Communication in Shared and Distributed Memory

CS121 Parallel Computing Spring 2019



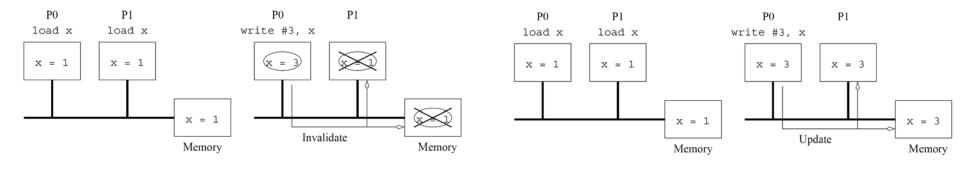
The cache coherence problem

- In shared memory systems, there is only one logical copy of each variable.
- However, if several processors want to access the variable, they can each store it in their cache, to avoid latency to access main memory.
- When one processor modifies the variable, other processors must be aware of the change.
- Since the variable is stored in multiple caches, the caches have be made coherent through some procedure / protocol.

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Cache coherence protocols

- Two main types of protocols, invalidate and update.
- Invalidate When one process modifies variable, all other cached copies and copy in memory are declared invalid.
 - If another process wants to access the variable, first process writes back new value to memory, and second process reads from memory.
- Update When one process modifies variable, it writes new value to other caches and memory.
- Invalidate and update tradeoff communication vs speed.
 - □ If other processes don't read the variable, update wastes communication.
 - If other processes do read the variable, invalidate causes stall for writeback and read.
- Since bandwidth is limited in parallel systems, most use invalidate.



Source: Introduction to Parallel Computing, Grama et al.



MSI protocol

- Invalidation based coherency protocol.
- The basis for widely used and higher performance protocols, e.g. MESI and MOESI.
- A variable X can be in the M (modified), S (shared) or I (invalid) state.
- When a processor performs an action (e.g. read or write), it may cause a state change and coherence messages to be sent to the main memory and all other processors.

MSI protocol

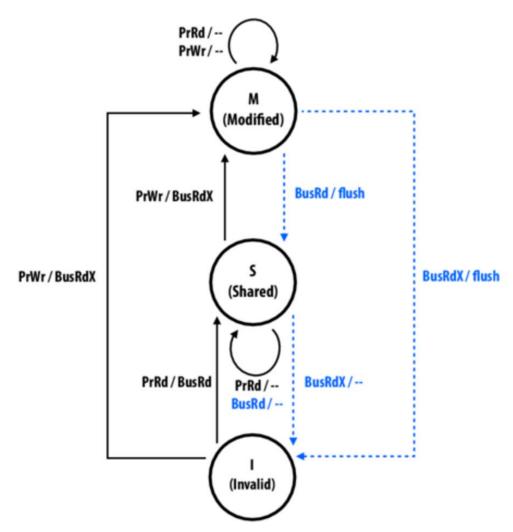
- S (shared): X may exist in multiple caches.
 - X's value hasn't changed since last time each processor read X from main memory.
 - All copies of X are up to date.
 - Processors can continue to read X from own caches.
- M (modified / dirty) state
 - □ A processor p changed its cached value of X.
 - □ p must inform other processors their cached X value now invalid.
 - □ p can still read / write to X in its own cache.
 - When p evicts X, must write back (flush) its latest value to main memory.
- I (invalid): Another processor has changed X's value.
 - ☐ This processor's value for X is out of date.
 - □ Must read X from main memory.
 - □ When reading X, will cause processor holding X in M state to first write its value to main memory.

MSI example

Time

Instruction at Processor 0	Instruction at Processor 1	Variables and their states at Processor 0		
				x = 5, D
				y = 12, D
read x		x = 5, S		x = 5, S
	read y		y = 12, S	y = 12, S
x = x + 1	y = y + 1	x = 6, D	y = 13, D	x = 5, I y = 12, I
read y			y = 13, S	y = 13, S
	read x	x = 6, S	x = 6, S	x = 6, S
x = x + y			x = 6, I	
	y = x + y	y = 13, I	y = 19, D	y = 13, I
x = x + 1		x = 20, D		x = 6, I
	y = y + 1		y = 20, D	y = 13, I





Source: http://15418.courses.cs.cmu.edu/spring2015content/lectures/10_cachecoherence1/

A / B: Input request A, output action B. Processor messages in black
Bus messages in blue.
PrRd: processor read request
PrWr: processor write request
flush: processor writes back data to memory
BusRdX: obtain copy with intent to modify
BusRd: obtain copy of var with no intent to
modify

Examples

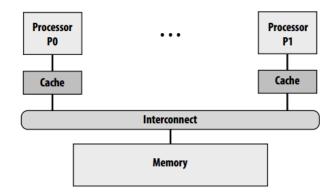
- □ Var currently shared. Proc writes new value (generates PrWr), leading to BusRdX msg.
 Proc goes to M state. All other procs (currently in S state) go to I state.
- □ Var currently dirty (last updated by proc in M state). Proc in I state wants to read var (generates PrRd), leading to BusRd msg. Proc in M state flushes current var value to memory. All procs go to S state.
- ☐ Proc in M state wants to read / write.

 Generates PrRd / PrWr local message, but no bus messages. Hence no coherence traffic.



Snoopy cache system

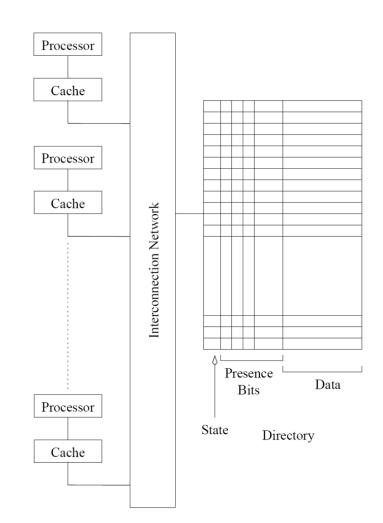
- MSI (and other protocols) can be implemented on different types of hardware.
- A basic (i.e. cheap) setup is a snoopy coherence protocol implemented on a bus or ring.
 - All processes listen on the bus for coherency traffic and respond accordingly.
 - Protocol works correctly because messages are broadcast on bus, so all processes hear all messages.
- If only one processor modifies a variable, all accesses are to its cache, and no coherence traffic ⇒ good performance.
- If multiple processors modify the variable, many flushes and coherency traffic ⇒ bus becomes performance bottleneck.





Directory cache system

- Based on observation that only processors with shared or dirty copy of variable need to hear its coherence messages.
- Keep a directory data structure in memory, indicating for each memory block which processors hold shared or dirty copies.
 - Given p procs, for each memory block use p bits indicating processors relevant for the block.





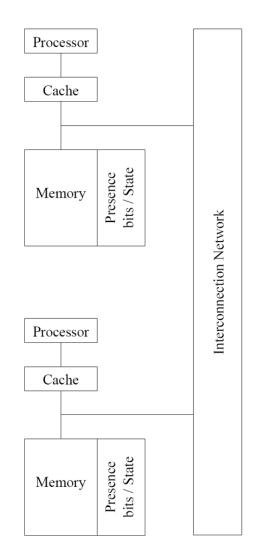
Example

- Initially several procs hold var X in S state. They're marked in X's presence bits in directory.
- Proc 0 modifies X. Main mem and all present procs besides proc 0 recv invalidate msg.
- All their presence bits for X are reset; only proc 0 still present in directory.
- Later (invalid) proc 1 reads X. Since proc 1 in I state, it reads directory, finds proc 0 in M state, and causes proc 0 to flush X.
- Procs 0 and 1 marked in directory in S state.



Distributed directory cache

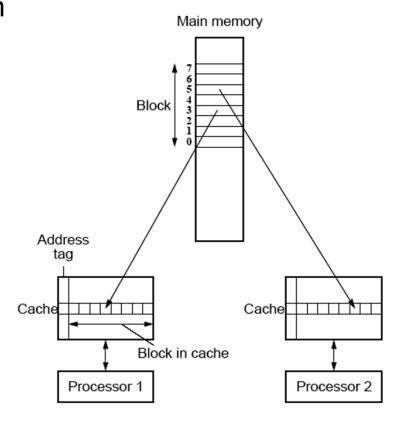
- Since directory stored in memory, all coherency traffic access memory, which becomes bottleneck.
- Also, directory needs large O(mp) amount of storage, m = # memory blocks, p = # processors.
- To improve performance, distribute directory among the processors.
 - Each processor handles a fixed memory range, and stores directory for the range.
 - Processor needing directory info on a var queries processor responsible for the var.





False sharing

- Data transferred into / from cache in units of cache lines (aka blocks).
 - □ Typical L1 cache line size is 64-128B.
 - Multiple words fit into one cache line.
- Processors accessing different words can access same cache line.
 - If one processor modifies cache line, other processors with same cache line must be updated or invalidated.
- Solution is (try to) lay out data so data accessed by different processors in different lines.
 - □ Padding.
 - □ Wastes precious cache space.





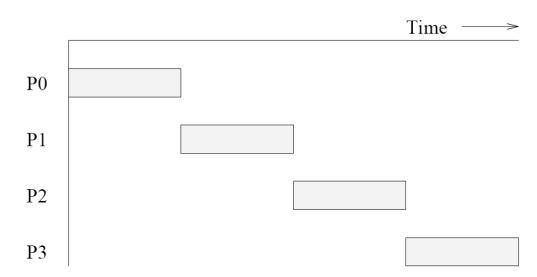
Communication costs

- First consider cost in message passing systems, then shared memory.
- Time to transfer a message of size m from one node to another consists of
 - □ Startup time t_s: Prepare message header, error correction, running routing protocol, interfacing with router, etc.
 - Once per message.
 - □ Per hop time t_h: Used by router to determine next hop.
 - □ Per word transfer time t_w: If bandwidth is r, per word transfer time from source to dest is 1/r.



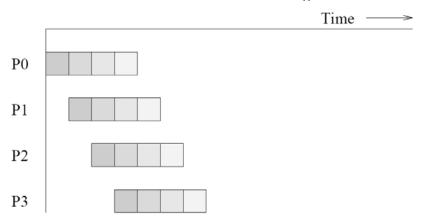
Store and forward routing

- Each intermediate node waits to receive entire message before forwarding it to next hop on path.
- Takes m t_w+t_n time per link, so for I links t_s+ l(m t_w+t_n) total time.
 - \Box t_h small compared to m t_w, so time is \approx t_s+ I m t_w.



Packet routing

- Break large message into small packets.
- Intermediate node can receive a packet as soon as it finishes forwarding previous packet it received.
 - □ Pipeline parallelism.
- Also lets packets take different routes, and easier error correction.
 - ☐ Essential for Internet, with unpredictable network state, high error rates.
- But overhead from each packet's routing info, error correction, sequence number etc.
- Total time $t_s + t_h I + t_w m$.
 - \Box First packet arrives at time $t_s + t_h I + t_w$.
 - □ Remaining m-1 packets arrive every t_w time.





Cut-through switching

- Similar to packet routing, but optimized for parallel computers.
- Messages take same path. No routing info.
- Small (~ 32B) flits (flow control digits) transmitted at high rate.
 - ☐ First flit (header) is allocated path by switches / routers. Remaining (body and tail) flits follow same path.
- Simple, per message (instead of per packet) error correction.
- To reduce latency for high priority flits (e.g. cache lines), use multilane cut-through routing.
- Also called virtual cut-through. A related technique is wormhole routing.

Overall cost model

- Total communication time depends on data volume m and number of hops l.
- However, programmer has little control over I.
 - Usually can't control process to processor mapping.
 - Many systems use randomized two step routing to minimize congestion: first send message to random node, then send it to destination.
 - \square Per hop time t_h usually small compared to t_s or m t_w .
- Communication time can be simplified to t_s+m t_w.
- Assumes uncongested network.
 - □ If congestion on link is c, i.e. c messages are sent over the link, time becomes t_s + c m t_w.
- **Ex** \sqrt{p} x \sqrt{p} mesh where nodes randomly communicate with each other.
 - □ Across a bisection there are O(p) communications.
 - \square But mesh bisection width is \sqrt{p} .
 - □ So some link carries $O(p) / \sqrt{p} = O(\sqrt{p})$ messages.
 - □ So communication time is $t_s + O(\sqrt{p} \text{ m } t_w)$.

b/A

Comm cost in shared memory

- Shared memory communication costs are more unpredictable.
 - Memory layout determined by system. Hard to estimate amount of local / remote memory accesses.
 - Cache thrashing depends on scheduling and process allocation.
 - Coherency traffic, spatial locality and false sharing also very nondeterministic.
- But to first order, still model communication time as t_s + t_wm.
 - □ t_s and t_m are much smaller in shared memory than distributed memory architectures.



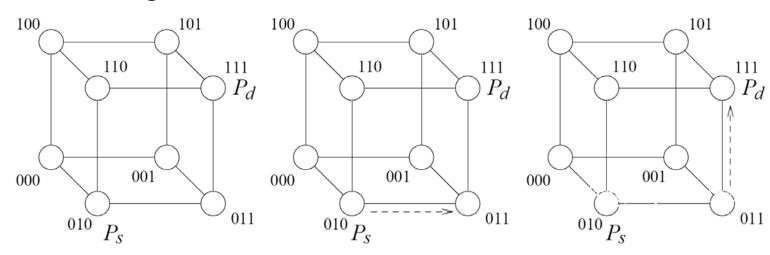
Routing

- We saw interconnection networks such as mesh, hypercube, tree, etc. How do processes communicate on these networks?
- Routing algorithm selects a path between two communicating processes.
- Routes are ideally short, uncongested and easy to compute. But tradeoffs exist.
 - Ex Short (minimal) routes may be more congested.
 - □ Ex Deterministic, i.e. fixed given source and destination, or adaptive, i.e. route around congestion.

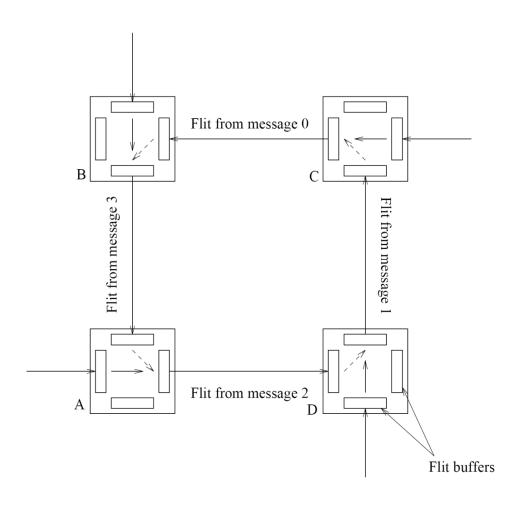


Dimension and E-cube routing

- Dimension routing for a k-dim mesh orders the dimensions (e.g. XYZ) and routes messages in order of dimension.
- E-cube routing does dimension routing on dimensions of a hypercube.
 - □ Let s, d be bit representations of source and destination.
 - □ Compute r = s XOR d, and from least to most significant digit of r, route along dimensions with 1-bit.
- Ex Routing from 010 to 111.



Deadlocks

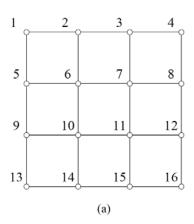


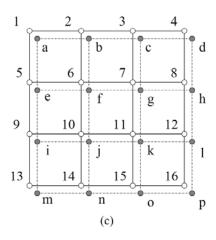
- Dimension and E-cube routing prevent deadlocks.
- Ex Without dimension routing.
 - \square A \rightarrow D \rightarrow C, D \rightarrow C \rightarrow B, C \rightarrow B \rightarrow A, B \rightarrow A \rightarrow D
 - A's flit can't move from AD to DC, because DC is occupied by D's flit.
 - D's flit can't move from DC to CB, because CB is occupied by C's flit. Etc.
- With XY routing
 - \square A \rightarrow D \rightarrow C, D \rightarrow A \rightarrow B, C \rightarrow B \rightarrow A, B \rightarrow C \rightarrow D.
 - □ A and C's flits first move along X dim, then B and D's flits.

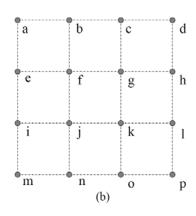


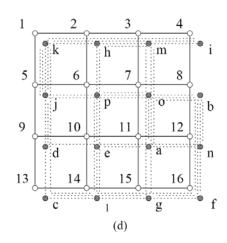
Process-processor mappings

- Process communication pattern determined by the program.
- Processor communication pattern determined by the hardware.
- To run a program on a piece of hardware, must map processes to processors.
- Poor mappings can cause communication bottlenecks, reduce performance.
- Ex (a) and (b) show processor and process communication patterns.
 - Mapping (c) causes no bottlenecks.
 - Mapping (d) creates bottlenecks at links 15, 23, etc.









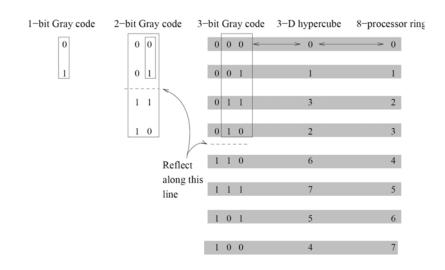


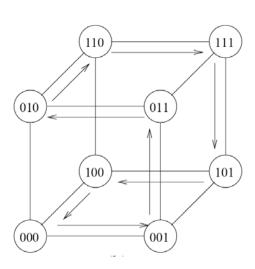
Embeddings

- Give a map f from the graph P of process communication to graph R of processor communication pattern.
 - □ Each process of P maps to a processor in R.
 - □ Each edge from p_1 and p_2 in P maps to a shortest path between $f(p_1)$ to $f(p_2)$ in R.
- Congestion is max number of routing paths that cross an edge in R.
 - \square Ex On previous example congestion = 5, e.g. on edge (1,5).
- Dilation is max length of route between any two neighbors in P.
 - \square Ex On previous example dilation = 5, e.g. for edge (b,c).
- Expansion is (# processes) / (# processors).
 - □ Assume for simplicity it is 1.

Line to hypercube

- Map size 2^k line graph into k-dim hypercube.
- Gray codes An ordering of k digit binary numbers where consecutive values differ in one digit.
 - Recursive construction Let G_{k-1} be a k-1 digit Gray code. Prepend G_{k-1} with 0. Then take another G_{k-1} , reverse it and prepend with 1. Concatenate the two copies.
- Map node i in line graph to node G_k(i) in hypercube.
- i and i+1 are mapped to neighbors in hypercube.
 - \Box $G_k(i)$ and $G_k(i+1)$ differ in one bit, so are connected in hypercube.
 - □ So dilation is 1.
- Each hypercube edge is mapped onto by at most one line graph edge.
 - □ So congestion is 1.

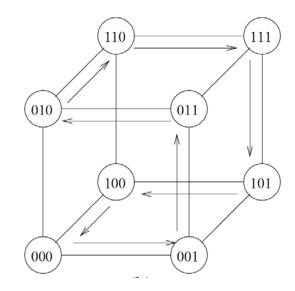






Hypercube to line

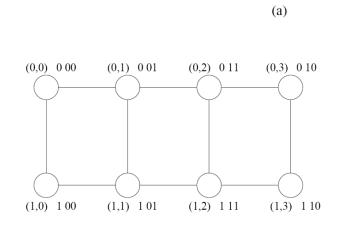
- To map k-dim hypercube into size 2^k line graph, just use the reverse mapping, i.e. node i in hypercube maps to $G_i^{-1}(i)$ in line.
- To compute congestion, recall bisection width of k-dim hypercube is 2^{k-1}.
 - ☐ Bisection width of line is 1.
 - □ Thus, 2^{k-1} edges of the hypercube need to cross the middle edge of the line graph, and the congestion is 2^{k-1}.
- Dilation is $\Theta(2^k)$, e.g. from node 0 to node 2^{k-1} .

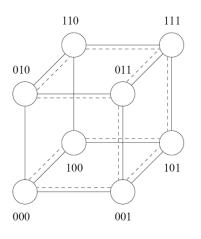


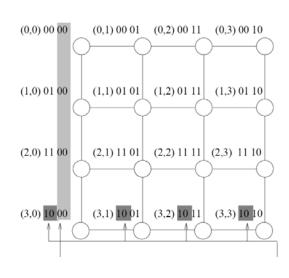
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2D mesh to hypercube

- Map a $2^r \times 2^s$ mesh into an (r + s)-dim hypercube.
- Map node (i, j) in mesh to node G_r(i) || G_s(j) in hypercube.
 - Neighbors in the mesh map to nodes that differ in one bit, i.e. neighbors in the hypercube.
 - □ So dilation and congestion are both 1.
- Note that different rows and columns of the mesh map to distinct sub-hypercubes.



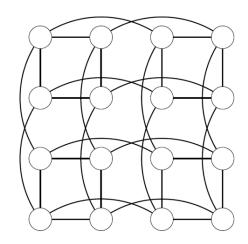


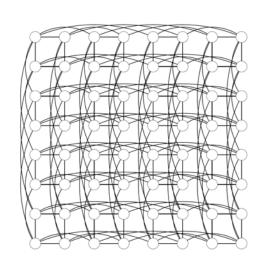




Hypercube to 2D mesh

- Map (log p)-dim hypercube into \sqrt{p} x \sqrt{p} mesh.
 - □ Assume \sqrt{p} for simplicity is a power of 2, and let $q = \log \sqrt{p} = (\log p) / 2$.
- If we fix last q binary digits of the nodes in hypercube, we get another q-dim hypercube.
 - Ex Take 4-dim hypercube, and fix last two digits to 10. Then get another hypercube (0010, 0110, 1110, 1010).
- For each q digit binary number r, map the hypercube from fixing the last q digits in hypercube to row r of mesh.
 - ☐ Use the hypercube to line mapping.
 - □ Congestion is $\sqrt{p}/2$.
- For each q digit binary number r, map the hypercube from fixing the first q digits in hypercube to column r of mesh.
- Congestion in rows and column independent. So overall congestion is $\sqrt{p}/2$.

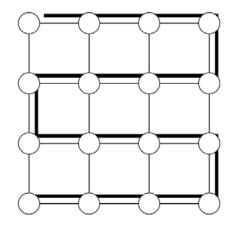


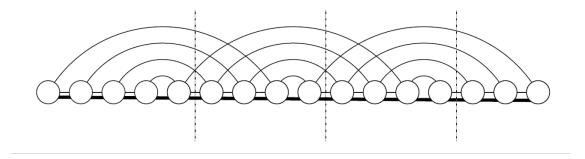




Line and mesh

- Line maps into mesh using zig-zag embedding.
 - □ Congestion and dilation are 1.
- To map mesh to line, invert the mapping.
- For a \sqrt{p} x \sqrt{p} mesh, congestion is \sqrt{p} .
 - □ Every two consecutive rows must traverse edge connecting them in the line graph.
- Dilation is $2\sqrt{p} 1$, between the first nodes in consecutive rows.





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Cost performance tradeoffs

- Cost of a network can be measured in terms of e.g. number of wires, bisection width (complexity), etc.
- Wire complexity Square p node mesh has with O(log p) wires per link has same cost as p node hypercube.
- Average distance in mesh is $O(\sqrt{p})$, and in hypercube is $O(\log p)$.
- With O(log p) wires per link in mesh, t_w gets reduced by O(log p) factor.
 - □ Avg latency in mesh is $t_s + O(t_h \sqrt{p}) + O(m t_w / log p)$.
 - \square Avg latency in hypercube is $t_s + O(t_h \log p) + m t_w$.
 - □ For fixed number of processors and large message size, m
 t_w >> t_h, so mesh has lower latency.
- Hypercube better under contention, since it has much greater bisection width.