



Lecture 15: Attention Model and Transformer

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Fall, 2020

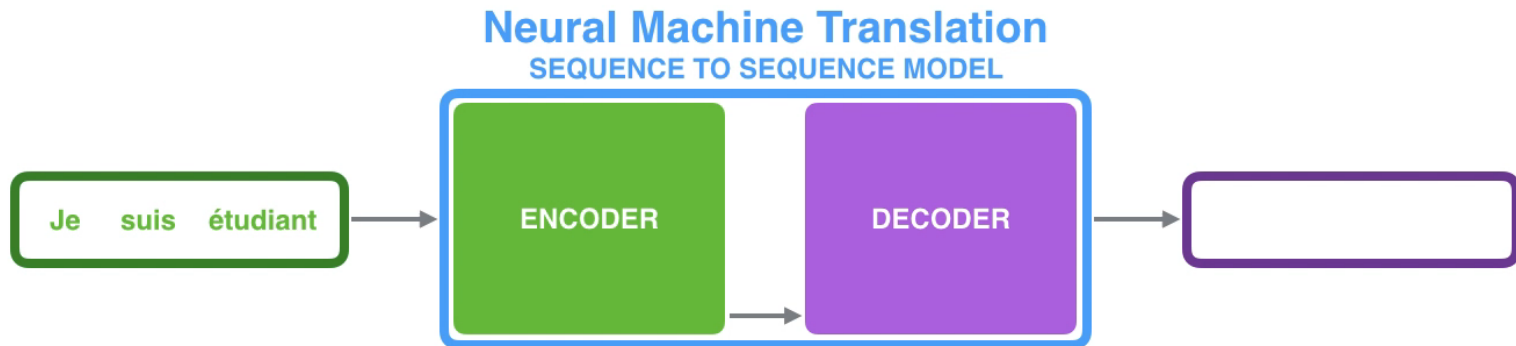
Outline

- Recap and motivation
- Attention models in RNNs
- Transformer

Acknowledgement: Hugo Larochelle's, Mehryar Mohri@NYU's, Yingyu Liang@Princeton's, Bhiksha Raj@CMU's & Feifei Li@Stanford's course notes

Recap

- RNN models
 - Encoder-decoder architecture



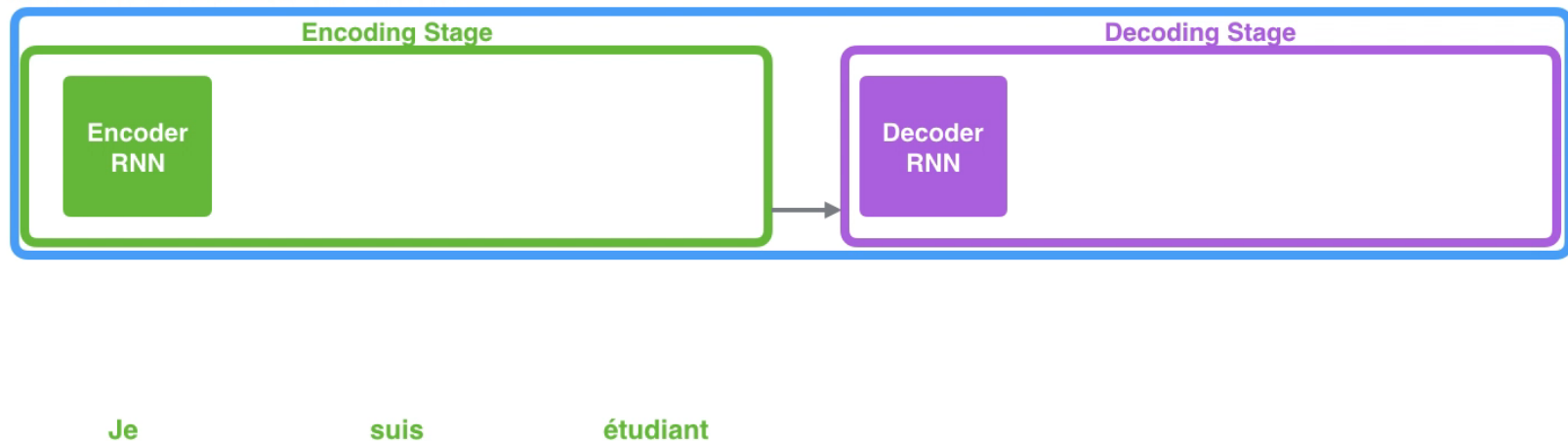
<https://jalammar.github.io/visualizing-neural-machine-translation-mechanics-of-seq2seq-models-with-attention/>

Recap

- RNN models
 - Encoder-decoder architecture

Neural Machine Translation

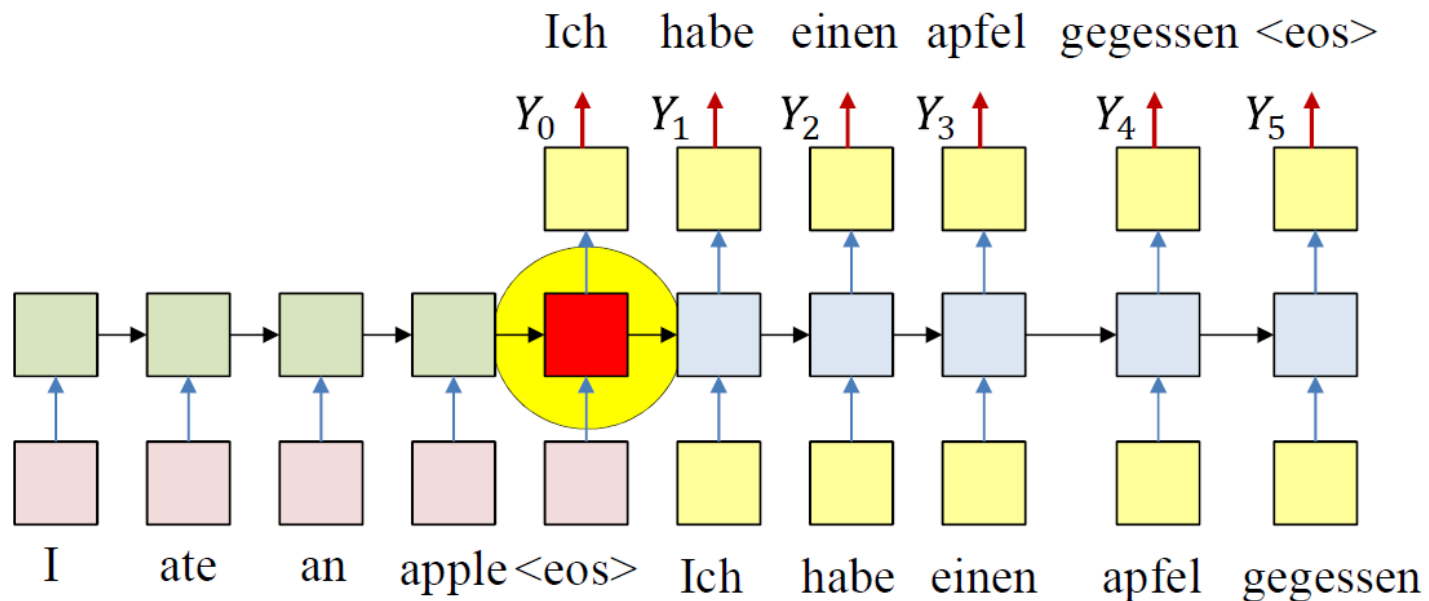
SEQUENCE TO SEQUENCE MODEL



<https://jalammar.github.io/visualizing-neural-machine-translation-mechanics-of-seq2seq-models-with-attention/>

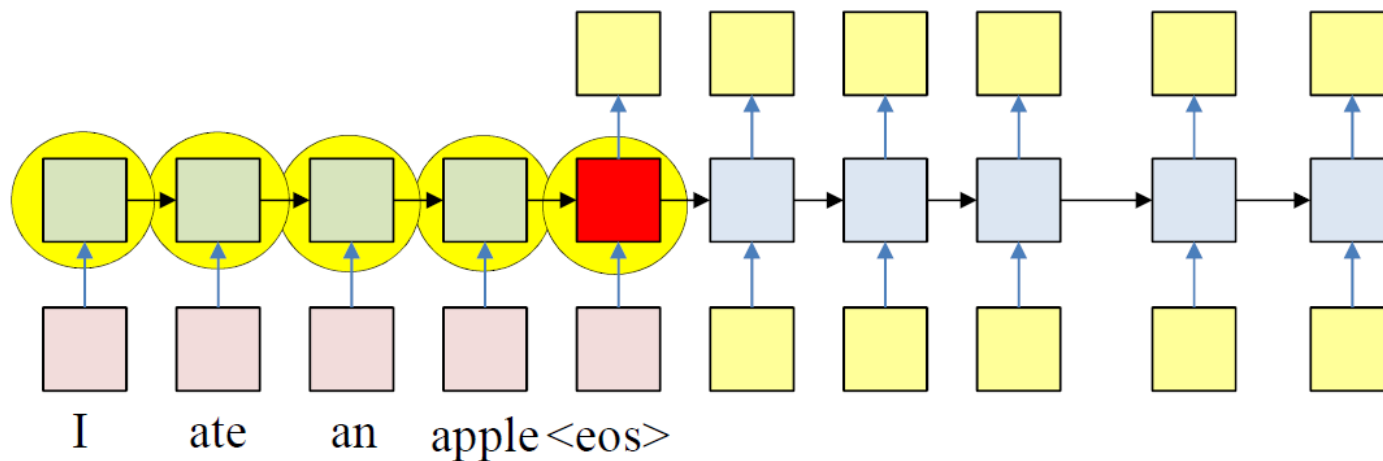
A problem with this framework

- All the information on the input sequence is embedded into a single vector
 - The latent layer at the end of the input sequence
 - This layer is overloaded with information



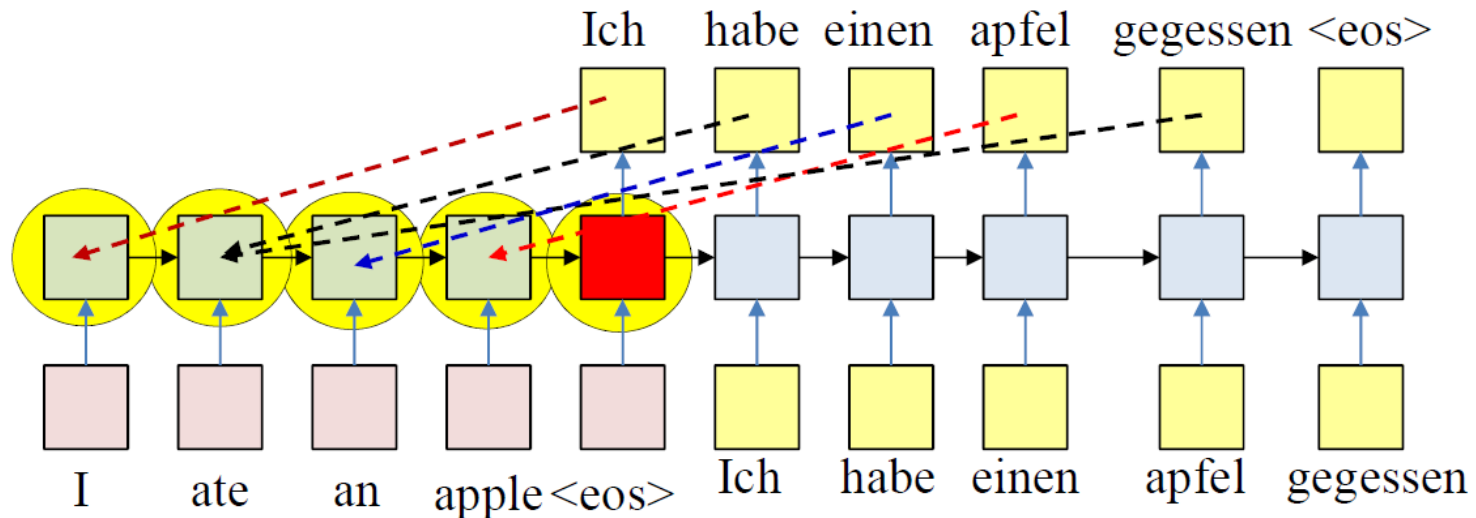
A problem with this framework

- All latent values carry information
 - Some of which may be diluted downstream



A problem with this framework

- All latent values carry information
 - Some of which may be diluted downstream
 - Different outputs are related to different inputs



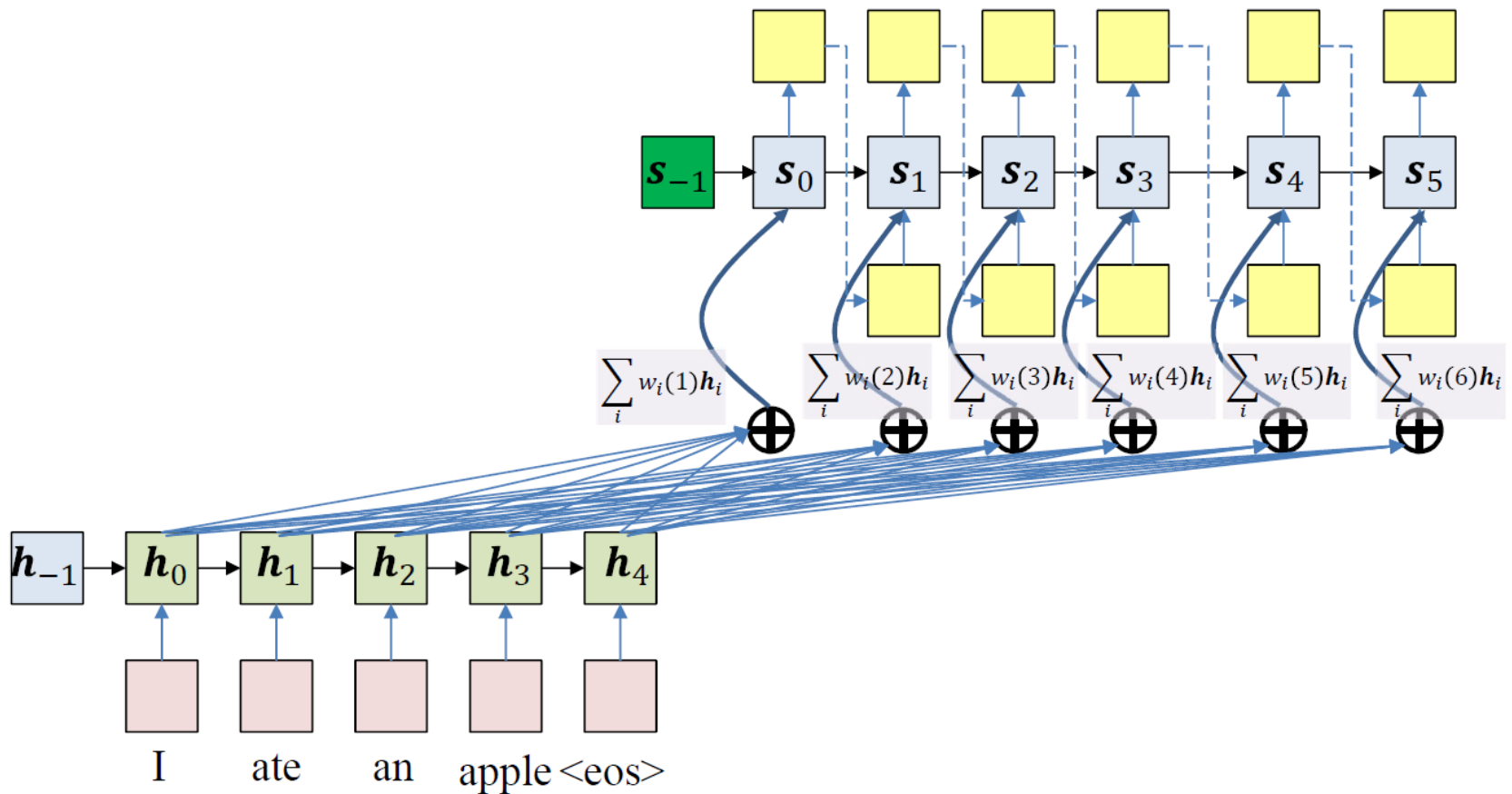
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Attention models

- Compute a weighted combination of all the hidden outputs into a single vector

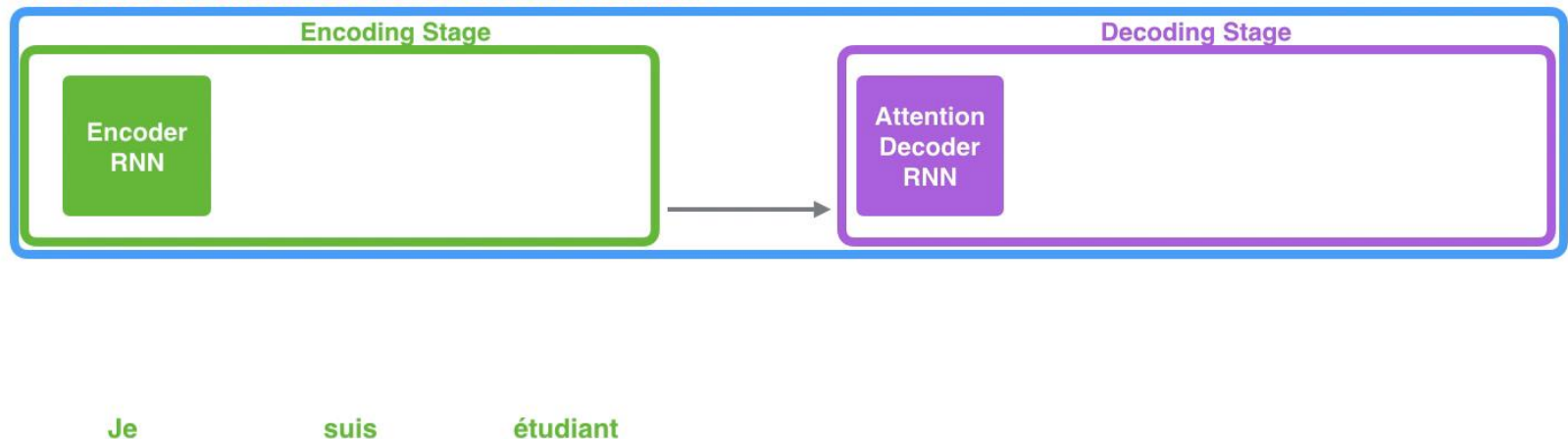


Attention models

- Compute a weighted combination of all the hidden outputs into a single vector

Neural Machine Translation

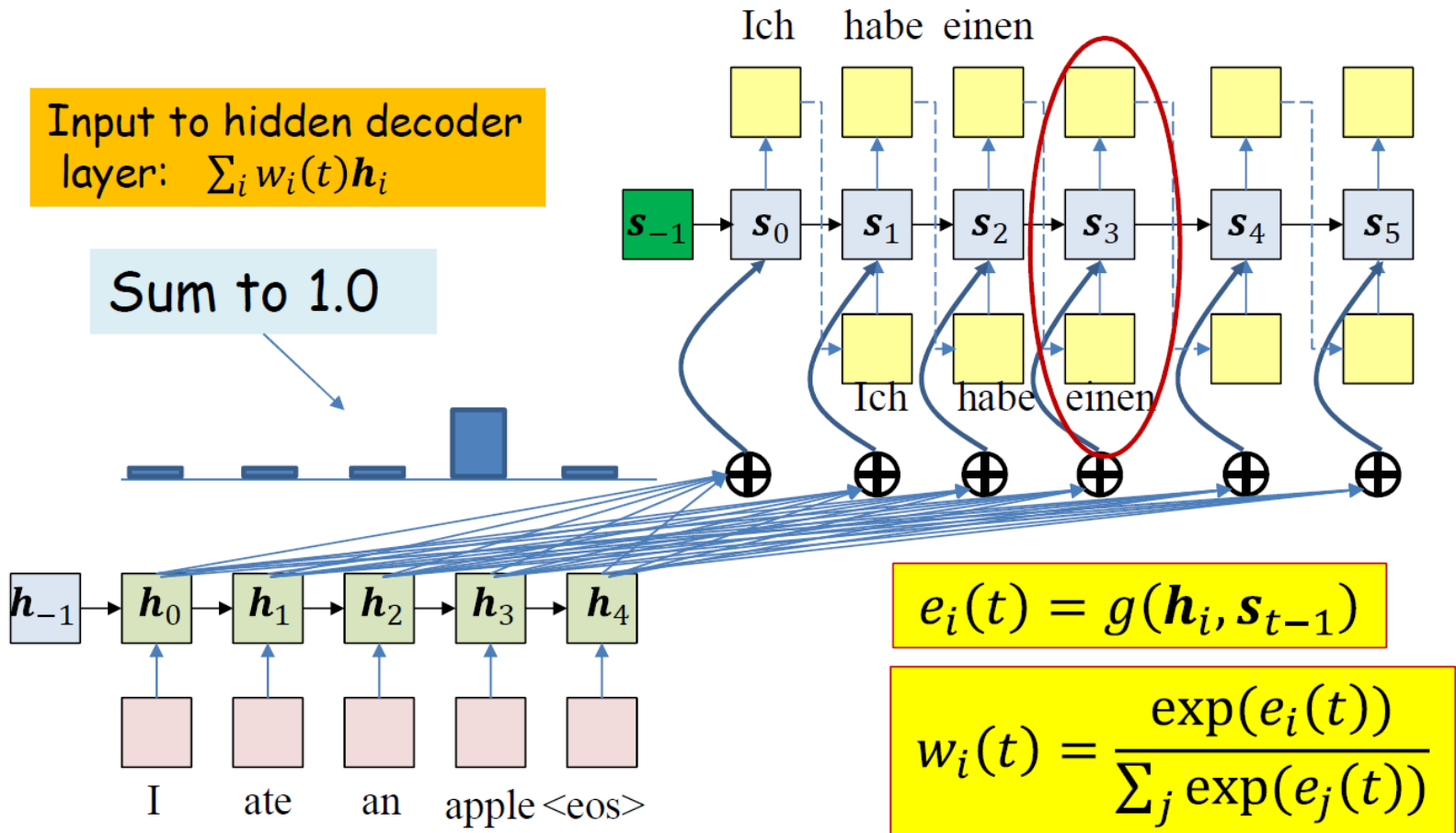
SEQUENCE TO SEQUENCE MODEL WITH ATTENTION



<https://jalammar.github.io/visualizing-neural-machine-translation-mechanics-of-seq2seq-models-with-attention/>

Attention models

- The weights are a distribution over the input
 - A function $g()$ on two hidden states followed by a softmax



Attention models

- Compute a weighted combination of all the hidden outputs into a single vector

Attention at time step 4

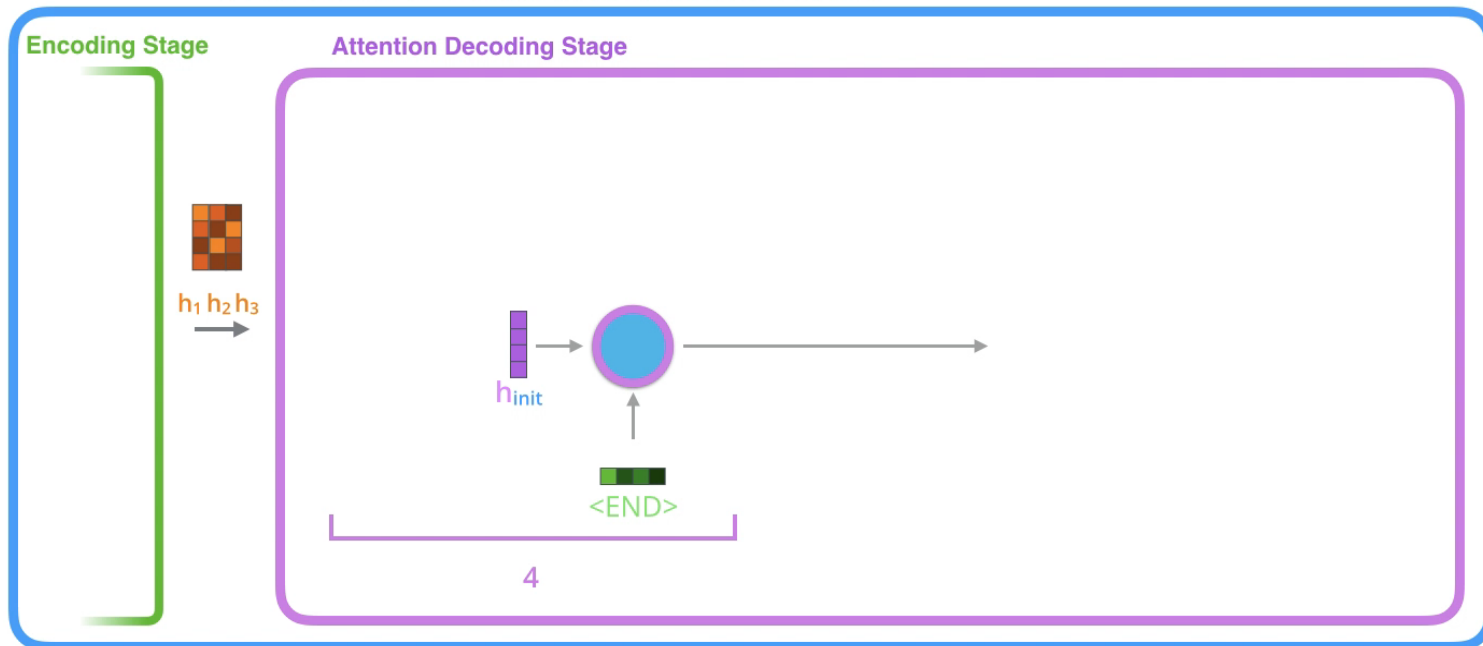


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Attention models

- Compute a weighted combination of all the hidden outputs into a single vector

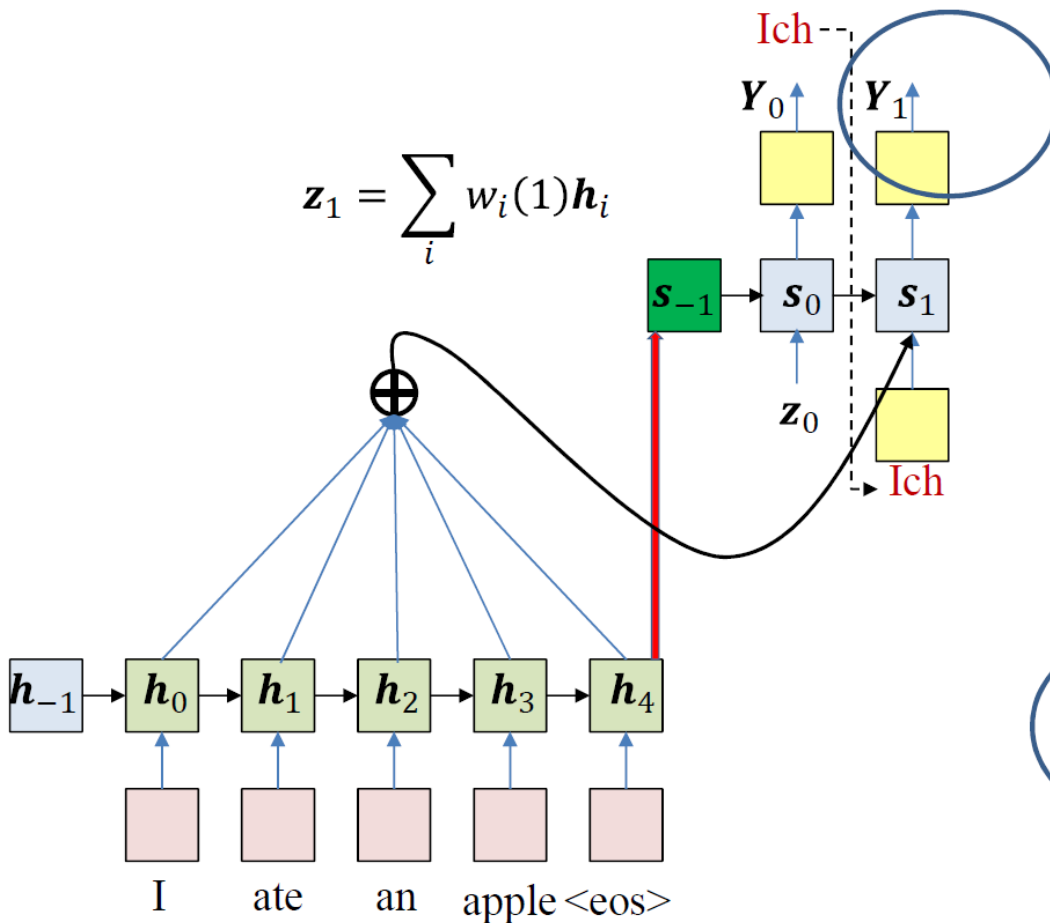
Neural Machine Translation SEQUENCE TO SEQUENCE MODEL WITH ATTENTION



<https://jalammar.github.io/visualizing-neural-machine-translation-mechanics-of-seq2seq-models-with-attention/>

What does the attention learn?

- The key component of this model is the attention weight
 - It captures the relative importance of each position in the input to the current output



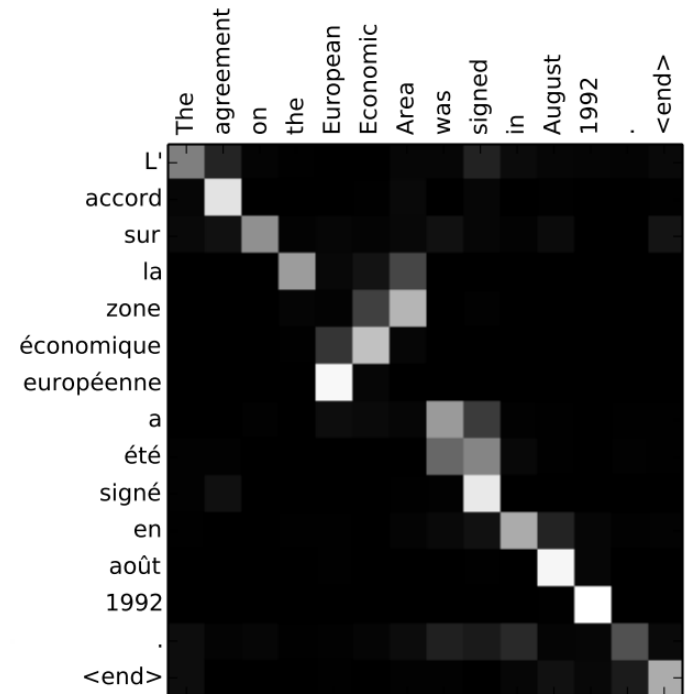
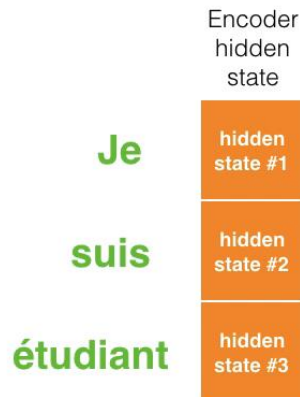
$$g(\mathbf{h}_i, \mathbf{s}_0) = \mathbf{h}_i^T \mathbf{W}_g \mathbf{s}_0$$

$$e_i(1) = g(\mathbf{h}_i, \mathbf{s}_0)$$

$$w_i(1) = \frac{\exp(e_i(1))}{\sum_j \exp(e_j(1))}$$

Attention models

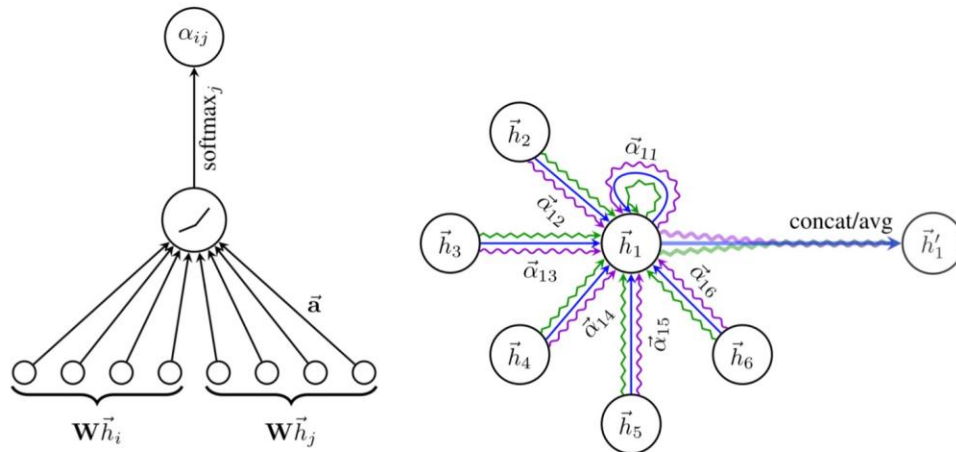
- Compute a weighted combination of all the hidden outputs into a single vector



<https://jalammar.github.io/visualizing-neural-machine-translation-mechanics-of-seq2seq-models-with-attention/>

Graph Neural Networks (GNNs) with **Attention**

Monti et al. (CVPR 2017), Hoshen (NIPS 2017), Veličković et al. (ICLR 2018)

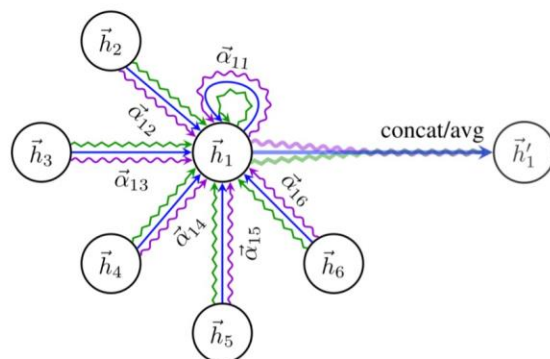
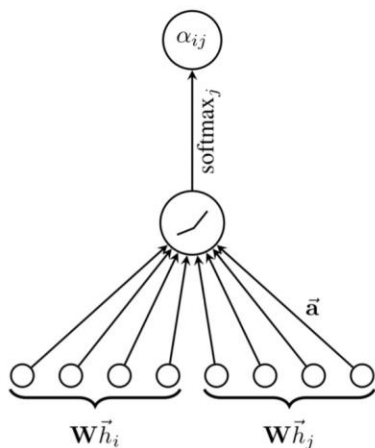


[Figure from Veličković et al. (ICLR 2018)]

$$\vec{h}'_i = \sigma \left(\frac{1}{K} \sum_{k=1}^K \sum_{j \in \mathcal{N}_i} \alpha_{ij}^k \mathbf{w}^k \vec{h}_j \right)$$

Graph Neural Networks (GNNs) with Attention

Monti et al. (CVPR 2017), Hoshen (NIPS 2017), Veličković et al. (ICLR 2018)



[Figure from Veličković et al. (ICLR 2018)]

Pros:

- No need to store intermediate edge-based activation vectors (when using dot-product attn.)
- Slower than GCNs but faster than GNNs with edge embeddings

Cons:

- (Most likely) less expressive than GNNs with edge embeddings
- Can be more difficult to optimize

$$\vec{h}'_i = \sigma \left(\frac{1}{K} \sum_{k=1}^K \sum_{j \in \mathcal{N}_i} \alpha_{ij}^k \mathbf{W}^k \vec{h}_j \right) \quad \alpha_{ij} = \frac{\exp \left(\text{LeakyReLU} \left(\vec{\mathbf{a}}^T [\mathbf{W}\vec{h}_i \| \mathbf{W}\vec{h}_j] \right) \right)}{\sum_{k \in \mathcal{N}_i} \exp \left(\text{LeakyReLU} \left(\vec{\mathbf{a}}^T [\mathbf{W}\vec{h}_i \| \mathbf{W}\vec{h}_k] \right) \right)}$$

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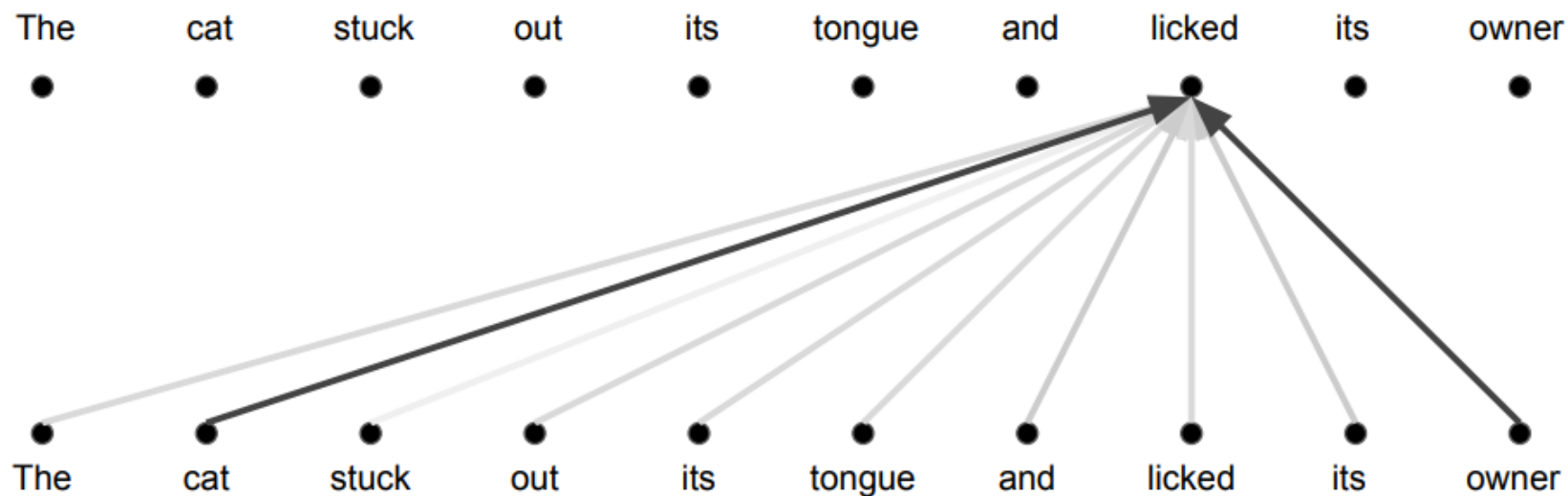
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Limitations of RNNs

- RNNs involve sequential computation
 - Cannot parallelize = time-consuming
- RNNs “forget” past information
 - LSTM helps to some degree, but not too long
 - No explicit modeling of long and short range dependencies

Self-Attention

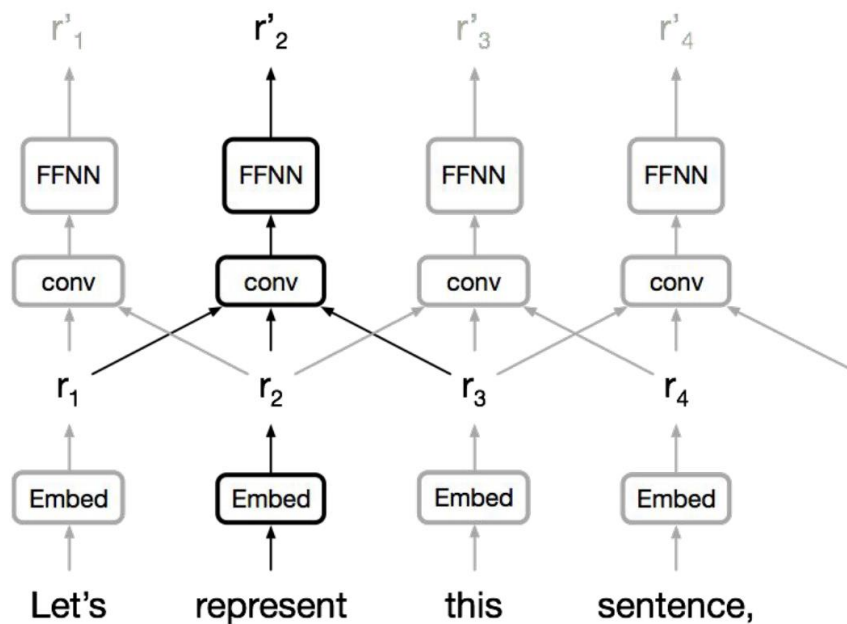
- Use (self-)attention as representation?



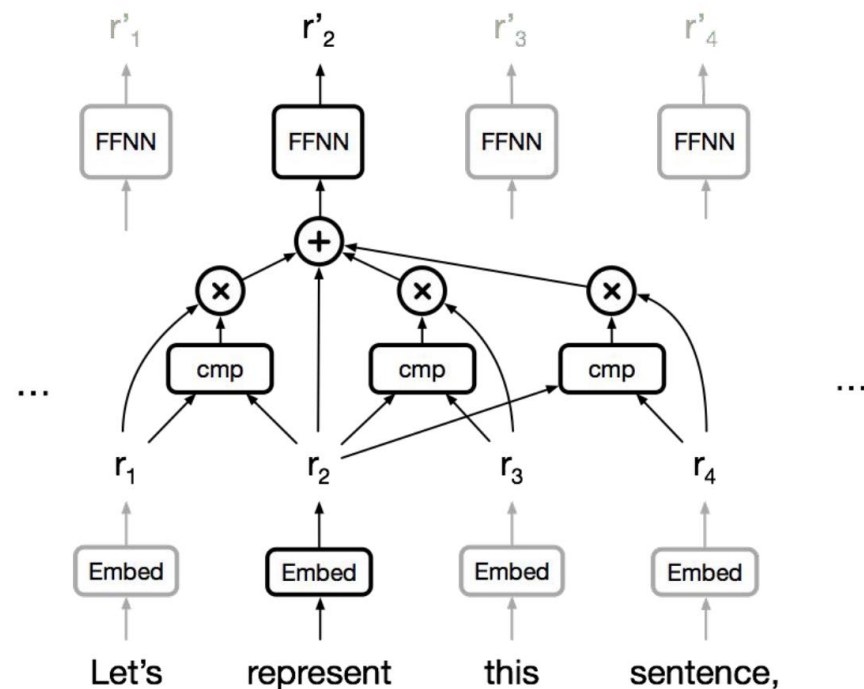
Self-Attention

- Use (self-)attention as representation?

CNN

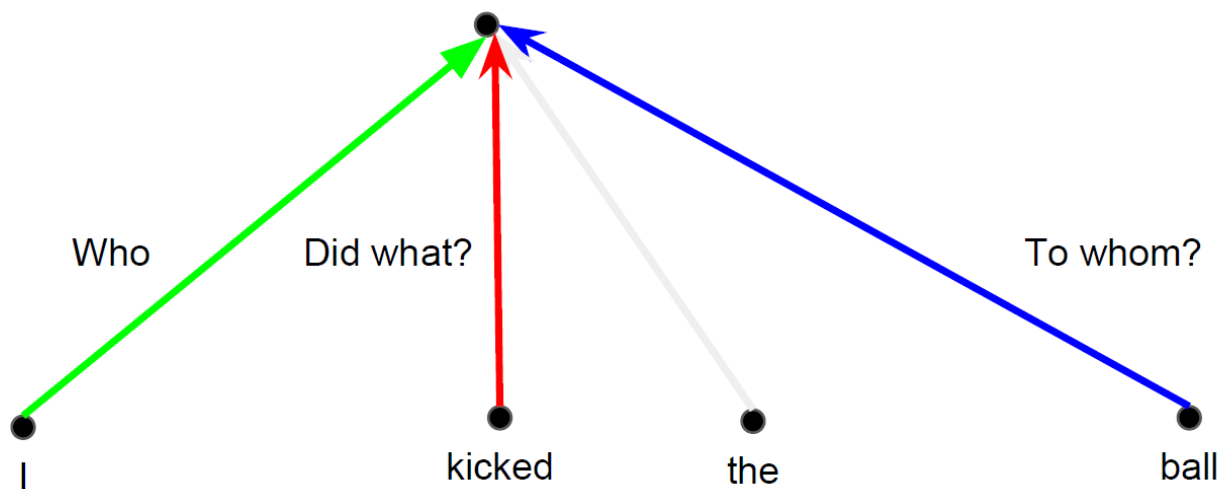


Self-attention



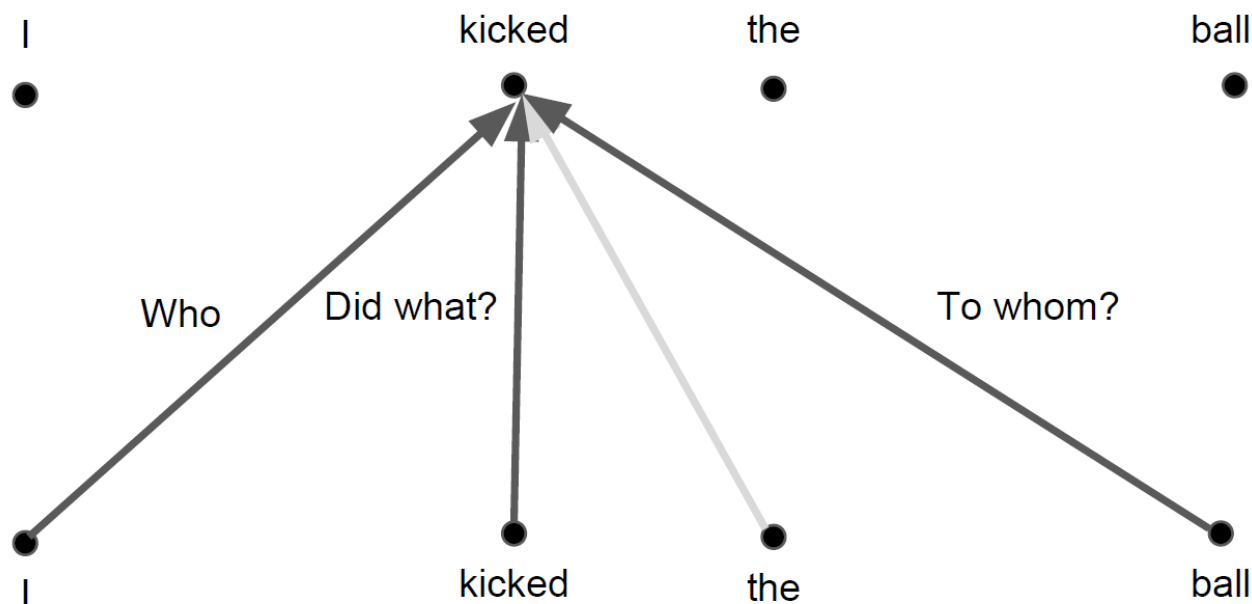
Convolution

- Convolution as representation



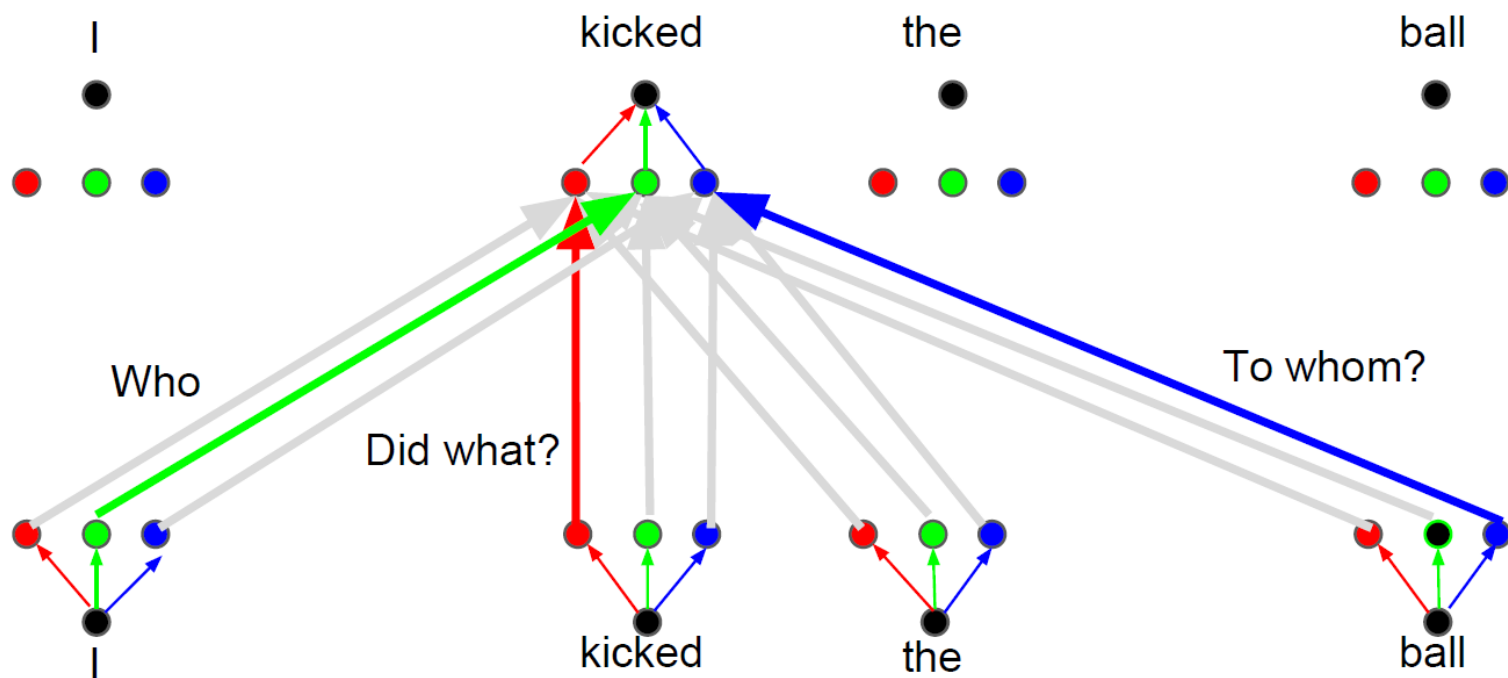
Self-Attention

- Self-attention as representation



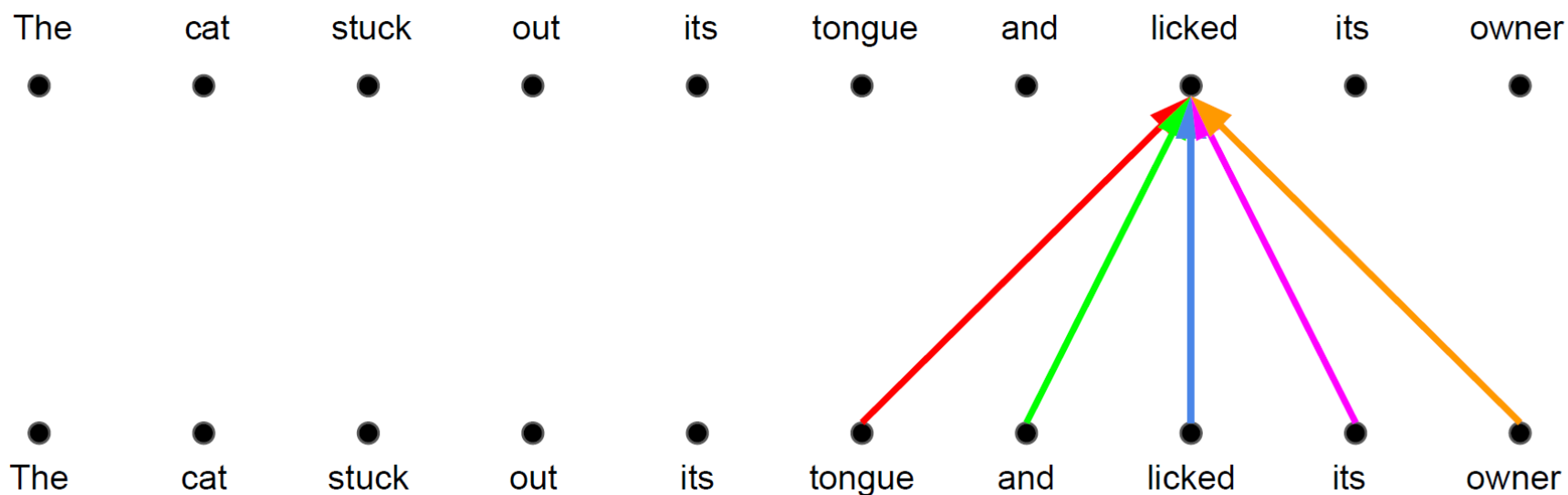
Self-Attention

■ Parallel attention heads



Convolution

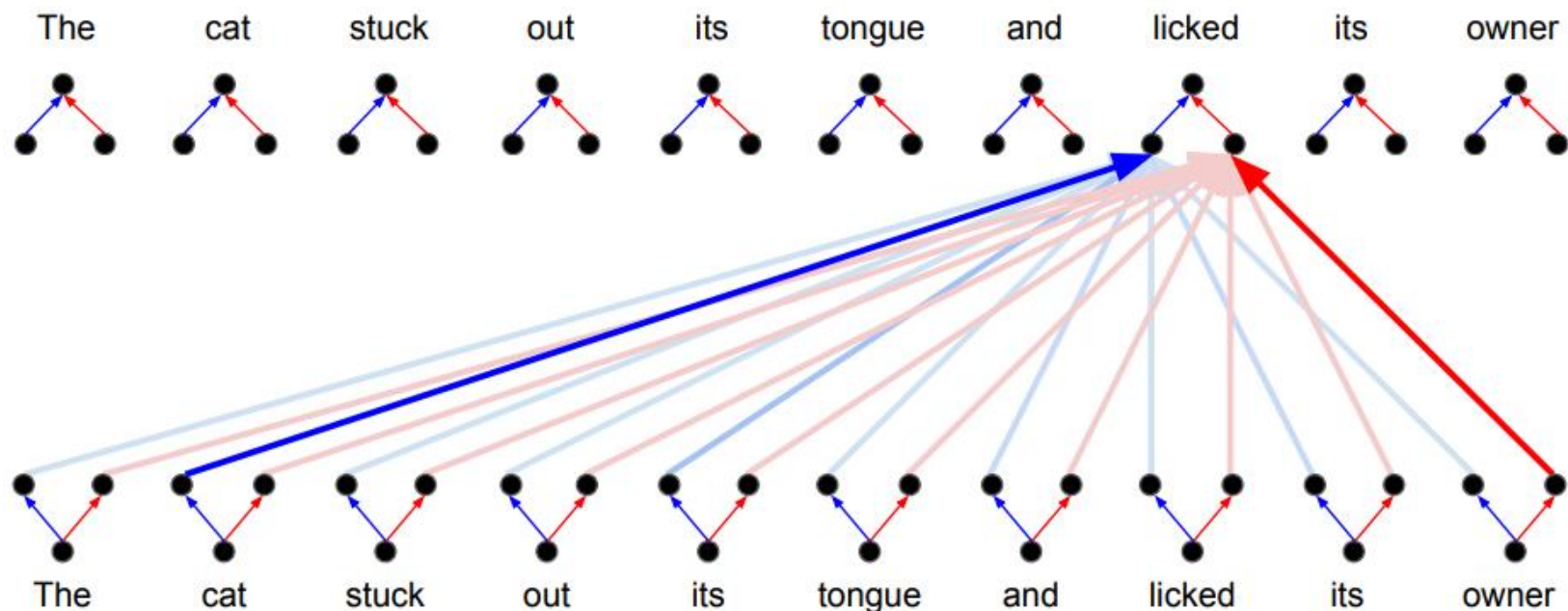
- Different linear transformations by relative position



Self-Attention

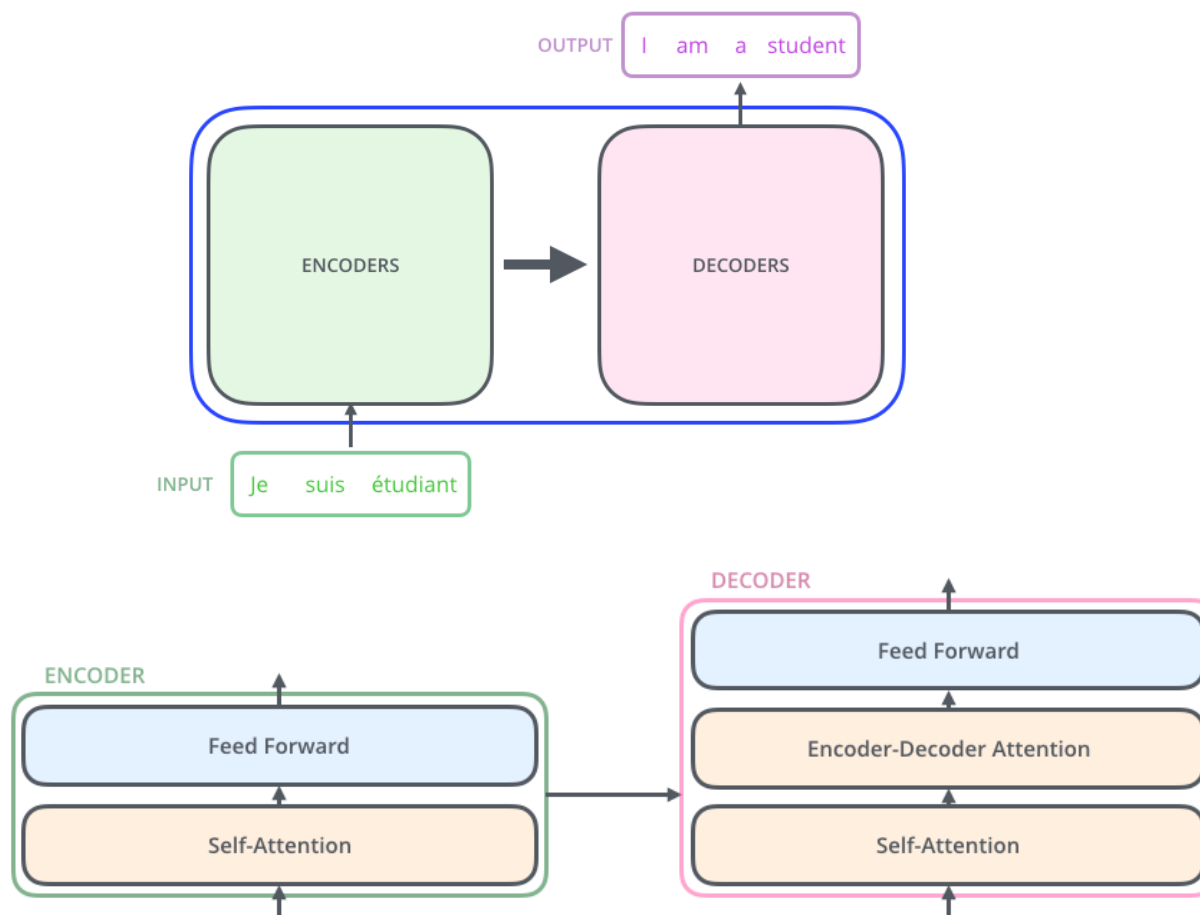
■ Multi-head attention

- Parallel attention layers with different linear transformations on input and output.



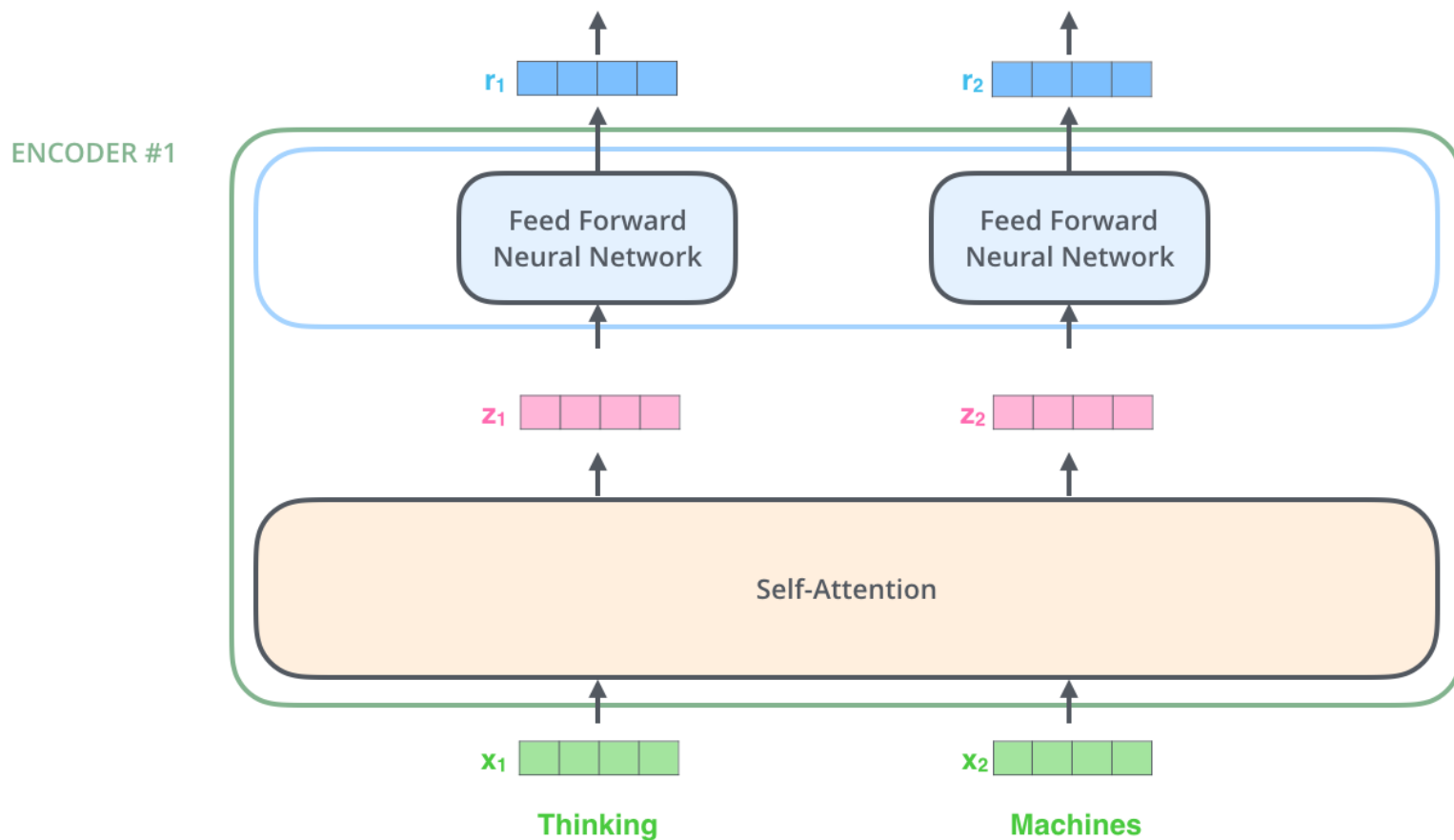
The Transformer

- Encoder-decoder network



The Transformer

■ Encoder network



The Transformer

■ Self-attention

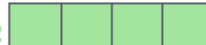
Input

Thinking


Machines

Embedding

x_1 

x_2 

Queries

q_1 


q_2 



W^Q

Keys

k_1 

k_2 



W^K

Values

v_1 

v_2 

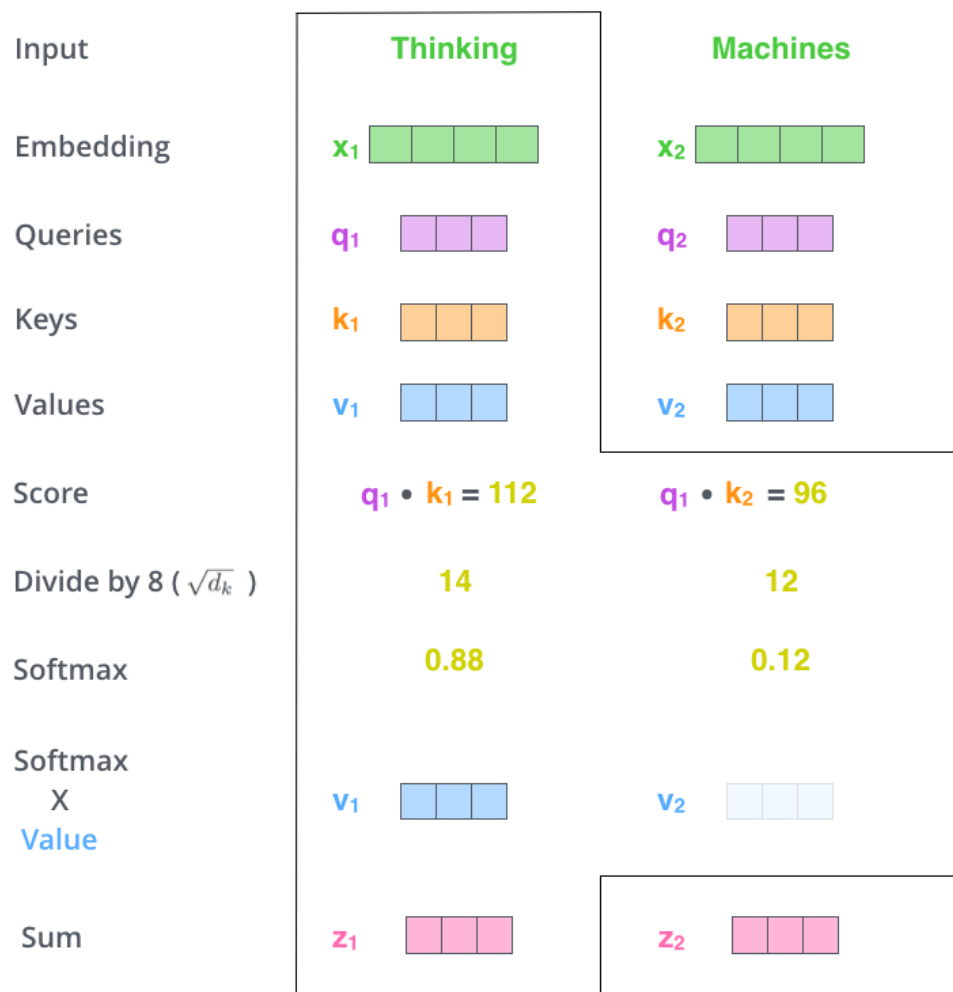


W^V

<http://jalammar.github.io/illustrated-transformer/>

The Transformer

■ Self-attention



The Transformer

■ Self-attention in matrix calculation

$$\begin{matrix} \text{X} \\ \begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline \end{array} \end{matrix} \times \begin{matrix} \text{W}^{\text{Q}} \\ \begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline \end{array} \end{matrix} = \begin{matrix} \text{Q} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix}$$

$$\begin{matrix} \text{X} \\ \begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline \end{array} \end{matrix} \times \begin{matrix} \text{W}^{\text{K}} \\ \begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline \end{array} \end{matrix} = \begin{matrix} \text{K} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix}$$

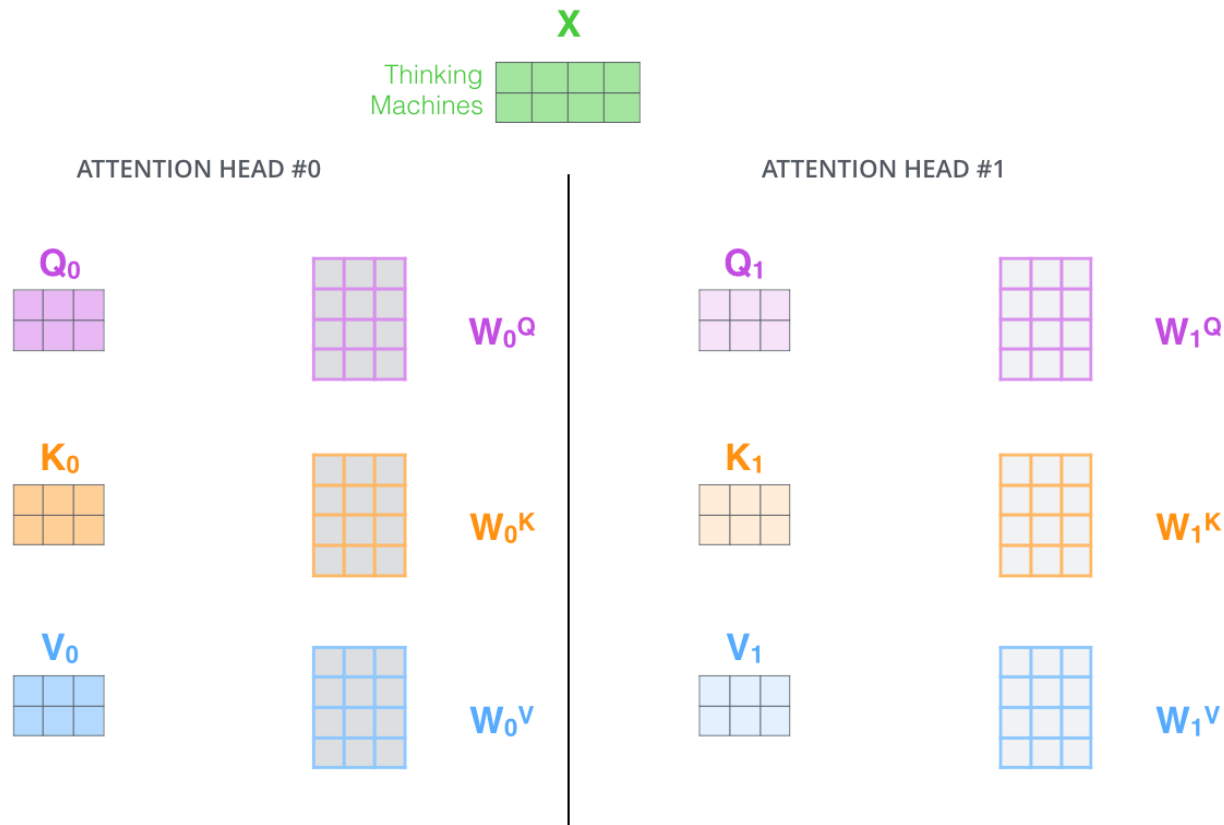
$$\begin{matrix} \text{X} \\ \begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline \end{array} \end{matrix} \times \begin{matrix} \text{W}^{\text{V}} \\ \begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline \end{array} \end{matrix} = \begin{matrix} \text{V} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix}$$

$$\begin{aligned} & \text{softmax} \left(\frac{\begin{matrix} \text{Q} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix} \times \begin{matrix} \text{K}^{\text{T}} \\ \begin{array}{|c|c|} \hline & \\ \hline & \\ \hline & \\ \hline \end{array} \end{matrix}}{\sqrt{d_k}} \right) \begin{matrix} \text{V} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix} \\ &= \begin{matrix} \text{Z} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix} \end{aligned}$$

The Transformer

■ Multi-head attention

- Parallel attention layers with different linear transformations on input and output.



Attention

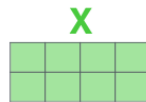
■ Multi-head attention

- Parallel attention layers with different linear transformations on input and output.

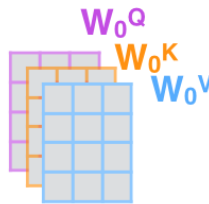
1) This is our input sentence*

Thinking
Machines

2) We embed each word*



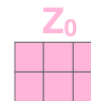
3) Split into 8 heads. We multiply X or R with weight matrices



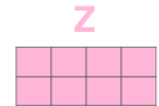
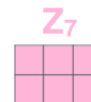
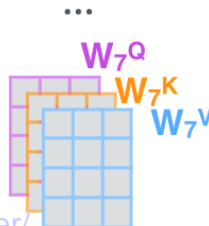
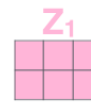
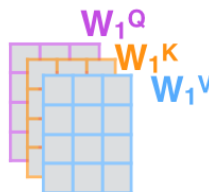
4) Calculate attention using the resulting $Q/K/V$ matrices



5) Concatenate the resulting Z matrices, then multiply with weight matrix W^O to produce the output of the layer



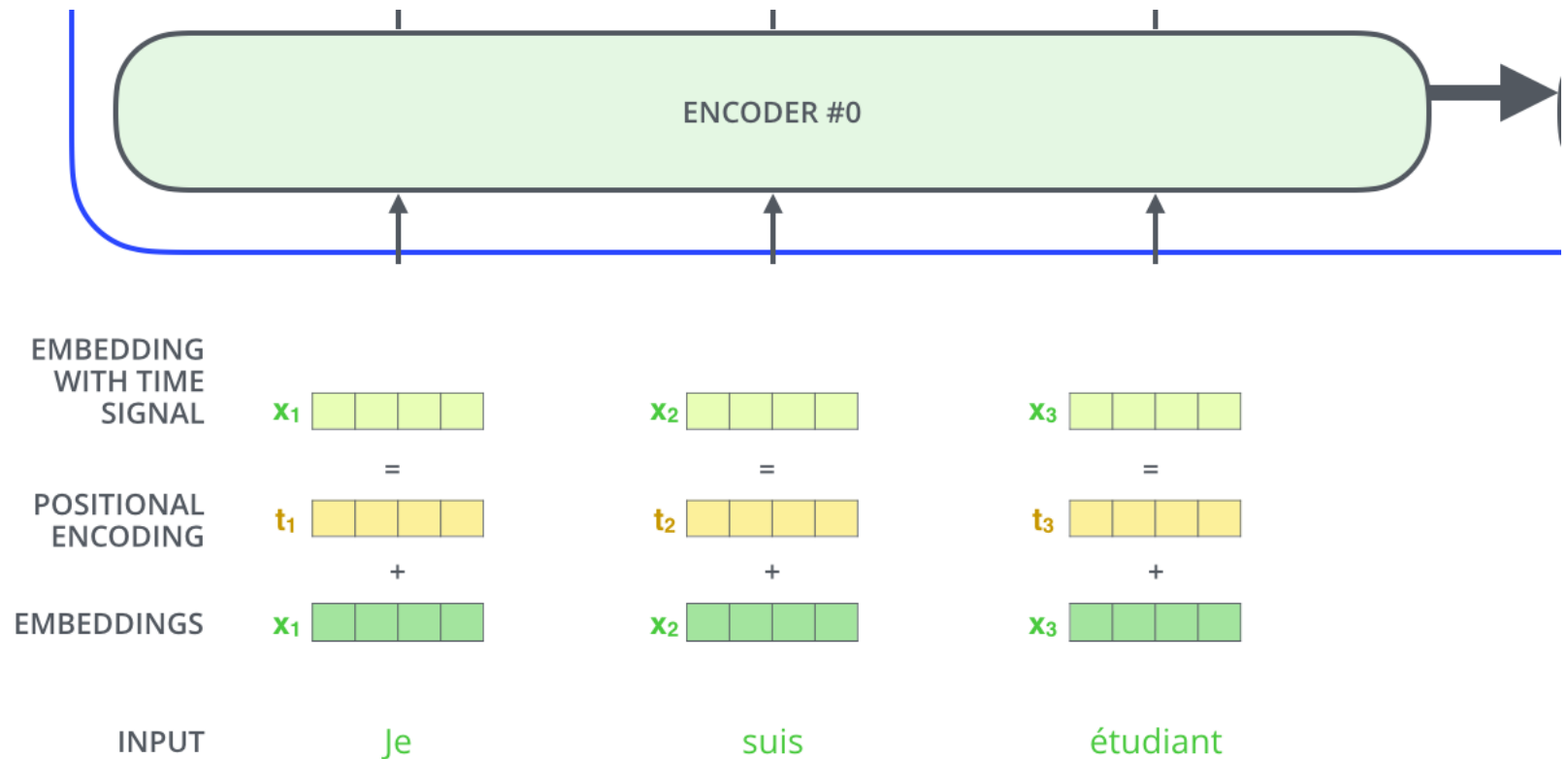
* In all encoders other than #0, we don't need embedding. We start directly with the output of the encoder right below this one



<http://jalammar.github.io/illustrated-transformer/>

The Transformer

- Encoder network: the order information
 - Positional encoding



The Transformer

■ Positional encoding

□ Sinusoid

- Can extrapolate beyond max. sequence length at test-time
- Represent periodicity of positions: a continuous way of binary encoding of position

$$PE_{pos,2i} = \sin(pos/10000^{2i/d_{emb}}),$$

$$PE_{pos,2i+1} = \cos(pos/10000^{2i/d_{emb}}),$$

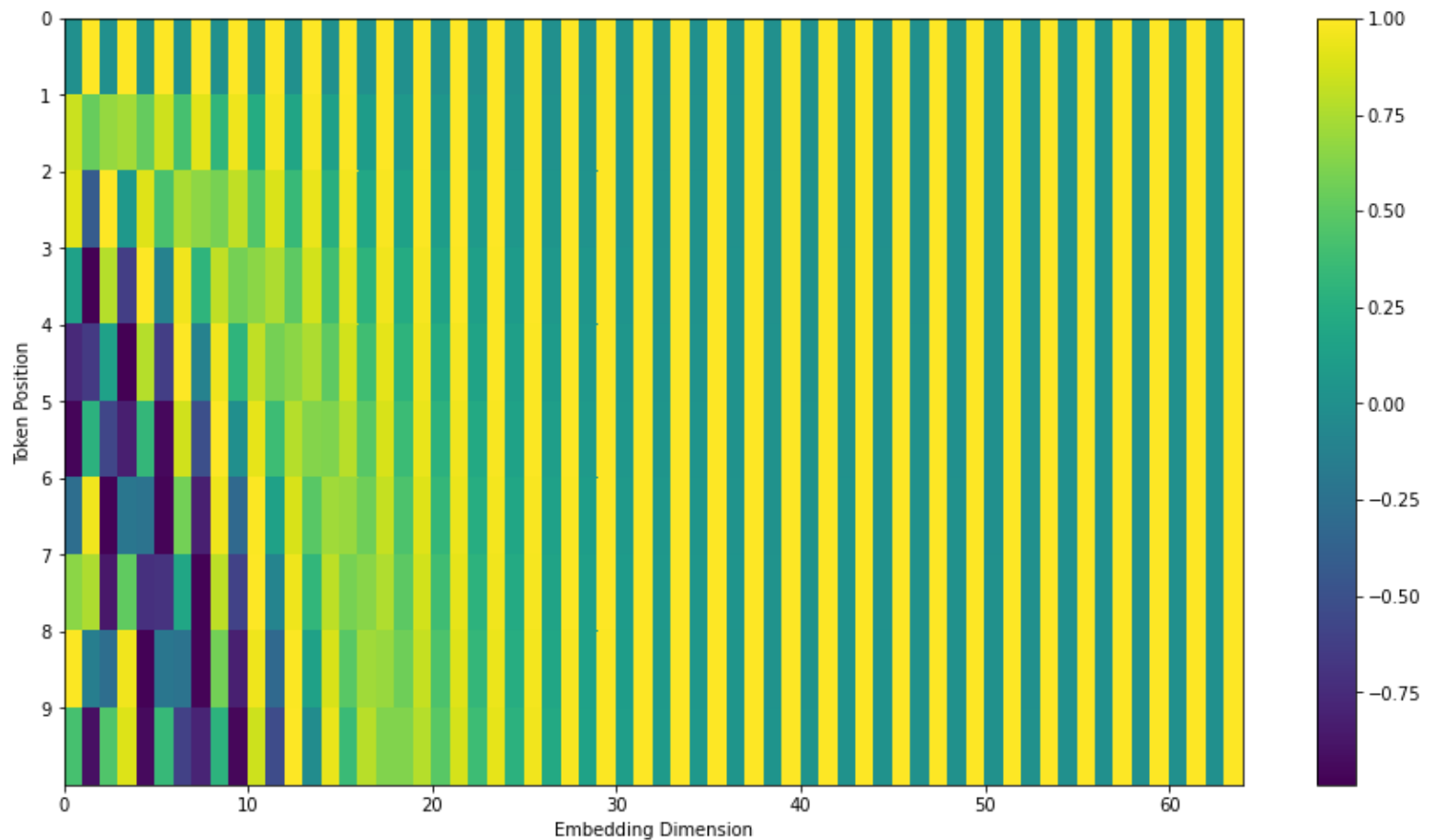
□ Learned

- Rather straightforward
- Cannot extrapolate

The Transformer

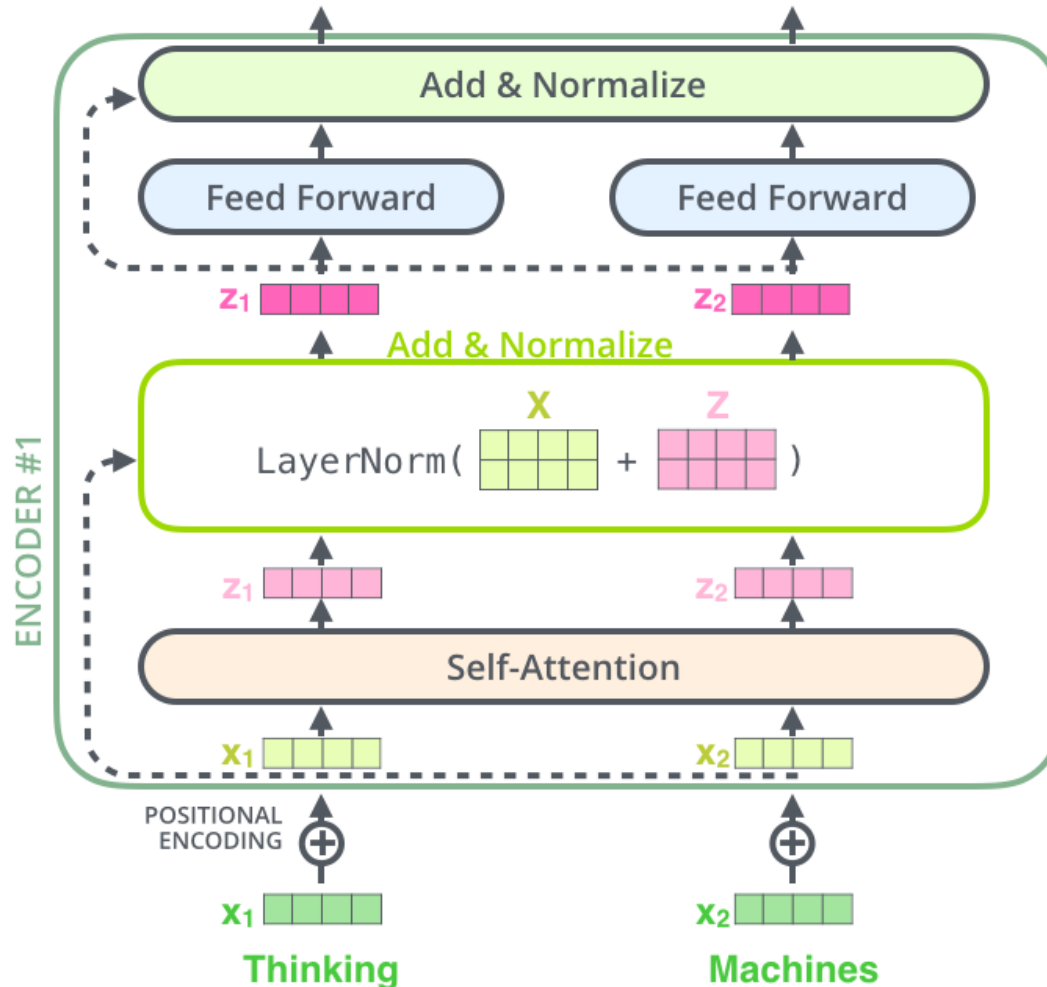
■ Positional encoding

□ Sinusoid



The Transformer

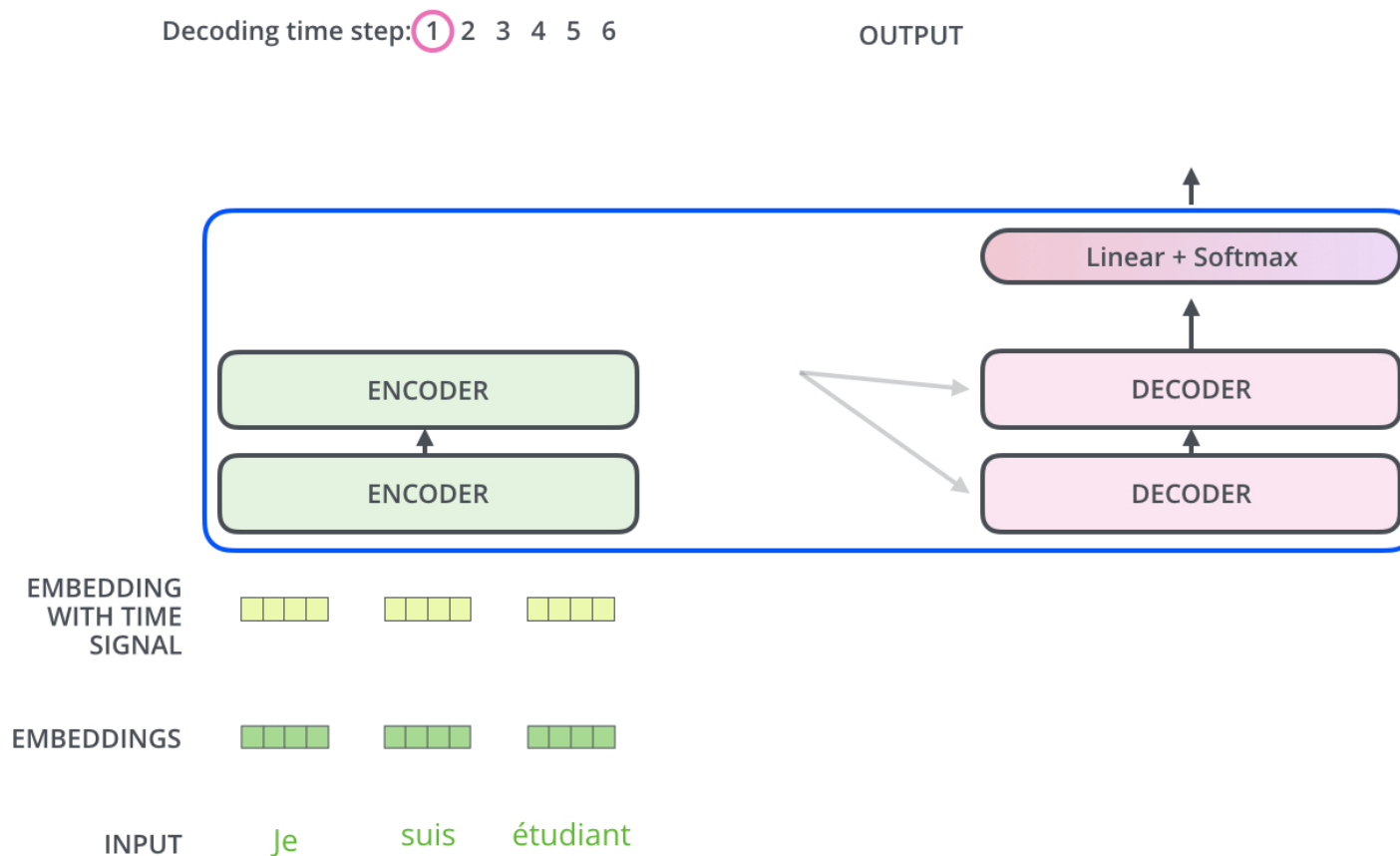
- Residual connections



<http://jalammar.github.io/illustrated-transformer/>

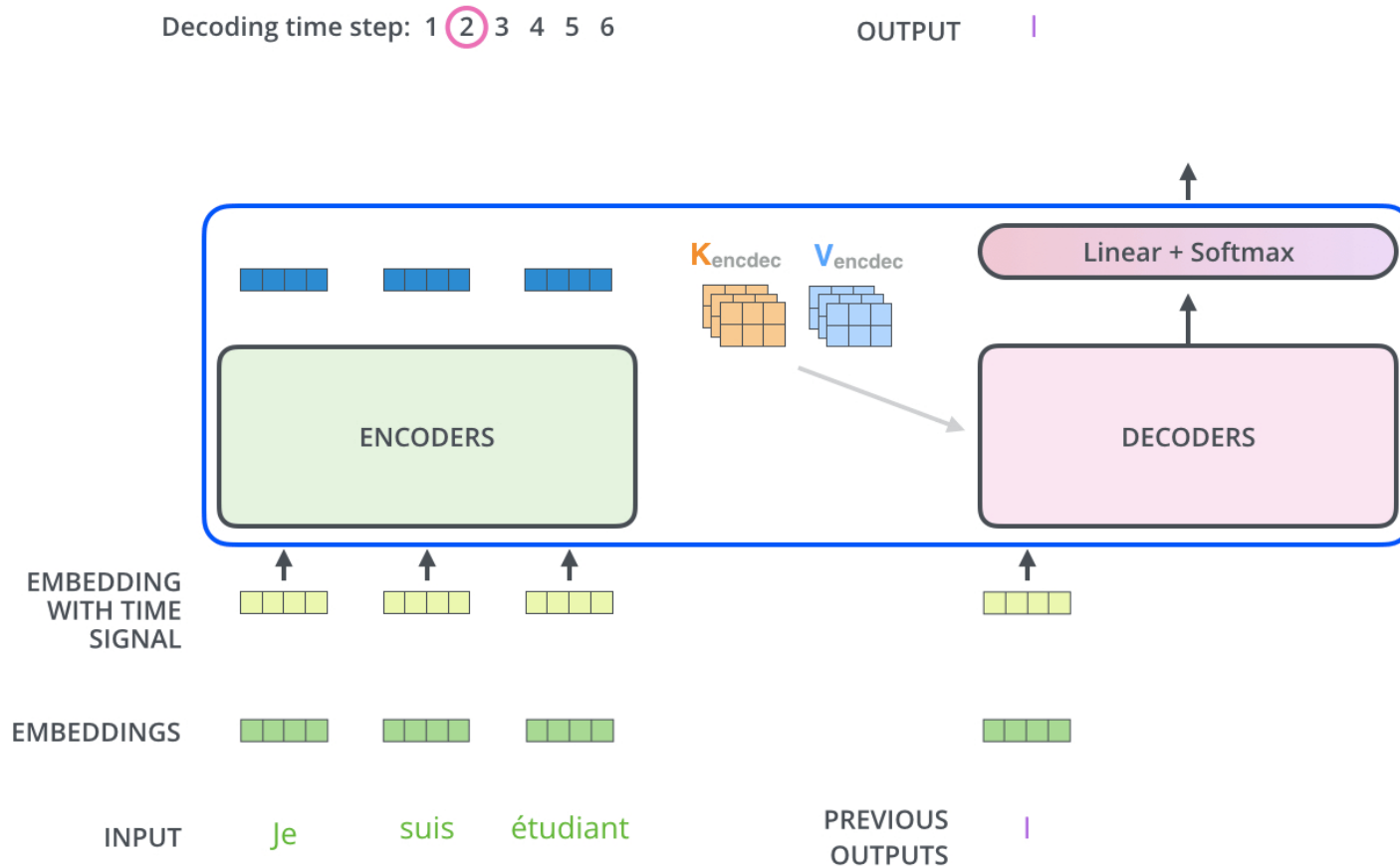
The Transformer

■ Decoder network



The Transformer

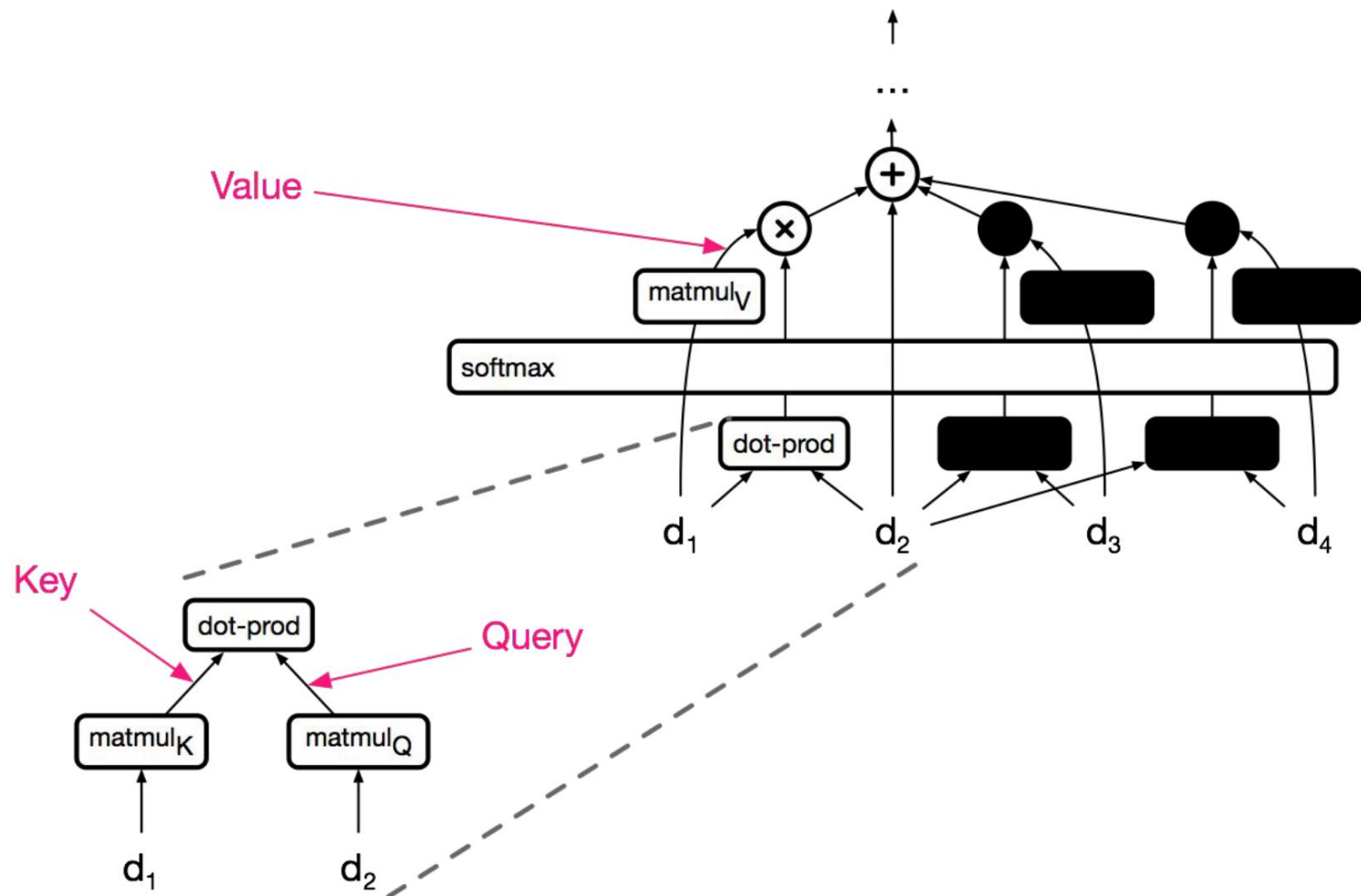
■ Decoder network



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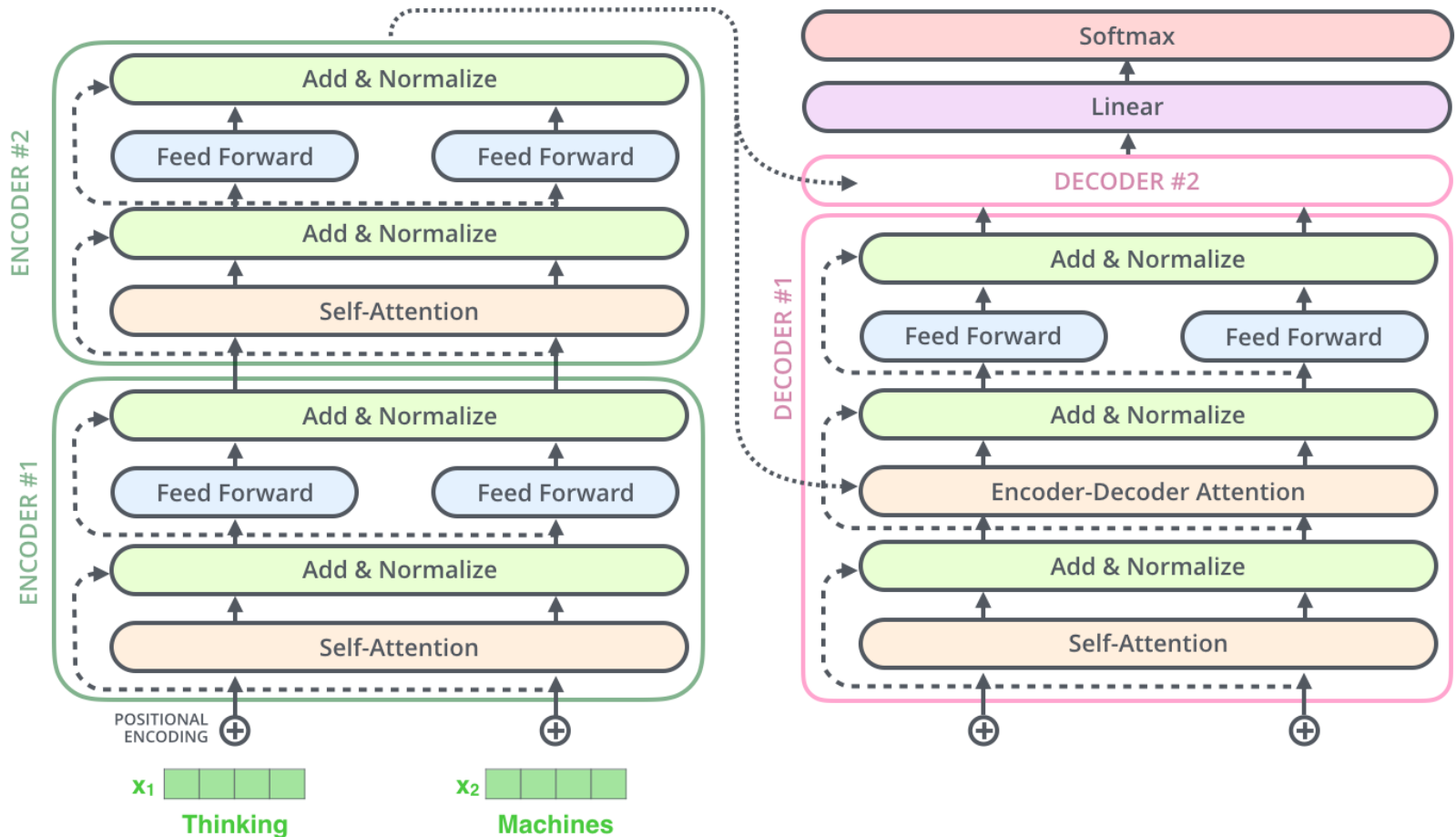
The Transformer

■ Decoder network



The Transformer

Overall architecture

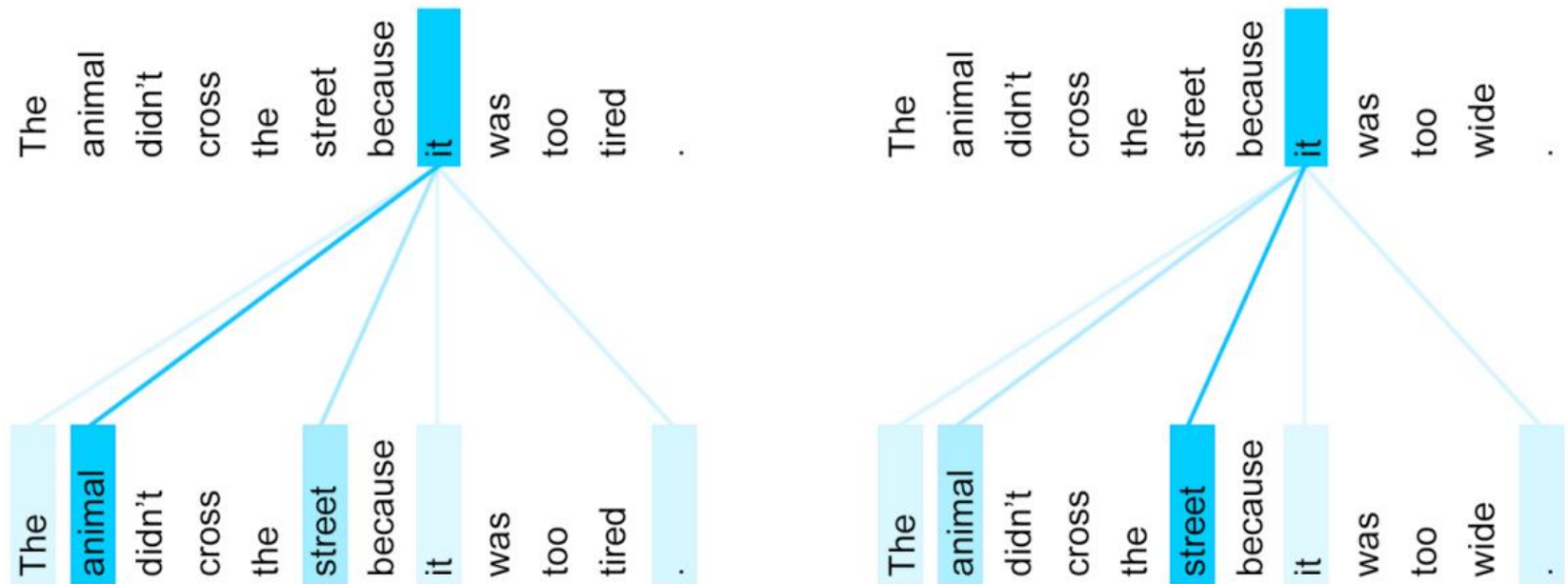


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The Transformer

■ Self-attention example

- Self-attention layers learnt "it" could refer to different entities in the different contexts



Visualization of the 5th to 6th self-attention layer in the encoder

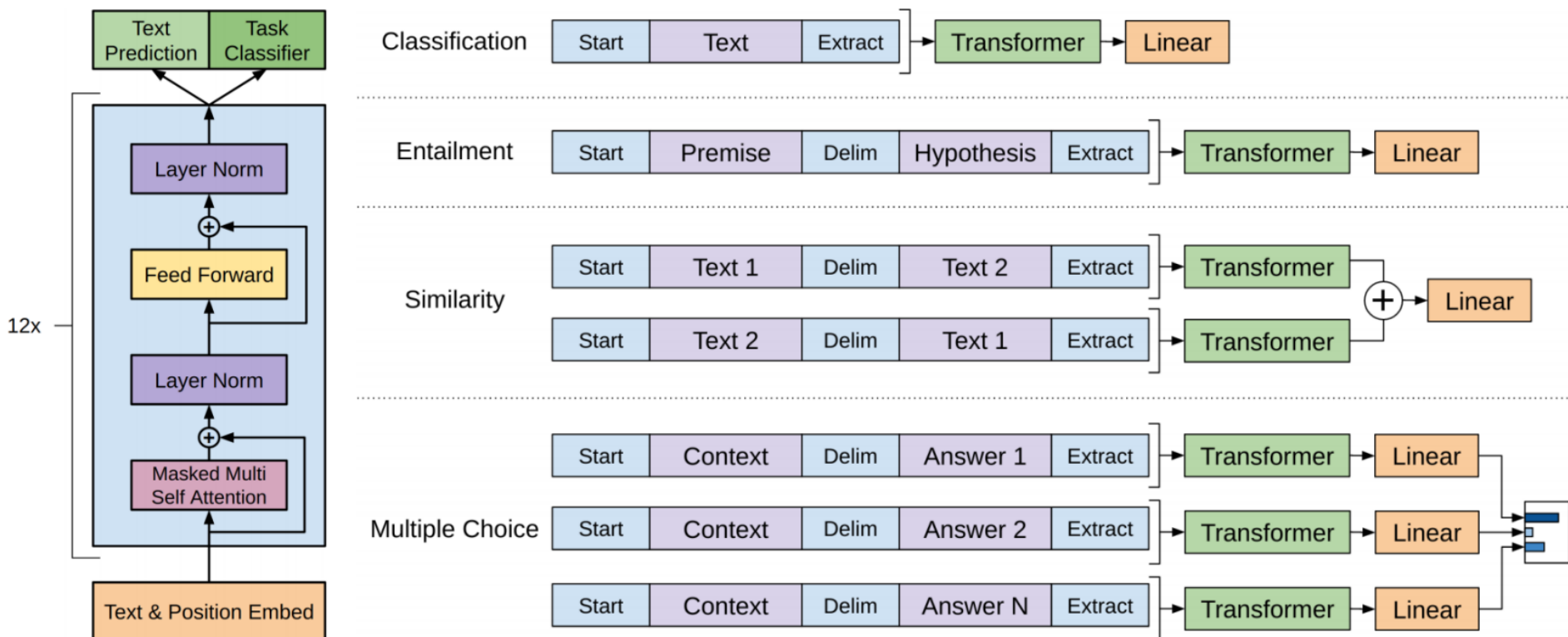
The Transformer

- Attention is all you need
 - BLEU scores of state-of-the-art models on the WMT14 English-to-German translation task

Translation Model	Training time	BLEU (diff. from MOSES)
Transformer (large)	3 days on 8 GPU	28.4 (+7.8)
Transformer (small)	1 day on 1 GPU	24.9 (+4.3)
GNMT + Mixture of Experts	1 day on 64 GPUs	26.0 (+5.4)
ConvS2S (FB)	18 days on 1 GPU	25.1 (+4.5)
GNMT	1 day on 96 GPUs	24.6 (+4.0)

Transformer Language Pre-training

- We can pre-train a language model for NLP tasks.
 - The pre-trained model is then fine-tuned on target tasks.



Transformer Language Pre-training

- We can pre-train a language model for NLP tasks.
 - Generated texts

Context (human-written): In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect English.

GPT-2: The scientist named the population, after their distinctive horn, Ovid's Unicorn. These four-horned, silver-white unicorns were previously unknown to science.

Now, after almost two centuries, the mystery of what sparked this odd phenomenon is finally solved.

Dr. Jorge Pérez, an evolutionary biologist from the University of La Paz, and several companions, were exploring the Andes Mountains when they found a small valley, with no other animals or humans. Pérez noticed that the valley had what appeared to be a natural fountain, surrounded by two peaks of rock and silver snow.

Pérez and the others then ventured further into the valley. "By the time we reached the top of one peak, the water looked blue, with some crystals on top," said Pérez.

Pérez and his friends were astonished to see the unicorn herd. These creatures could be seen from the air without having to move too much to see them – they were so close they could touch their horns.

Radford, Alec, et al. "Language Models are Unsupervised Multitask Learners." 2019

Summary

■ Self-Attention

- Constant 'path length' between any two positions.
- Unbounded memory.
- Trivial to parallelize (per layer).
- Models Self-Similarity.
- Relative attention provides expressive timing, equivariance, and extends naturally to graphs.