CS150 Discussion IV

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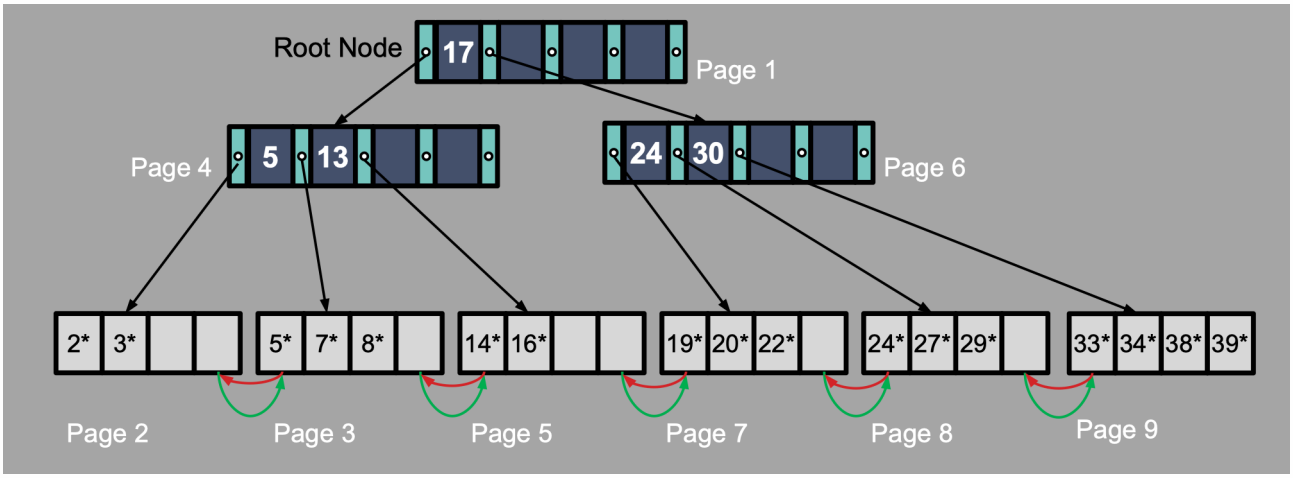
1. B^+ Tree

A quick review

- balanced tree
- internal nodes direct the search, the leaf nodes contain the data entries
- doubly linked list
- a parameter d := the order of the tree

  $d \leq \#\text{ entries} \leq 2d$ for interior nodes

  $1 \leq \#\text{ entries} \leq 2d$ for root node



Cost model for search

d := order of the B^+ Tree

f := fanout, $f \in [d+1, 2d+1]$, here assume it's constant for simplicity

N := total number of pages we'd like to index

F := fill factor (~usually $2/3$)

B := #available buffer pages

- our B^+ Tree needs to have room to index N/F pages
- what is the height h of our B^+ Tree?

  $h = \lceil \log_f \frac{N}{F} \rceil$
- L_B is the number the number of levels such that the sum of all the levels' nodes fit in the buffer

  $B \geq 1 + f + \cdots + f^{L_B - 1} = \sum_{l=0}^{L_B-1} f^l$
- IO cost: $\lceil \log_f \frac{N}{F} \rceil - L_B + 1$, where $B \geq 1 + f + \cdots + f^{L_B - 1} = \sum_{l=0}^{L_B-1} f^l$

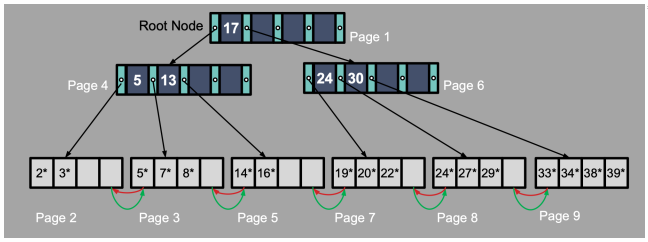
$+\lceil \log_f \frac{N}{F} \rceil$: We read in one page per level of the tree

$-L_B$: However, levels that we can fit in buffer are free!

$+1$: Finally we read in the actual record

Examine the codes

find




```
function find(value V)
/* Returns leaf node C and index i such that C.P_i points to first record
* with search key value V */
    Set C = root node
    while (C is not a leaf node) begin
        Let i = smallest number such that V ≤ C.K_i
        if there is no such number i then begin
            Let P_m = last non-null pointer in the node
            Set C = C.P_m
        end
        else if (V = C.K_i)
            then Set C = C.P_{i+1}
        else C = C.P_i /* V < C.K_i */
    end
    /* C is a leaf node */
    Let i be the least value such that K_i = V
    if there is such a value i
        then return (C, i)
        else return null ; /* No record with key value V exists*/
```

insert

```
procedure insert(value K, pointer P)
    if (tree is empty) create an empty leaf node L, which is also the root
    else Find the leaf node L that should contain key value K
    if (L has less than n − 1 key values)
        then insert_in_leaf (L, K, P)
        else begin /* L has n − 1 key values already, split it */
            Create node L'
            Copy L.P_1 ... L.K_{n−1} to a block of memory T that can
                hold n (pointer, key-value) pairs
            insert_in_leaf (T, K, P)
            Set L'.P_n = L.P_n; Set L.P_n = L'
            Erase L.P_1 through L.K_{n−1} from L
            Copy T.P_1 through T.K_{⌈n/2⌉} from T into L starting at L.P_1
            Copy T.P_{⌈n/2⌉+1} through T.K_n from T into L' starting at L'.P_1
            Let K' be the smallest key-value in L'
            insert_in_parent(L, K', L')
        end

procedure insert_in_leaf (node L, value K, pointer P)
    if (K < L.K_1)
        then insert P, K into L just before L.P_1
        else begin
            Let K_i be the highest value in L that is less than K
            Insert P, K into L just after T.K_i
        end
```

```
procedure insert_in_parent(node N, value K', node N')
    if (N is the root of the tree)
        then begin
            Create a new node R containing N, K', N'   /* N and N' are pointers */
            Make R the root of the tree
            return
        end
    Let P = parent (N)
    if (P has less than n pointers)
        then insert (K', N') in P just after N
        else begin /* Split P */
            Copy P to a block of memory T that can hold P and (K', N')
            Insert (K', N') into T just after N
            Erase all entries from P; Create node P'
            Copy T.P_1 ... T.P_{⌈n/2⌉} into P
            Let K'' = T.K_{⌈n/2⌉}
            Copy T.P_{⌈n/2⌉+1} ... T.P_{n+1} into P'
            insert_in_parent(P, K'', P')
        end
```

2. Buffer Management

Exercises

1. What does it mean to say that a page is pinned in the buffer pool? Who is responsible for pinning pages? Who is responsible for unpinning pages?

2. Name an important capability of a DBMS buffer manager that is not supported by a typical operating system's buffer manager.

3. What happens if a page is requested when all pages in the buffer pool are dirty?