

Problem 1(10pts): True or False: For each statement, choose T if the statement is correct, otherwise, choose F.

Fill all the answers in the table below.

Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9	Q10

- (1) Every full binary tree is also a complete binary tree.
- (2) There are n elements inserted one by one into an initially empty binary heap. The total time complexity is $O(n \log n)$.
- (3) A full binary tree with n non-leaf nodes contains $2n - 1$ total nodes.
- (4) A binary tree of height $h = 0$ is perfect.
- (5) We have a binary heap of n elements and wish to add n more elements into it while maintaining the heap property. It can be done in $O(n)$.
- (6) In a binary max-heap containing n numbers, the smallest element can be found in time $O(n)$.
- (7) If a binary tree is a min-heap, then the post-order traversal of this tree is descending.
- (8) If the post-order traversal of a complete binary tree is descending, then the binary tree is a min-heap.
- (9) If the pre-order traversal and post-order traversal of two binary trees are equal respectively, then the two binary trees are exactly the same.
- (10) In a binary tree, every non-root node has exactly one parent.

Problem 2(9pts) Fill in the blanks.

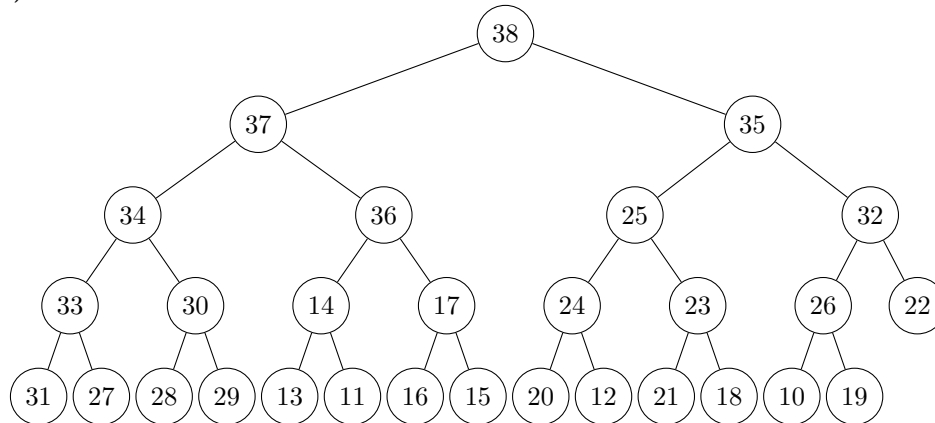
- (1) The maximum number of nodes in a binary tree of height h is _____
- (2) In a binary min-heap with n elements, we can only access the top of the heap. The 7^{th} smallest element can be found in time $O(\text{_____})$ if duplicated elements are not allowed.
- (3) In a binary min-heap with n elements, we can access the array storing the heap. The 7^{th} smallest element can be found in time $O(\text{_____})$ if duplicated elements are not allowed.
- (4) (3pts) The elements 32, 15, 20, 30, 12, 25, 33 are inserted **one by one** in the given order into a **max-heap**. Please represent the final heap as an array (in-place).

0	1	2	3	4	5	6

Problem 3(6pts) Given the in-order and post-order traversal of a binary tree T are $ADHGKLMRUXTW$ and $AHDLKGUXRWTM$ respectively.

Draw the tree T and write the pre-order traversal of T .

Problem 4(6pts)



- (1) (1pt) Is this heap a max-heap or a min-heap?
- (2) (3pts) Suppose that you do a **pop** operation on the heap above. Write down all the elements that need to be compared in the operation.
- (3) (3pts) Suppose that inserting the key x was the last operation performed in the binary heap in the figure. That is, after inserting x , the heap is shown as the figure above. Write down all possible value of x .