CS 101 Fall 2021 - Quiz 1-B

9/28/2021 - 25 Minutes **Name:** **ID number:** **Score:**

Remember that your work is graded on the quality of your writing and explanation as well as the validity.

Problem 1 (5pts) Notes of discussion

I promise that I will complete this QUIZ independently, and will not use any electronic products or paper-based materials during the QUIZ, nor will I communicate with other students during this QUIZ.

True or False: I have read the notes and understood them.

1

Problem 2(10pts) Stack and Queue

(1) (6 Points) Suppose there is an initially empty stack with the capacity 7, then we do a sequential of 7 `push` and 7 `pop` operations. If the order of the element pushed in the stack is 1 2 3 4 5 6 7, then for each order of the popped elements listed below, tick a "✓" in the box if it could be existing.

2 4 6 5 7 3 1	☐
7 6 4 5 3 1 2	☐
1 3 5 2 6 4 7	☐
1 2 3 4 7 5 6	☐
5 3 4 6 2 7 1	☐
2 4 5 6 3 7 1	☐

(2) (4 Points) Suppose there is an initially empty queue with capacity 7 which is implemented by an array (viewed circularly). Show the array after the following operations being operated and indicate the place of the front and back of the queue.

(a) Enqueue(1) Enqueue(2) Enqueue(3)
Dequeue()
Enqueue(4) Enqueue(5) Enqueue(6) Enqueue(7) Enqueue(8)
Dequeue()
Enqueue(4)
Dequeue()

____

(b) Enqueue(1) Enqueue(2) Enqueue(3) Enqueue(4) Enqueue(5)
Dequeue()
Enqueue(3) Enqueue(2) Enqueue(1)
Dequeue() Dequeue() Dequeue() Dequeue()
Enqueue(1)
Dequeue()

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Problem 3(5pts) Algorithm Design

(1) Try to convert the polynomial below into the array form which is talked in the class. Note the exponents should be descending.

$$2200x^{2800} + 4396x^{777} + 443x$$

index	0	1	2
coefficient			
exponent			

(2) Try to do addition on the two polynomial A and B below and store the result in C. Each polynomial is stored in the struct PLY.

```
struct PLY {
    int coefficient[VERY_LARGE];    // denote the coefficient of each item
    int exponent[VERY_LARGE];       // denote the exponent of each item, descending
    int len;                        // denote the total number of items
};

PLY add(const PLY &A, const PLY &B) {
    PLY C;
    int i = 0;
    int j = 0;
    int k = 0;
    while (i < A.len or __________) {
        if (______________ or ___________ and A.exponent[i] > B.exponent[j]) {
            C.exponent[k] = A.exponent[i];
            C.coefficient[k] = A.coefficient[i];
            k++;
            i++;
        } else if (i >= A.len or j < B.len and A.exponent[i] < B.exponent[j]) {
            C.exponent[k] = B.exponent[j];
            C.coefficient[k] = B.coefficient[j];
            k++;
            j++;
        } else if (A.exponent[i] == B.exponent[j]) {
            C.exponent[k] = B.exponent[j];
            C.coefficient[k] = ____________________________________________________;
            k++;
            i++;
            j++;
        }
    }
    C.len = k;
    return C;
}
```

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Problem 4(16pts) Asymptotic Analysis

(1) (10') Order the following functions so that for all i, j, if f_i comes before f_j in the order then $f_i = \Omega(f_j)$. Do **NOT** justify your answers.

- $f_1(n) = n!$
- $f_2(n) = 3^{\log_2 n}$
- $f_3(n) = 2^{\sqrt{n}}$
- $f_4(n) = \log_2 n$
- $f_5(n) = \frac{1}{3}^n$
- $f_6(n) = 3^n$
- $f_7(n) = 2^{\log_2 10n}$
- $f_8(n) = 1000$
- $f_9(n) = n^{\frac{1}{3}}$
- $f_{10}(n) = \sqrt{n}$

As an answer you may just write the functions as a list, e.g. $f_8, f_9, f_1, \cdots$

(2) (6') For each pair of functions $f(n)$ and $g(n)$, give your answer whether $f(n) = o(g(n))$, $f(n) = \omega(g(n))$ or $f(n) = \Theta(g(n))$. Give a **proof** of your answers.

- $f(n) = \log x$ and $g(n) = n^{\epsilon}, \forall \epsilon > 0$

- $f(n) = n!$ and $g(n) = n^n$