubber	102
31	lubber2	101

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•	sid	sname
	22	dustin
	28	уирру
	31	lubber
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	58	rusty

sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102





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sid	sname
22	dustin
28	уирру
31	lubber
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sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
		•

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102





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```

sid sname	
22 dustin	
28 yuppy	
31 lubber	
→ 31 lubber2	
44 guppy	
58 rusty	

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
•	•	•

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sid	sname	bid	
28	уирру	103	
28	yuppy	104	
31	lubber	101	
31	lubber	102	
31	lubber2	101	
31	lubber2	102	





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sid	sname
22	dustin
28	уирру
31	lubber
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58	rusty

		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
	-	•

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102





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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
=	44	guppy
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		_
sid	bid	
28	103	
28	104	
31	101	
31	102	
42	142	
58	107	
	·	•

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102

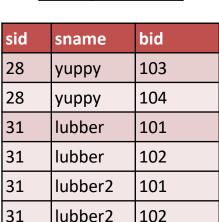


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  else {
    reset s to mark
    advance r
   mark = NULL
```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

sid	bid
28	103
28	104
31	101
31	102
42	142
58	107





```
do {
  if (!mark) {
    while (r < s) { advance r }
   while (r > s) { advance s }
   // mark start of "block" of S
   mark = s
  if (r == s) {
    result = <r, s>
    advance s
    return result
  else {
    reset s to mark
    advance r
   mark = NULL
```

	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
>	44	guppy
	58	rusty

sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

	,	
		
sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101

102

lubber2

31





```
do {
  if (!mark) {
   while (r < s) { advance r }
    while (r > s) { advance s }
    // mark start of "block" of S
   mark = s
  if (r == s) {
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    return result
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    advance r
    mark = NULL
```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

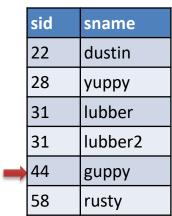
sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102





```
do {
  if (!mark) {
   while (r < s) { advance r }
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    mark = s
  if (r == s) {
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    advance s
    return result
  else {
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    advance r
    mark = NULL
```



sid	bid
28	103
28	104
31	101
31	102
42	142
58	107
	·

	Berkel

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



```
do {
  if (!mark) {
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  if (r == s) {
    result = \langle r, s \rangle
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```

	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
>	44	guppy
	58	rusty

bid
103
104
101
102
142
107



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



```
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```

	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
-	44	guppy
	58	rusty

sid	bid
28	103
28	104
31	101
31	102
42	142
58	107
	28 28 31 31 42



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



```
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	22	dustin
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	31	lubber2
- >	44	guppy
	58	rusty

bid
103
104
101
102
142
107



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



```
do {
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```

	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
>	58	rusty

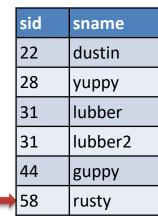
sid	bid
28	103
28	104
31	101
31	102
42	142
58	107



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



```
do {
  if (!mark) {
    while (r < s) { advance r }
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    mark = s
  if (r == s) {
    result = <r, s>
    advance s
    return result
  else {
    reset s to mark
    advance r
    mark = NULL
```



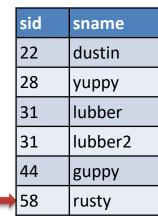
sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

	1 000	
sid	sname	bid
28	уирру	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102





```
do {
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   while (r < s) { advance r }
   while (r > s) { advance s }
    // mark start of "block" of S
    mark = S
  if (r == s) {
    result = <r, s>
    advance s
    return result
  else {
    reset s to mark
    advance r
    mark = NULL
```



sid	bid
28	103
28	104
31	101
31	102
42	142
58	107

1	Berkeley cs186
1	cs186

sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



```
do {
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	sid	sname
	22	dustin
	28	уирру
	31	lubber
	31	lubber2
	44	guppy
-	58	rusty

sid	bid
28	103
28	104
31	101
31	102
42	142
58	107



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



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do {
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	sid	sname
	22	dustin
	28	уирру
	31	lubber
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sid	bid
28	103
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31	102
42	142
58	107



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102

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do {
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    mark = s
  if (r == s) {
    result = \langle r, s \rangle
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    mark = NULL
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sid	sname
22	dustin
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sid	bid
28	103
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42	142
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sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



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   mark = s
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    advance s
    return result
  else {
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    advance r
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```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

31
42
58

sid

bid

103

104

101

102

142

107



sid	sname	bid
28	yuppy	103
28	yuppy	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102



```
do {
 if (!mark) {
    while (r < s) { advance r }
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   mark = s
  if (r == s) {
    result = <r, s>
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  else {
    reset s to mark
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    mark = NULL
```

sid	sname
22	dustin
28	уирру
31	lubber
31	lubber2
44	guppy
58	rusty

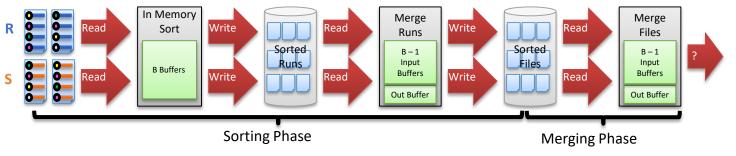
sid	bid
28	103
28	104
31	101
31	102
42	142
58	107



sid	sname	bid
28	уирру	103
28	уирру	104
31	lubber	101
31	lubber	102
31	lubber2	101
31	lubber2	102
58	rusty	107



Cost of Sort-Merge Join





- Cost: Sort R + Sort S + ([R]+[S])
 - But in worst case, last term could be |R| *[S] (very unlikely!)
 - Q: what is worst case?
- Question: How big does the buffer have to be to sort both R and S in two passes each?
- Suppose buffer B > $\sqrt{(\max([R], [S]))}$
 - Both R and S can be sorted in 2 passes
 - -4*1000 + 4*500 + (1000 + 500) = 7500