Quiz 3

Week 3 Sept/29/2021

CS 280: Fall 2021

Instructor: Lan Xu

Name:

On your left:
On your right:

Instructions:

Please answer the questions below. Show all your work. This is an open-book test. NO discussion/collaboration is allowed.

Problem 1. Convolution Kernel (10 points)

We have a video sequence and we would like to design a 3D convolutional neural network to recognize events in the video. The frame size is 32x32 and each video has 30 frames. Let's consider the first convolutional layer.

• We use a set of 3x3x3 convolutional kernels. Assume we have 64 kernels and apply stride 2 in spatial domain and temporal domain, what is the size of output feature map? Use proper padding if needed.

$$T \times H \times W \qquad 30 \times 32 \times 32 = m_0 \times m_1 \times m_2$$

$$k = 3 \times 3 \times 3 \qquad S = 2 \times 2 \times 2$$

$$O_i = \left[\frac{m_i + 2 \times P_i - d_i \times (k_i - U - I)}{S_i} + I \right]$$
the shape of output is $k \times 0 \times 0 \times 0 \times U_2$

$$Take the zero padding! 2 \qquad clearly tell$$

$$1 \times 30 \times 32 \times 32 \qquad bullet = clearly tell$$

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Problem 2. Adam (10 points)

Explain why the bias correction is needed in the Adam update. Hint: You should derive the update rule for t=1.

1) what is bias correction

W/O bias correction

$$M_0, V_0 = 0, 0$$

$$\begin{aligned} M_{t} &= \beta_{1} M_{t-1} + (l-\beta_{1}) g_{t} \\ V_{t} &= \beta_{2} V_{t-1} + (l-\beta_{2}) g_{t}^{2} \end{aligned} \qquad \begin{array}{l} \text{bias correction} \\ m_{t} \leftarrow \frac{m_{t}}{l-\beta_{t}} \\ V_{t} \leftarrow \frac{V_{t}}{l-\beta_{2}^{t}} \end{aligned}$$

(2) for t=1

$$m_1 = \beta_1 \cdot o + (1-\beta_1) g_1$$
 $\widehat{m}_1 = \frac{m_1}{1-\beta_1} = g_1$

$$\widehat{m}_{l} = \frac{m_{l}}{1-\beta_{l}} = g_{l}$$

$$V_1 = \beta_1 \cdot 0 + (1-\beta_2)g_1^2$$
 $\hat{V_1} = \frac{V_1}{1-\beta_2} = g_1^2$

$$\hat{V}_1 = \frac{V_1}{1-\beta_2} = g_1^2$$

 $\theta_1 = \theta_0 - \alpha \frac{\hat{m}_1}{\sqrt{V_1} + b}$ Core idea: too, the estimate m_t (for g_t) and V_t (for g_t)

(3) Explanation is biased towards mo (and V_0). Bias correction corrects when $t \to \infty$,

the bias by α $m_t = \beta m_{t-1} + (1-\beta)g_t$ factor of $\frac{1}{1-\beta t}$ if $E[m_t] \to 0$ $E[m_t] \to 0$ $E[m_t] \to 0$

$$\therefore M_{t} = \beta^{t} M_{0} + (-\beta) \sum_{i=0}^{t-1} \beta^{i} \mathcal{G}_{t-i}$$

$$E[M_t] = (\Gamma\beta) \cdot E[g_t] \xrightarrow{|\Gamma|} (I-g^t) + \beta^t \cdot E[m_0] = E[g_t] + \frac{\beta^t}{|\Gamma|} \cdot E[m_0]$$

$$= (\Gamma\beta^t) E[g_t] + \beta^t \cdot E[m_0] \quad \text{if initialize with } m_0 = 0.$$

$$\beta \in (0,1), \beta^{t} \rightarrow 0$$

mt is an unbiased estimate for 9t.

when to n

mt is biased towards mo

1 However, Let
$$\widehat{m}_t = \frac{m_t}{\Gamma \beta t}$$

$$E[m_0] = E[g_t] + \frac{\beta^2}{1-\beta^4} \cdot E[m_0]$$
1. If instead [7] with $m_0 = 0$.