Announcement

- Homework 2
 - Due: Oct. 22, 11:59pm
- Programming Assignment 2
 - Due: Oct. 29, 11:59pm

First-Order Logic

AIMA Chapter 8, 9

Pros of propositional logic

- Propositional logic allows partial/disjunctive/negated information
 - (unlike most data structures and databases)
- Propositional logic is compositional:
 - meaning of $B_{1,1} \wedge P_{1,2}$ is derived from meaning of $B_{1,1}$ and of $P_{1,2}$
- Meaning in propositional logic is context-independent
 - (unlike natural language, where meaning depends on context)

Cons of propositional logic

- Can't directly talk about properties of individuals or relations between individuals (e.g., "Bill is tall")
- ☼ Generalizations, patterns, regularities can't easily be represented (e.g., "all triangles have 3 sides")

First-order logic

- Whereas propositional logic assumes the world contains facts...
- First-order logic (like natural language) assumes the world contains
 - Objects: people, houses, numbers, colors, baseball games, wars, ...
 - Relations: red, round, prime, bigger than, part of, comes between, ...
 - Functions: father of, best friend of, one more than, ...
- Also called first-order predicate logic

Syntax of FOL: Basic elements

- Logical symbols
 - Connectives \neg , \wedge , \vee , \Rightarrow , \Leftrightarrow
 - Quantifiers ∀, ∃
 - Variablesx, y, a, b, ...
 - Equality =
- Non-logical symbols (ontology)
 - Constants
 KingArthur, 2, ShanghaiTech, ...
 - PredicatesBrother, >, ...
 - FunctionsSqrt, LeftLegOf, ...

Atomic sentences

```
Atomic sentence = predicate (term_1,...,term_n)

or term_1 = term_2

Term = constant or variable

or function (term_1,...,term_n)
```

Example:

```
Brother(KingJohn,RichardTheLionheart) >(Length(LeftLegOf(Richard)), Length(LeftLegOf(KingJohn)))
```

Complex sentences

Complex sentences are made from atomic sentences using connectives

$$\neg S$$
, $S_1 \land S_2$, $S_1 \lor S_2$, $S_1 \Rightarrow S_2$, $S_1 \Leftrightarrow S_2$,

Example:

Sibling(KingJohn,Richard) ⇒ Sibling(Richard,KingJohn)

$$>(1,2) \lor \le (1,2)$$

$$>(1,2) \land \neg >(1,2)$$

Semantics of FOL

- Sentences are true with respect to a model, which contains
 - Objects and relations among them
 - Interpretation specifying referents for

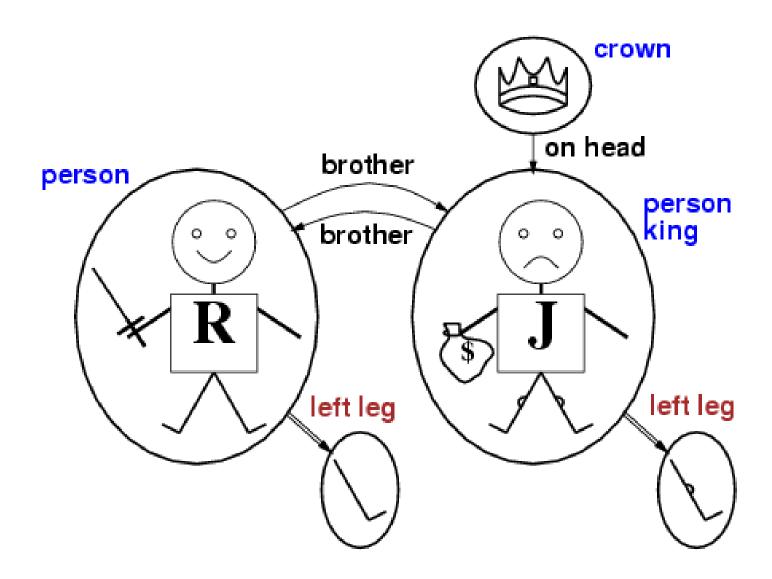
```
constant symbols → objects

predicate symbols → relations

function symbols → functional relations
```

 An atomic sentence predicate(term₁,...,term_n) is true iff the objects referred to by term₁,...,term_n are in the relation referred to by predicate

Models for FOL: Example



Models for FOL: Example

Consider the interpretation:

```
Richard → Person R

John → Person J

Brother → the brotherhood relation
```

Under this interpretation, *Brother*(*Richard*, *John*) is true in the model.

Models for FOL

- How many models do we have? Infinite!
 Models vary in:
 - the number of objects (1 to ∞)
 - the relations among the objects
 - the mapping from constants to objects
 - the mapping from predicates to relations
 - **–**

Quantifiers

- Allows us to express properties of collections of objects instead of enumerating objects by name
- Universal: "for all" ∀
- Existential: "there exists" ∃

Universal quantification

```
\forall<variables> <sentence>
Example: \forall x \ At(x,STU) \Rightarrow Smart(x)
(Everyone at ShanghaiTech is smart)
```

 $\forall x P$ is true in a model m iff P is true with x being each possible object in the model

 Roughly speaking, equivalent to the conjunction of instantiations of P

```
At(John,STU) \Rightarrow Smart(John)
 \land At(Richard,STU) \Rightarrow Smart(Richard)
 \land At(STU,STU) \Rightarrow Smart(STU)
 \land ...
```

A common mistake to avoid

- Typically, ⇒ is the main connective with ∀
- Common mistake: using ∧ as the main connective with ∀:

```
\forall x \ At(x,STU) \land Smart(x)
```

means "Everyone is at STU and everyone is smart"

Existential quantification

```
∃<variables> <sentence>
Example: ∃x At(x,STU) ∧ Smart(x)
(Someone at ShanghaiTech is smart)
```

 $\exists x P$ is true in a model m iff P is true with x being some possible object in the model

 Roughly speaking, equivalent to the disjunction of instantiations of P

```
(At(John,STU) ∧ Smart(John))
∨ (At(Richard,STU) ∧ Smart(Richard))
∨ (At(STU,STU) ∧ Smart(STU))
∨ ...
```

Another common mistake to avoid

- Typically, ∧ is the main connective with ∃
- Common mistake: using ⇒ as the main connective with
 ∃:

```
\exists x \ At(x,STU) \Rightarrow Smart(x)
```

is true if there is anyone who is not at STU!

Properties of quantifiers

- ∀x ∀y is the same as ∀y ∀x
- $\exists x \exists y \text{ is the same as } \exists y \exists x$
- ∃x ∀y is not the same as ∀y ∃x
 - ∃x ∀y Loves(x,y)"There is a person who loves everyone in the world"
 - ∀y ∃x Loves(x,y)"Everyone in the world is loved by at least one person"
- Quantifier duality: each can be expressed using the other

```
\forall x \text{ Likes}(x,\text{IceCream}) \equiv \neg \exists x \neg \text{Likes}(x,\text{IceCream})
\exists x \text{ Likes}(x,\text{Broccoli}) \equiv \neg \forall x \neg \text{Likes}(x,\text{Broccoli})
```

Sentences with variables

- A variable is free in a formula if it is not quantified
 - e.g., $\forall x P(x,y)$
- A variable is bound in a formula if it is quantified
 - e.g., $\forall x \exists y \ P(x,y)$
- In a FOL sentence, every variable must be bound.

FOL example: kinship

- Brothers are siblings
 - $\forall x,y \; Brother(x,y) \Rightarrow Sibling(x,y).$
- "Sibling" is symmetric

```
\forall x,y \ Sibling(x,y) \Leftrightarrow Sibling(y,x).
```

One's mother is one's female parent

```
\forall x,y \; Mother(x,y) \Leftrightarrow (Female(x) \land Parent(x,y)).
```

A first cousin is a child of a parent's sibling

```
\forall x,y \ FirstCousin(x,y) \Leftrightarrow \exists p,ps \ Parent(p,x) \land Sibling(ps,p) \land Parent(ps,y)
```

FOL example: kinship

Siblings are people with the same parents

```
\forall x,y \; Sibling(x,y) \Leftrightarrow \exists m,f \; Parent(m,x) \land Parent(f,x) \land Parent(m,y) \land Parent(f,y)
```

Is this correct?

Equality

 $term_1 = term_2$ is true under a given interpretation if and only if $term_1$ and $term_2$ refer to the same object

Example: Siblings are people with the same parents:

```
\forall x,y \; Sibling(x,y) \Leftrightarrow [\neg(x=y) \land \exists m,f \; \neg(m=f) \land Parent(m,x) \land Parent(f,x) \land Parent(m,y) \land Parent(f,y)]
```

FOL example

True or false?

```
\forall x \ CollegeStudent(x) \Rightarrow Student(x)
```

 $\forall x \ Student(x) \Rightarrow CollegeStudent(x)$

- Sentences are true/false with respect to a model
 - No truth-value without a model!
 - Symbols do not carry meanings by themselves
 David Hilbert: "One must be able to say at all times
 - instead of points, straight lines, and planes
 - tables, chairs, and beer mugs."



Inference in first-order logic

Universal instantiation (UI)

(Term without variables)

For any sentence α, variable v and ground term g:

$$\frac{\forall v \alpha}{\text{Subst}(\{v/g\}, \alpha)} \leftarrow \text{Substitute } v \text{ with } g \text{ in } \alpha$$

- Every instantiation of a universally quantified sentence is entailed by it
- UI can be applied multiple times to add new sentences
- E.g., $\forall x \ King(x) \land Greedy(x) \Rightarrow Evil(x)$ yields:
 - King(John) ∧ Greedy(John) ⇒ Evil(John)
 - King(Richard) ∧ Greedy(Richard) ⇒ Evil(Richard)
 - King(Father(John)) ∧ Greedy(Father(John)) ⇒Evil(Father(John))

Existential instantiation (EI)

 For any sentence α, variable v, and constant symbol k that does not appear elsewhere in the knowledge base:

- El can be applied once to replace an existential sentence
- E.g., ∃x Crown(x) ∧ OnHead(x,John) yields:
 Crown(C₁) ∧ OnHead(C₁,John)
 provided C₁ is a new constant symbol, called a Skolem constant

Reduction to propositional inference

- Suppose the KB contains just the following:
 - ∀x King(x) \wedge Greedy(x) \Rightarrow Evil(x)
 - King(John)
 - Greedy(John)
 - Brother(Richard, John)

- Instantiating the universal sentence in all possible ways, we have:
 - King(John) ∧ Greedy(John) ⇒ Evil(John)
 - King(Richard) ∧ Greedy(Richard) ⇒ Evil(Richard)
 - King(John)
 - Greedy(John)
 - Brother(Richard, John)
- The new KB is propositionalized: proposition symbols are
 - King(John), Greedy(John), Evil(John), King(Richard), etc.

- Every FOL KB can be propositionalized so as to preserve entailment
 - i.e., a ground sentence is entailed by new KB iff entailed by original KB
- A naïve idea for FOL inference:
 - propositionalize KB and query, apply resolution, return result
- Problem: with function symbols, there are infinitely many ground terms,
 - e.g., Father(Father(Father(John)))

- Theorem (Herbrand, 1930)
 - If a sentence α is entailed by an FOL KB, it is entailed by a finite subset of the propositionalized KB
- Idea:

For n = 0 to ∞ do

- create a propositional KB by instantiating with depth-n terms
- 2. if α is entailed by this KB, return true

Function nesting levels

Does this work?

- Problem
 - works if α is entailed
 - infinite loops if α is not entailed
- Theorem (Turing, 1936; Church, 1936): entailment for FOL is semi-decidable
 - algorithms exist that say yes to every entailed sentence
 - but no algorithm exists that says no to every non-entailed sentence.

Problems with propositionalization

- Propositionalization generates many irrelevant sentences
- E.g., from:
 - ∀x King(x) \wedge Greedy(x) \Rightarrow Evil(x)
 - King(John)
 - − ∀y Greedy(y)

The query *Evil(John)* seems obviously true. But propositionalization produces lots of facts such as *Greedy(Richard)* that are irrelevant.

Given:

```
    - ∀x King(x) ∧ Greedy(x) ⇒ Evil(x)
    - King(John)
    - ∀y Greedy(y)

Only variables can be substituted
```

- If we can find the substitution $\theta = \{x/John, y/John\}$, then we get
 - − King(John) ∧ Greedy(John) ⇒ Evil(John)
 - King(John)
 - Greedy(John)

and we can answer the query *Evil(John)* immediately

- Unification finds substitutions that make different expressions identical
 - E.g., King(x) vs. King(John); Greedy(x) vs. Greedy(y)

• Unify(α , β) = θ if $\alpha\theta = \beta\theta$

p	q	θ
Knows(John,x)	Knows(John,Jane)	
Knows(John,x)	Knows(y,OJ)	
Knows(John,x)	Knows(y,Mother(y))	
Knows(John,x)	Knows(x,OJ)	

• Unify(α,β) = θ if $\alpha\theta = \beta\theta$

p	q	θ
Knows(John,x)	Knows(John,Jane)	{x/Jane}
Knows(John,x)	Knows(y,OJ)	
Knows(John,x)	Knows(y,Mother(y))	
Knows(John,x)	Knows(x,OJ)	

• Unify(α , β) = θ if $\alpha\theta = \beta\theta$

p	q	θ
Knows(John,x)	Knows(John,Jane)	{x/Jane}
Knows(John,x)	Knows(y,OJ)	{x/OJ,y/John}
Knows(John,x)	Knows(y,Mother(y))	
Knows(John,x)	Knows(x,OJ)	

Unification

• Unify(α , β) = θ if $\alpha\theta = \beta\theta$

p	q	θ
Knows(John,x)	Knows(John,Jane)	{x/Jane}
Knows(John,x)	Knows(y,OJ)	{x/OJ,y/John}
Knows(John,x)	Knows(y,Mother(y))	{y/John,x/Mother(John)}
Knows(John,x)	Knows(x,OJ)	

Unification

• Unify(α,β) = θ if $\alpha\theta = \beta\theta$

p	q	θ
Knows(John,x)	Knows(John,Jane)	{x/Jane}
Knows(John,x)	Knows(y,OJ)	{x/OJ,y/John}
Knows(John,x)	Knows(y,Mother(y))	{y/John,x/Mother(John)}
Knows(John,x)	Knows(x,OJ)	{fail}
		†

Can be avoided by standardizing apart: eliminate overlap of variables, e.g., Knows(z,OJ)

Unification

- To unify Knows(John,x) and Knows(y,z),
 θ = {y/John, x/z } or θ = {y/John, x/John, z/John}
 - The first unifier is more general than the second.
- There is a single most general unifier (MGU) that is unique up to renaming of variables.
 - $MGU = \{ y/John, x/z \}$

FOL Inference

- Horn logic (the FOL case)
 - Forward chaining
 - Backward chaining
- General FOL
 - Resolution

Horn clauses in FOL

- $p_1 \wedge p_2 \wedge ... \wedge p_n \Rightarrow q$
 - $-p_1, p_2, ..., p_n, q$ are atomic sentences
 - All variables assumed to be universally quantified
- E.g., $human(x) \Rightarrow mortal(x)$

Generalized Modus Ponens (GMP)

$$\frac{p_1', p_2', \dots, p_n', (p_1 \land p_2 \land \dots \land p_n \Rightarrow q)}{q\theta} \quad \text{where } p_i'\theta = p_i \theta \text{ for all } i$$

```
Example: King(John), Greedy(y), (King(x) \land Greedy(x) \Rightarrow Evil(x)) p_1' is King(John) p_1 is King(x) p_2' is Greedy(y) p_2 is Greedy(x) Therefore, \theta is {x/John, y/John}
```

q is Evil(x), so $q\theta$ is Evil(John)

Example knowledge base

 The US law says that it is a crime for an American to sell weapons to hostile nations. The country Nono, an enemy of America, has some missiles, and all of its missiles were sold to it by Colonel West, who is American.

Prove that Col. West is a criminal

Example knowledge base contd.

```
... it is a crime for an American to sell weapons to hostile nations:
    American(x) \land Weapon(y) \land Sells(x,y,z) \land Hostile(z) \Rightarrow Criminal(x)
Nono ... has some missiles, i.e., \exists x \ Owns(Nono,x) \land Missile(x):
     Owns(Nono,M_1) and Missile(M_1)
... all of its missiles were sold to it by Colonel West
    Missile(x) \land Owns(Nono,x) \Rightarrow Sells(West,x,Nono)
Missiles are weapons:
    Missile(x) \Rightarrow Weapon(x)
An enemy of America counts as "hostile":
    Enemy(x,America) \Rightarrow Hostile(x)
West, who is American ...
    American(West)
The country Nono, an enemy of America ...
    Enemy(Nono, America)
```

Forward chaining proof

- $American(x) \land Weapon(y) \land Sells(x,y,z) \land Hostile(z) \Rightarrow Criminal(x)$ $Missile(x) \land Owns(Nono,x) \Rightarrow Sells(West,x,Nono)$
- $Missile(x) \Rightarrow Weapon(x)$
- $Enemy(x,America) \Rightarrow Hostile(x)$
- Owns(Nono,M₁), Missile(M₁), American(West), Enemy(Nono,America)

American(West)

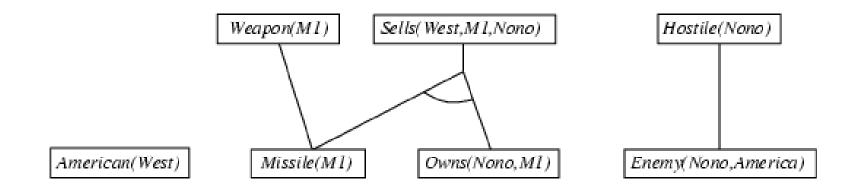
Missile(MI)

Owns(Nono, MI)

Enemy(Nono, America)

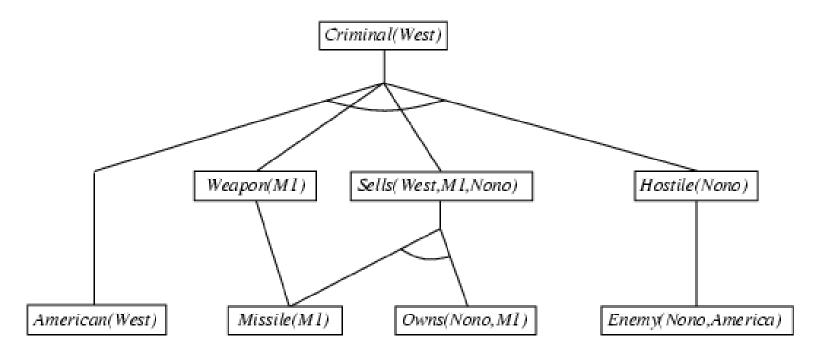
Forward chaining proof

- $American(x) \land Weapon(y) \land Sells(x,y,z) \land Hostile(z) \Rightarrow Criminal(x)$ $Missile(x) \land Owns(Nono,x) \Rightarrow Sells(West,x,Nono)$
- $Missile(x) \Rightarrow Weapon(x)$
- $Enemy(x,America) \Rightarrow Hostile(x)$
- Owns(Nono, M_1), Missile(M_1), American(West), Enemy(Nono, America)



Forward chaining proof

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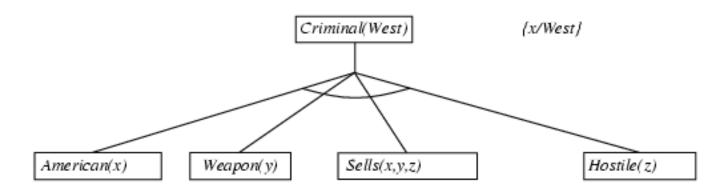
Properties of forward chaining

- Sound and complete for first-order Horn clauses
- FC terminates for first-order Horn clauses with no functions (Datalog) in finite number of iterations
- In general, FC may not terminate if α is not entailed
 - This is unavoidable: entailment with Horn clauses is also semi-decidable

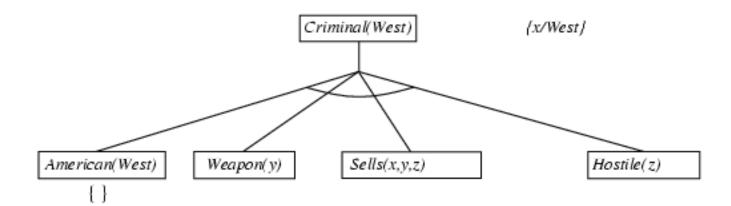
- American(x) \land Weapon(y) \land Sells(x,y,z) \land Hostile(z) \Rightarrow Criminal(x) Missile(x) \land Owns(Nono,x) \Rightarrow Sells(West,x,Nono)
- $Missile(x) \Rightarrow Weapon(x)$
- $Enemy(x,America) \Rightarrow Hostile(x)$
- Owns(Nono, M_1), Missile(M_1), American(West), Enemy(Nono, America)

Criminal(West)

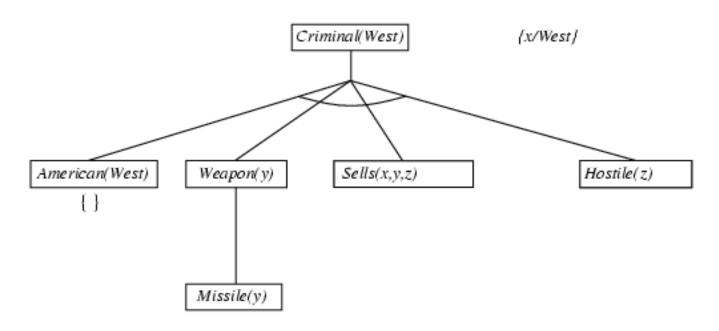
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- $Missile(x) \Rightarrow Weapon(x)$
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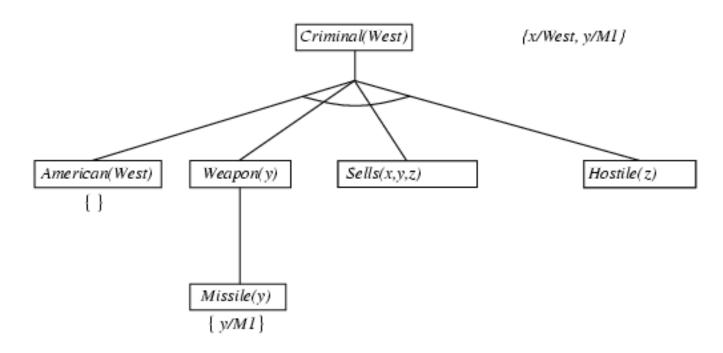
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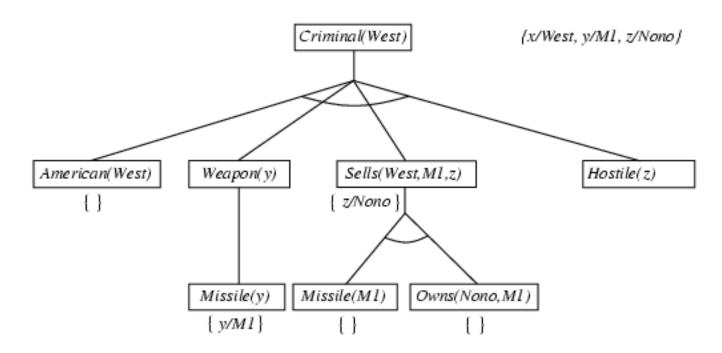
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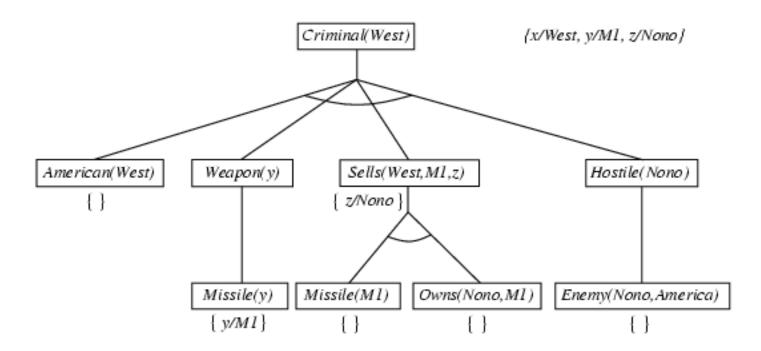
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Backward chaining

- Depth-first recursive proof search: space is linear in size of proof
- Avoid infinite loops by checking current goal against every goal on stack
- Avoid repeated subgoals by caching previous results
- Widely used for logic programming

Logic programming

- Ordinary programming
 - Identify problem
 - Assemble information
 - Figure out solution
 - Encode solution
 - Encode problem instance as data
 - Apply program to data

- Logic programming
 - Identify problem
 - Assemble information
 - − <coffee break> ©
 - Encode info in KB
 - Encode problem instances as facts
 - Ask queries (run SAT solver)

Logic programming: Prolog

- Was widely used in Europe, Japan (basis of 5th Generation project)
- Basis: backward chaining with Horn clauses
 - Program = set of Horn clauses
 - Inference: depth-first, left-to-right backward chaining
- Additions:
 - Built-in predicates for arithmetic etc., e.g., X is Y*Z+3
 - Built-in predicates that have side effects (e.g., input and output predicates, assert/retract predicates)
- Closed-world assumption ("negation as failure")

Resolution

Full first-order version:

$$\frac{\ell_1 \vee \cdots \vee \ell_k, \quad m_1 \vee \cdots \vee m_n}{(\ell_1 \vee \cdots \vee \ell_{i-1} \vee \ell_{i+1} \vee \cdots \vee \ell_k \vee m_1 \vee \cdots \vee m_{j-1} \vee m_{j+1} \vee \cdots \vee m_n)\theta}$$
 where Unify(ℓ_i , $\neg m_i$) = θ .

- The two clauses are assumed to be standardized apart so that they share no variables.
- Example:

$$\neg Rich(x) \lor Unhappy(x)$$

$$Rich(Ken)$$

$$Unhappy(Ken)$$
with $\theta = \{x/Ken\}$

- Inference algorithm: applying resolution steps to CNF(KB ∧ ¬α)
- Resolution is sound and complete for FOL

Conversion to CNF

```
\forall x [\forall y \ Animal(y) \Rightarrow Loves(x,y)] \Rightarrow [\exists y \ Loves(y,x)]
```

1. Eliminate biconditionals and implications $\forall x [\neg \forall y \neg Animal(y) \lor Loves(x,y)] \lor [\exists y Loves(y,x)]$

- 2. Move \neg inwards: $\neg \forall x \ p \equiv \exists x \neg p, \ \neg \exists x \ p \equiv \forall x \neg p$ $\forall x \ [\exists y \neg (\neg Animal(y) \lor Loves(x,y))] \lor [\exists y \ Loves(y,x)]$ $\forall x \ [\exists y \neg \neg Animal(y) \land \neg Loves(x,y)] \lor [\exists y \ Loves(y,x)]$ $\forall x \ [\exists y \ Animal(y) \land \neg Loves(x,y)] \lor [\exists y \ Loves(y,x)]$
- 3. Standardize variables: each quantifier should use a different variable

```
\forall x [\exists y \ Animal(y) \land \neg Loves(x,y)] \lor [\exists z \ Loves(z,x)]
```

Conversion to CNF contd.

```
\forall x [\exists y \ Animal(y) \land \neg Loves(x,y)] \lor [\exists z \ Loves(z,x)]
```

4. Skolemize: a more general form of existential instantiation. Each existential variable is replaced by a Skolem function of the enclosing universally quantified variables:

```
\forall x [Animal(F(x)) \land \neg Loves(x,F(x))] \lor Loves(G(x),x)
```

5. Drop universal quantifiers:

```
[Animal(F(x)) \land \neg Loves(x,F(x))] \lor Loves(G(x),x)
```

6. Distribute ∨ over ∧ :

```
[Animal(F(x)) \vee Loves(G(x),x)] \wedge [\negLoves(x,F(x)) \vee Loves(G(x),x)]
```

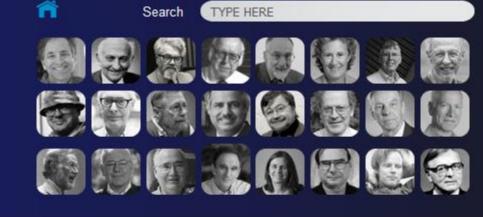
Resolution proof: Horn clauses

```
¬ Criminal(West)
\neg American(x) \lor \neg Weapon(y) \lor \neg Sells(x,y,z) \lor \neg Hostile(z) \lor Criminal(x)
                                    American(West)
                                                                \neg American(West) \lor \neg Weapon(y) \lor \neg Sells(West,y,z) \lor \neg Hostile(z)
                                \neg Missile(x) \lor Weapon(x)
                                                                         \neg Weapon(y) \lor \neg Sells(West,y,z) \lor \neg Hostile(z)
                                              Missile(M1)
                                                                          \neg Missile(y) \lor \neg Sells(West,y,z) \lor \neg Hostile(z)
        \neg Missile(x) \lor \neg Owns(Nono,x) \lor Sells(West,x,Nono)
                                                                                  \neg Sells(West,M1,z) \lor \neg Hostile(z)
                                      Missile(M1)
                                                                  \neg Missile(M1) \lor \neg Owns(Nono,M1) \lor \neg Hostile(Nono)
                                 Owns(Nono,M1)
                                                                       \neg Owns(Nono, M1) \lor \neg Hostile(Nono)
                          \neg Enemy(x,America) \lor Hostile(x)
                                                                               ¬ Hostile(Nono)
                              Enemy(Nono, America)
                                                                    Enemy(Nono, America)
```

Semantic Web: Application of Logic to WWW







A.M. TURING AWARD WINNERS BY ...

ALPHABETICAL LISTING

YEAR OF THE AWARD

RESEARCH SUBJECT



Inventor of World Wide Web Receives ACM A.M. Turing Award

Sir Tim Berners-Lee Designed Integrated Architecture and Technologies that Underpin the Web

ACM named Sir Tim Berners-Lee, a Professor at Massachusetts Institute of Technology and the University of Oxford, the recipient of the 2016 ACM A.M. Turing Award. Berners-Lee was cited for

The Semantic Web

Since the late 1990s Berners-Lee's primary focus has been on trying to get Web publishers and technology companies to add a set of capabilities he called the "Semantic Web." Berners-Lee defined his idea as follows: "The Semantic Web is an extension of the current Web in which information is given well-defined meaning, better enabling computers and people to work in cooperation."

commerce, and perform many other important activities.

FEATURED AWARD WINNER

Sir Tim Berners

For inventing the World the first web browser, an fundamental protocols and allowing the Web to scale.

More on Sir Tim Berners-Lee and his

The ACM Turing Award, often referred to as the "Nobel Prize of

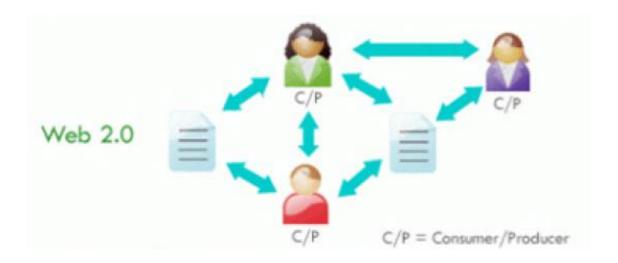
Web 1.0

- Information flows from providers to consumers
 - The majority of WWW users are consumers
 - Webpages are static and read-only



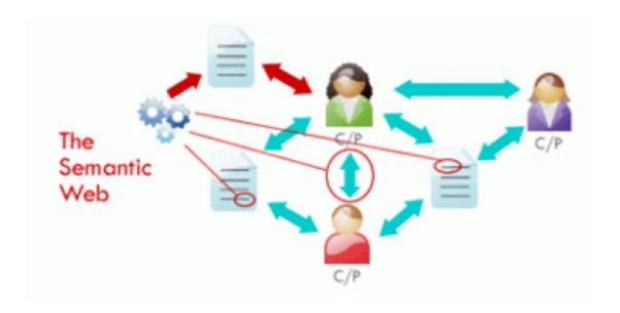
Web 2.0

- WWW users are both providers and consumers
 - Webpages are dynamic and interactive



Web 3.0 (Semantic Web)

- Computers mediate the information flow, helping users publish and acquire data
 - Semantic annotations (i.e., logic sentences) on data that can be understood and processed by computers
 - (Semantic Web is Symbolic AI applied to WWW)



RDF

- RDF (Resource Description Framework)
 - The basic language of semantic web ____ atomic sentence in FOL

- RDF represents information with triples:
 - RDF Triple (s,p,o)

binary predicate in FOL

- s/p/o: "subject", "property", and "object"
- s and p are URIs
- o is a URI or literal

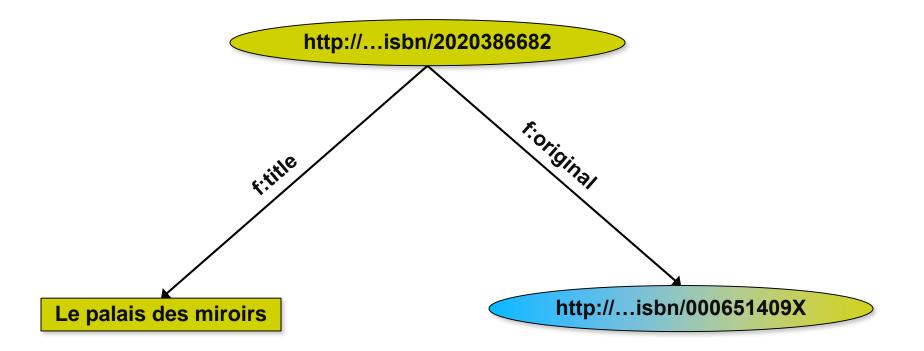
constant in FOL

 URI (Uniform Resource Identifier): a unique string of characters used to identify a resource

```
(<http://...isbn...6682>, <http://.../title>, Le palais des mirroirs)
```

RDF triples form a directed, labeled graph

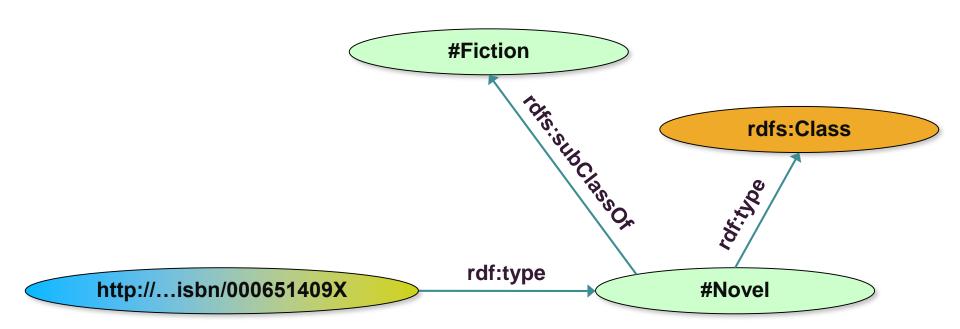
Example



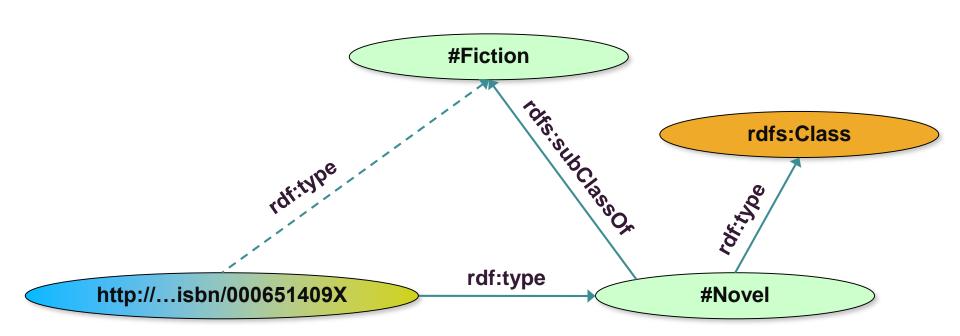
RDFS

- RDFS (RDF Schema) is used to specify the ontology (a set of constants and predicates)
 - "rdfs:Class": a collection of resources
 - novel, fiction, ...
 - "rdf:type": an individual belongs to a specific class
 - "«http://.../000651409X» is a novel"
 - "rdfs:subClassOf": all instances of one are also the instances of the other
 - "every novel is a fiction"
 - rdfs:domain, rdfs:range, rdfs:subPropertyOf, etc.

Classes, Resources, ...



Inference



```
(<http://.../isbn/000651409X> rdf:type #Fiction)
```

New triples can be inferred from RDFS rules!

Inference

- The RDF Semantics document has a list of (33) inference rules:
 - "if such and such triples are in the graph, add this and this"

```
If:
    uuu rdfs:subClassOf xxx .
    vvv rdf:type uuu .
Then add:
    vvv rdf:type xxx .
```

- Can do that recursively until the graph does not change
 - Forward chaining!

OWL

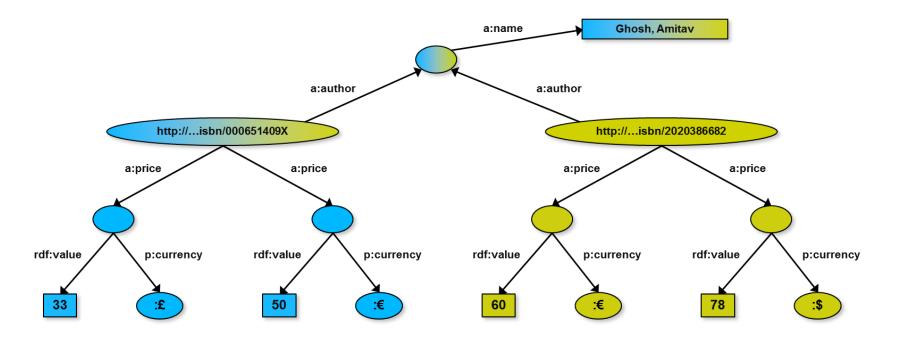
- OWL (Web Ontology Language)
 - relies on RDF Schemas
 - a lot of extensions based on description logic (DL)
 - DL: more expressive than PL, less so than FOL
 - can be used to represent:
 - Term equivalences
 - Characterization of properties (e.g., symmetric, transitive)
 - Disjointness of classes
 - Construct classes by intersection, union, complement
 - Construct classes by restricting property values
 - etc.

Querying RDF data

- In practice, complex queries into RDF data are needed
 - E.g., "give me (a,b) pairs for which there is an x such that (x parent a) and (b brother x) holds" (i.e., return the uncles)
- SPARQL (SPARQL Protocol and RDF Query Language)
 - Analogous to SQL for relational database

Example

• Returns: [<...409X>,33,:£], [<...409X>,50,:€] [<...6682>,60,:€], [<...6682>,78,:\$]



BBC Wildlife

- A BBC website on wildlife
- The whole website is automatically created from an RDF knowledge base
 - Every webpage is based on an RDF file
- Unfortunately, the site is offline since 2018 ☺
- An archive is available at https://github.com/rdmpage/bbc-wildlife

http://www.bbc.co.uk/nature/life/Equus_(genus)



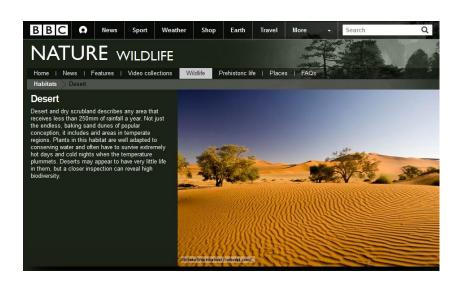
http://www.bbc.co.uk/nature/life/Equus_(genus).rdf

```
-<rdf:RDF>
 -<rdf:Description rdf:about="/nature/genus/Equus_(genus)">
     <foaf:primaryTopic rdf:resource="/nature/genus/Equus_(genus)#genus"/>
     <rd><rdfs:seeAlso rdf:resource="/nature/genus"/></rd>
   </rdf:Description>
 - <wo:Genus rdf:about="/nature/life/Equus (genus)#genus">
     <rdfs:label>Horses, donkeys and zebras</rdfs:label>
     <wo:name rdf:resource="http://www.bbc.co.uk/nature/genus/Equus (genus)#name"/>
     <foaf:depiction rdf:resource="http://ichef.bbci.co.uk/naturelibrary/images/ic/640x360/e/eq/equus genus
     /equus_genus_1. jpg"/>
   -<dc:description>
       From our own domestic horses to the iconic black and white striped zebras that roam wild on
       <a href="/nature/habitats/Temperate grasslands%2C savannas%2C and shrublands">plains and savannahs</a>
       , horses, asses and zebras are familiar to most of us. There are three species of zebra and three species of
      wild ass. There is just one species of
      <a href="/nature/life/Wild horse">horse</a>
      , and that encompasses the domestic horse.
       <br/>br/>
       <br/>br/>
      They all have a robust and sturdy appearance, long necks and a mane. Their long heads have moveable ears
      that the animals can turn towards and effectively localise sound. Each of their limbs ends in a vitally
      important hoof that encases and protects a single toe. Horses, asses and zebras are usually
      <a href="/nature/adaptations/Presociality">social</a>
      animals, living in either permanent or temporary herds on open terrains.
     </dc:description>
     <owl:sameAs rdf:resource="http://dbpedia.org/resource/Equus_(genus)"/>
     <wo:adaptation rdf:resource="/nature/adaptations/Hearing (sense)#adaptation"/>
     <wo:adaptation rdf:resource="/nature/adaptations/Herbivore#adaptation"/>
     <wo:adaptation rdf:resource="/nature/adaptations/Parental_investment#adaptation"/>
     <wo:adaptation rdf:resource="/nature/adaptations/Presociality#adaptation"/>
```

http://www.bbc.co.uk/nature/life/Equus_(genus).rdf

Connects to other resources in the dataset

Equus_(genus) wo:livesIn Deserts_and_xeric_shrublands



Habitats

The following habitats are found across the Horses, donkeys and zebras distribution range. Find out more about these environments, what it takes to live there and what else inhabits them.





Desert

Temperate grassland

www.bbc.co.uk/nature/habitats/Deserts and xeric shrublands

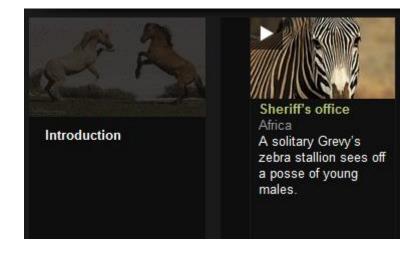
www.bbc.co.uk/nature/life/Equus_(genus)

http://www.bbc.co.uk/nature/life/Equus_(genus).rdf

Connects to resources in other BBC datasets

Equus (genus) po:Clip programmes/p014dcrj





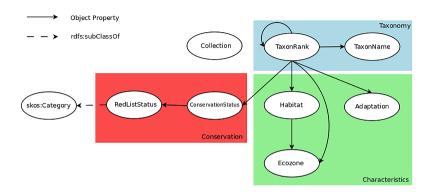
http://www.bbc.co.uk/programmes/p014dcrj

www.bbc.co.uk/nature/life/Equus_(genus)

BBC Wildlife Ontology

Ontology Diagram

The following diagram illustrates the relationships between the key classes in the ontology. A number of classes, e.g. sub classes of TaxonRank, Habitat and Adaptation have been omitted for clarity.



Ontology Terms

Automatically generated documentation for the ontology terms.

Classes

Adaptation	
URI	http://purl.org/ontology/wo/Adaptation
Description	An adaptation is any feature of an animal or plant which makes it better suited for a particular habitat or to do a particular task. For instance, being streamlined is an adaptation to swimming fast and being able to survive on very little water is an adaptation to life in the desert.
Subclasses	ExtremesAdaptation, BehaviouralPattern, CommunicationAdaptation, EcosystemRole, FeedingHabit, LifeCycle, LocomotionAdaptation, MorphologyAdaptation, PredationStrategy, ReproductionStrategy, SocialBehaviour, SurvivalStrategy
Properties	adaptation

Adapted to Extremes			

Adapted to Extremes	
URI	http://purl.org/ontology/wo/ExtremesAdaptation
Description	Organisms that are adapted to extremes (known as Extremophiles) are organisms that thrives in and even may require physically or geochemically extreme conditions that are detrimental to the majority of life on Earth.
Superclasses	Adaptation

Animal Intelligence	
URI	http://purl.org/ontology/wo/AnimalIntelligence
Description	Animal Intelligence or animal cognition is the title given to a modern approach to the mental capacities of non-human animals. It has developed out of comparative psychology, but has also been strongly influenced by the approach of ethology, behavioral ecology, and evolutionary psychology.

Behavioural Pattern	
URI	http://purl.org/ontology/wo/BehaviouralPattern
Description	Behavioural pattern describes an animal's dominant way of life. Arboreal animals, for example, live in trees and nocturnal animals are active at night.
Superclasses	Adaptation

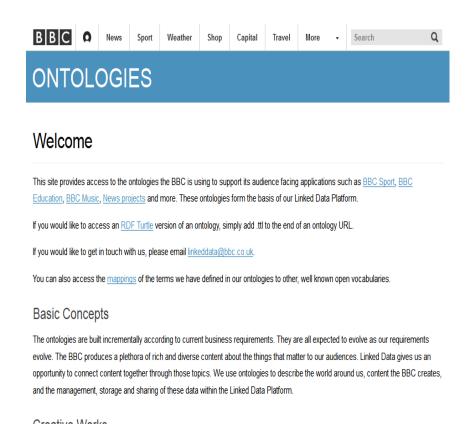
Class	
URI	http://purl.org/ontology/wo/Class
Description	A class is a scientific way to group related organisms together, some examples of classes being jellyfish, reptiles and sea urchins. Classes are big groups and contain within them smaller groupings called orders, families, genera and species.
Superclasses	TaxonRank
Properties	class

Collection	
URI	http://purl.org/ontology/wo/Collection
Description	A collection of resources, including documents, multimedia files, programme clips and their associated taxa, which aims to showcase a particular aspect of natural history film-making, or illustrate aspects of the natural world. A collection provides an alternate way to organize content over and above the basic taxonomic hierarchy.
Superclasses	http://purl.org/dc/dcmitype/Collection
Properties	collection

Communication Adaptation	
URI	http://purl.org/ontology/wo/CommunicationAdaptation

http://www.bbc.co.uk/ontologies

- 14 domain ontologies
 - Core Concepts Ontology
 - Programmes Ontology
 - Business News Ontology
 - Politics Ontology
 - Food Ontology
 - Sport Ontology
 - Wildlife Ontology
 -



Summary

- First-order logic:
 - objects and relations are semantic primitives
 - syntax: constants, functions, predicates, quantifiers
- Inference
 - Unification
 - Forward/backward chaining
 - Resolution
- Semantic web
 - Application of predicate logic to WWW