

Quiz 2  
Week 2  
CS 280: Fall 2020  
Instructor: Xuming He

Name:  
On your left:  
On your right:

**Instructions:**

Please answer the questions below. Show all your work. This is an open-book test. NO discussion/collaboration is allowed.

Problem 1. (10 points)

Consider the perceptron algorithm and let us re-write the weight updates as follows

$$\begin{aligned}\text{Initialization: } \mathbf{w}_1^+ &= \mathbf{w}_1^- = 0 \\ \text{Mistakes on positive: } \mathbf{w}_{t+1}^+ &= \mathbf{w}_t^+ + \mathbf{x} \\ \text{Mistakes on negative: } \mathbf{w}_{t+1}^- &= \mathbf{w}_t^- - \mathbf{x} \\ \text{Weight update: } \mathbf{w}_{t+1} &= \mathbf{w}_{t+1}^+ + \mathbf{w}_{t+1}^-\end{aligned}$$

If the inputs are images from two categories: apple (positive) and banana (negative). What would the final weights of  $\mathbf{w}_T^+$  look like as an image after  $T$  iterations, and why? What about  $\mathbf{w}_T^-$ ?

$T = 0$ ,  $\mathbf{w}_T = \mathbf{w}_0^+ + \mathbf{w}_0^- = 0$  and it makes mistake.

$T \geq 1$ , if an apple image  $\mathbf{x}_{\text{apple}}$  is given,  $\mathbf{w}_{t+1}^+ = \mathbf{w}_t^+ + \mathbf{x}_{\text{apple}}$ ,  $\mathbf{w}_{t+1}^- = \mathbf{w}_t^-$  +4

if a banana image  $\mathbf{x}_{\text{banana}}$  is given,  $\mathbf{w}_{t+1}^- = \mathbf{w}_t^- - \mathbf{x}_{\text{banana}}$ ,  $\mathbf{w}_{t+1}^+ = \mathbf{w}_t^+$

Thus,  $\mathbf{w}_T^+$  will look like an apple after iterations. +3

Similarly,  $\mathbf{w}_T^-$  will look like an inverse banana.

Therefore,  $\mathbf{w}_T$  will look like an image of an apple subtract a banana. +3

Consider a multiclass logistic regression with L2 regularization as follows:

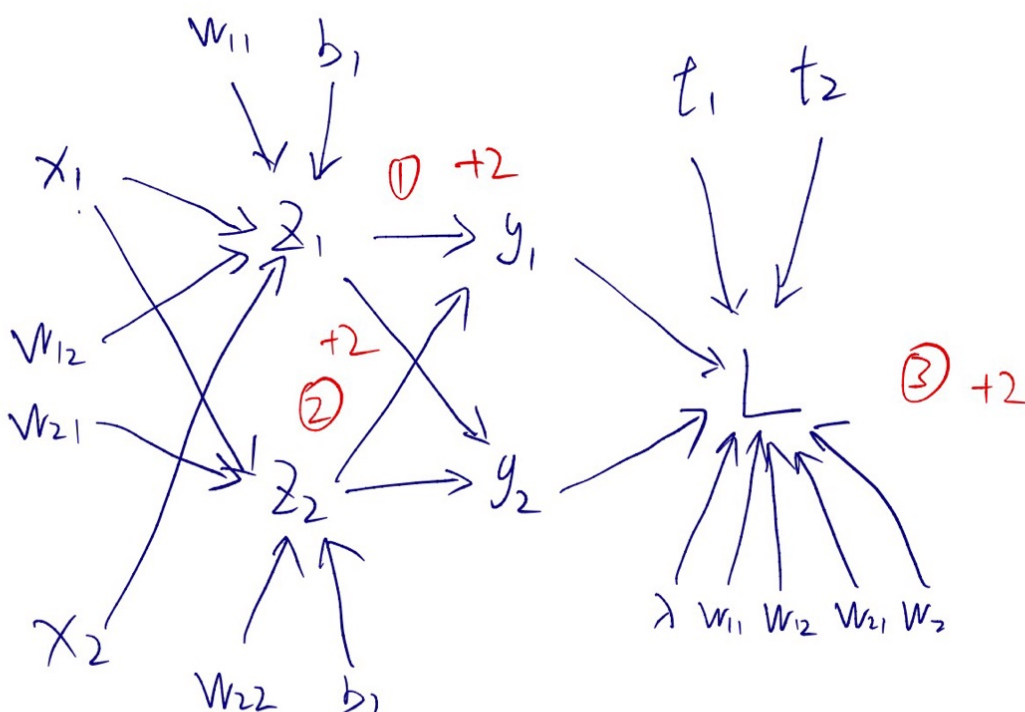
$$z_l = \sum_{j=1}^2 w_{lj} x_j + b_l, \quad l = 1, 2$$

$$y_k = \frac{e^{z_k}}{\sum_l e^{z_l}}, \quad k = 1, 2$$

$$\mathcal{L} = - \sum_k t_k \log y_k + \lambda \sum_{l=1}^2 \sum_{j=1}^2 \|w_{lj}\|^2$$

Draw a computational graph for this network and its loss. Note each node should be a scalar in this graph. Write down the forward pass based on the graph you have built.

①对+b, ①②③处关键节点 输入输出有错-2



$$z_1 = w_{11} x_1 + w_{12} x_2 + b_1$$

$$z_2 = w_{21} x_1 + w_{22} x_2 + b_2$$

$$y_1 = \frac{e^{z_1}}{\sum_i e^{z_i}} \quad y_2 = \frac{e^{z_2}}{\sum_i e^{z_i}}$$

$\mathcal{L}$  = 照抄题目即可...

+ 4 forward 过程