

**Problem 1 (5pts) Notes of discussion** I promise that I will complete this QUIZ independently, and will not use mobile phones, computers and other electronic products during the QUIZ, nor will I communicate with other students during this QUIZ.

True or False: I have read the notes and understood them.

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**Problem 2 (5pts) XOR Linked-List**

Each node of the ordinary doubly linked list has three elements, which store the address of the **previous** node, the address of the **next** node, and the **value**. If we combine the previous address and the next address into one **neighbor** address through **XOR** operation, we can greatly reduce the storage space cost. Such a data structure is called an XOR Linked-List.

Each node in the XOR Linked-List contains two elements: `node.value` and `node.neighbor`, in addition, `node.neighbor = node.next XOR node.prev`. There is an example of bitwise XOR:

00110000 XOR 01010000 = 01100000.

As shown in the figure below, there is an XOR linked-list with three nodes.

... < -- > A < -- > B < -- > C < -- > ...

The following three sub-questions are independent of each other. You can answer this question in any way you like, including but not limited to: pseudocode, Python/C code, natural language, etc. Please make sure your description is clear and easy to understand.

In each question, you know the addresses of B and C, and you can access the **neighbor** and **value** elements through this address. Please complete the following three sub-questions.

- (1) Knowing the address of node B and the address of node C, how to get the address of A?  
`A = C XOR B->neighbor`
- (2) Knowing the address of node B, the address of node C and the address of a new node D, how to insert node D between B and C?  
`D->neighbor = B XOR C`  
`B->neighbor = B->neighbor XOR C XOR D`  
`C->neighbor = C->neighbor XOR B XOR D`
- (3) Knowing the address of node B and the address of node C, how to delete node B from the XOR Linked-List?  
`A = C XOR B->neighbor`  
`A->neighbor = A->neighbor XOR B XOR C`  
`C->neighbor = C->neighbor XOR B XOR A`  
`delete(B)`

Hint: If you get puzzled, think about the properties of the XOR operation, such as:  $X \oplus Y \oplus X = Y$ .

**Problem 3(5pts) Algorithm Design**

- (1) Try to convert the polynomial below into the array form which is talked in the class. Note the exponents should be descending.

$$114x^{514} + 19x^{19} + 81x$$

index	0	1	2
coefficient	114	19	81
exponent	514	19	1

- (2) Try to do addition on the two polynomial A and B below and store the result in C. Each polynomial is stored in the struct PLY.

```

struct PLY {
    int exponent[VERY_LARGE];
    int coefficient[VERY_LARGE];
    int len;
};

PLY add(PLY &A, PLY &B) {
    PLY C;
    int i = 0;
    int j = 0;
    int k = 0;
    while (i < A.len or j < B.len) {
        if (j >= B.len or i < A.len and A.exponent[i] > B.exponent[j]) {
            C.exponent[k] = A.exponent[i];
            C.coefficient[k] = A.coefficient[i];
            k++;
            i++;
        } else if (i >= A.len or j < B.len and A.exponent[i] < B.exponent[j]) {
            C.exponent[k] = B.exponent[j];
            C.coefficient[k] = B.coefficient[j];
            k++;
            j++;
        } else if (A.exponent[i] == B.exponent[j]) {
            C.exponent[k] = A.exponent[i];
            C.coefficient[k] = A.coefficient[i] + B.coefficient[j];
            k++;
            i++;
            j++;
        }
    }
    C.len = k;
    return C;
}

```