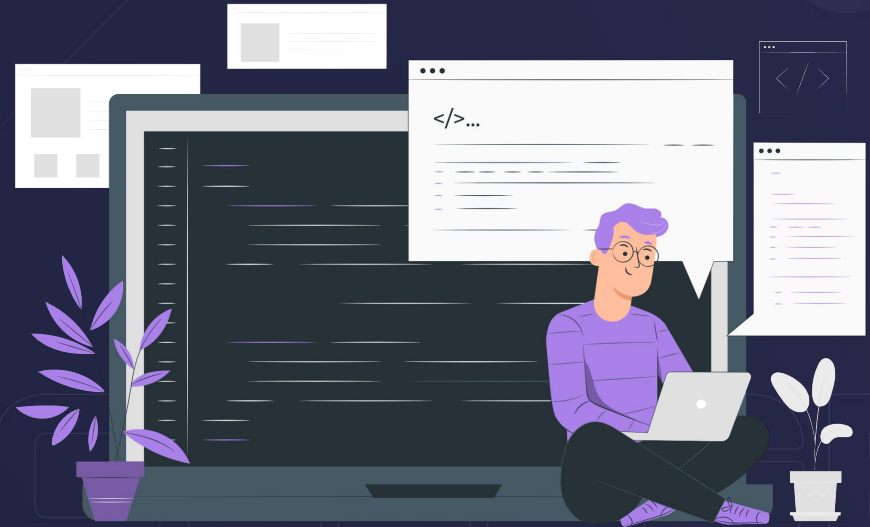


Lecture – 52

Binary Trees

[Basics]



Prerequisites

- Recursion → must
- Linked List

↓
trees will become easy

```
void pip(int n){
    Kaam → pre
    pip(n-1);
    Kaam → in
    pip(n-1);
    Kaam → post
}
```

Today's Checklist

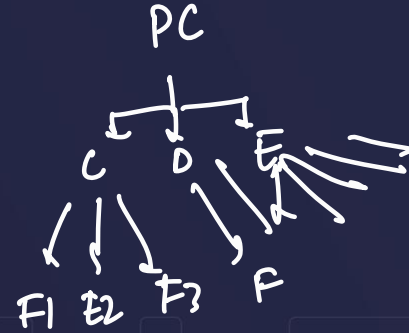
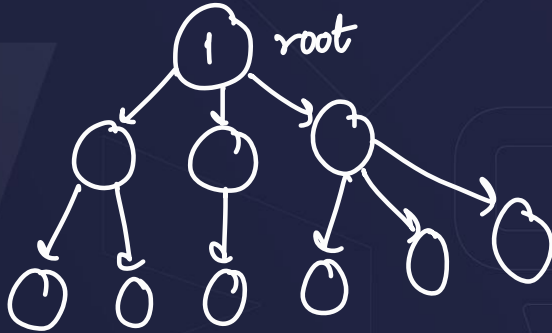
- What is a Tree data structure
- Representation
- Terminology
- Important properties of trees
- Types of Trees
- Applications of tree data structure
- What is a Binary Tree?
- Implementation
- Traversals → *Next Lecture*
- Problems
- Types of Binary Trees

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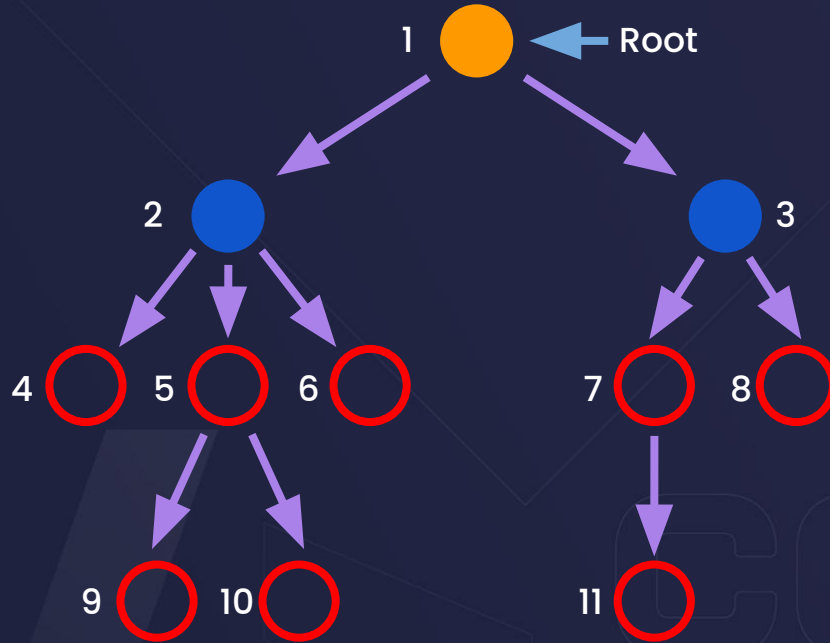
What is a Tree data structure

Array, LL, stack, queues → Linear Data Structure

Trees, graphs → non linear D.S.

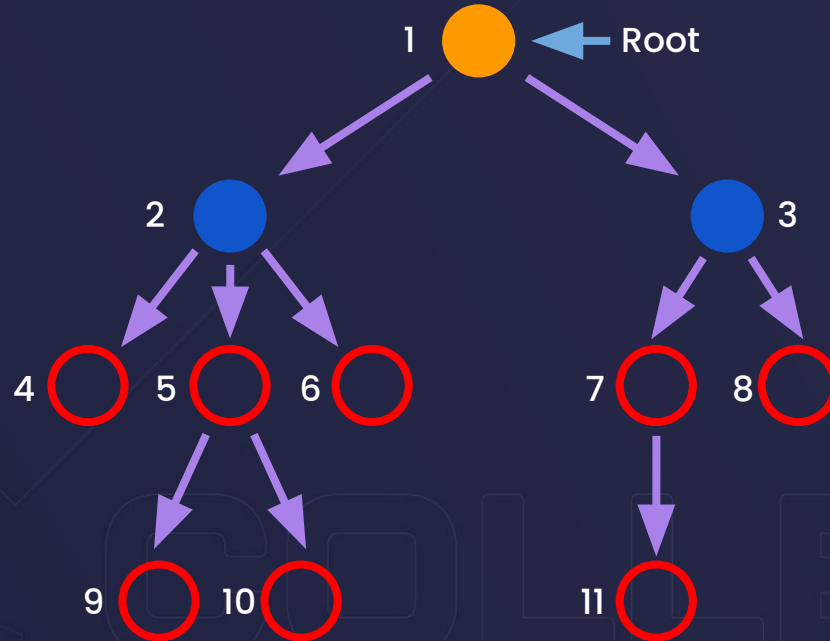


Representation



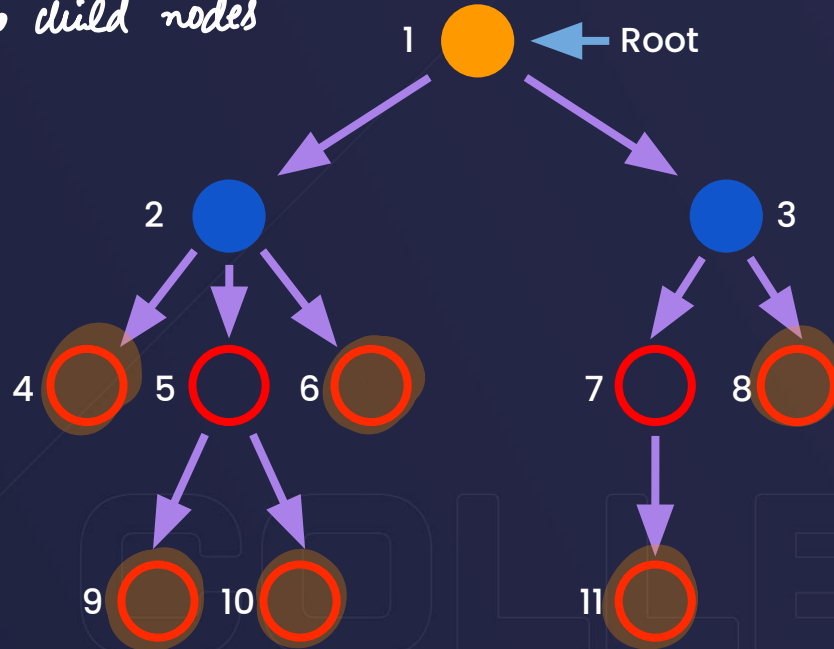
Terminology

1. Root
2. Child Node
3. Parent Node
4. Sibling Nodes



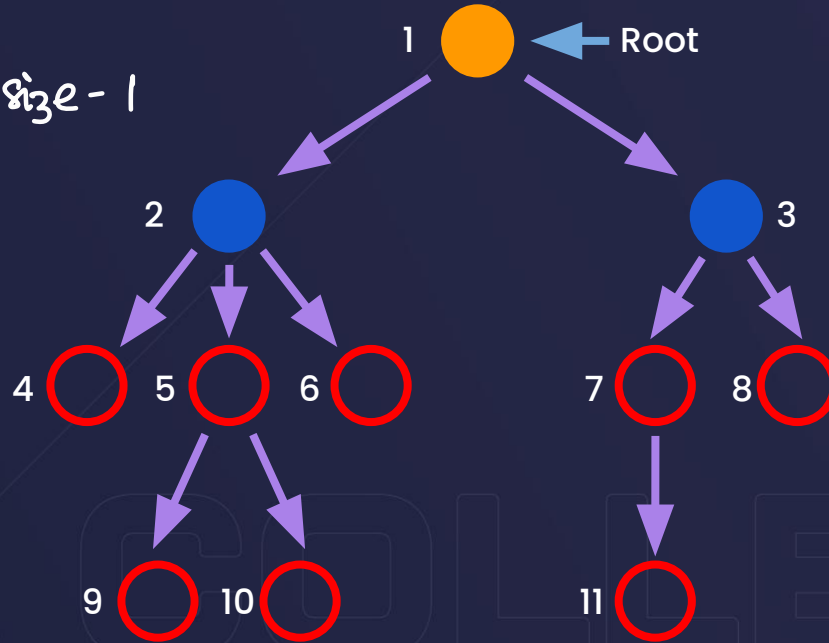
Terminology

- 5. Leaf Node → with no child nodes
- 6. Internal Node
- ✓ 7. Ancestor Node
- 8. Descendant Node



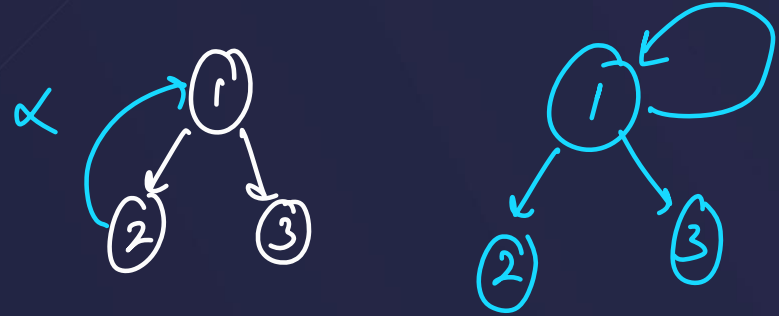
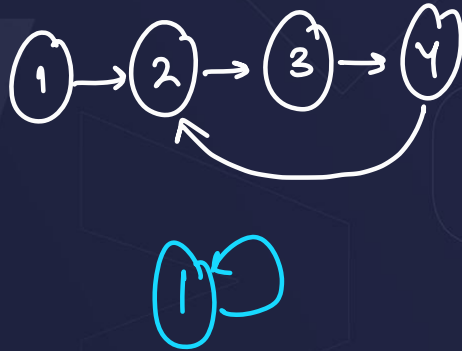
Terminology

- 9. Level
- 10. Number of edges = $size - 1$
- 11. Height = level - 1
- 12. Size = no. of nodes



Important Properties of trees

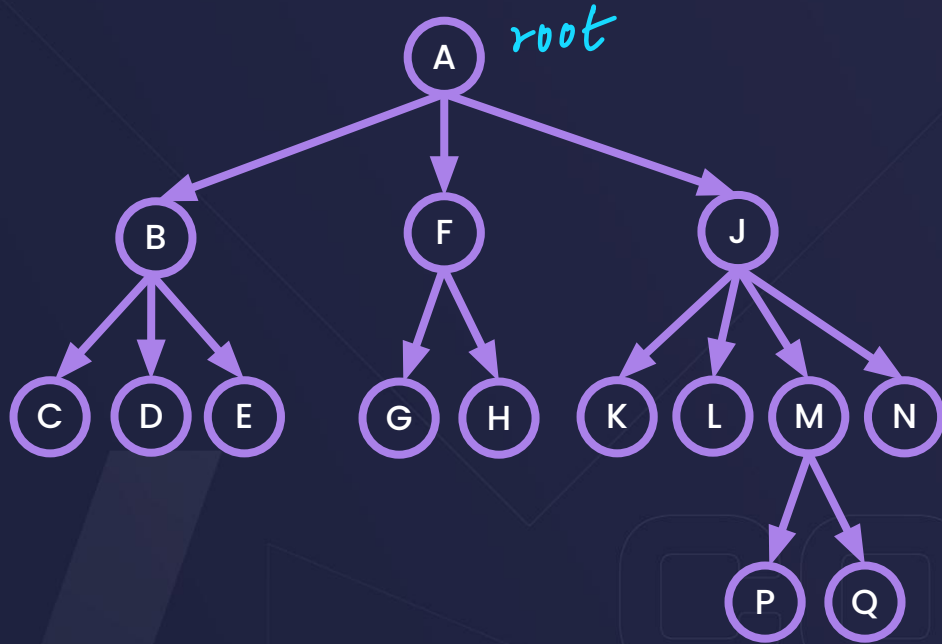
1. Traversing in a tree is done by depth first search and breadth first search algorithm.
2. It has no loop and no circuit.
3. It has no self-loop.



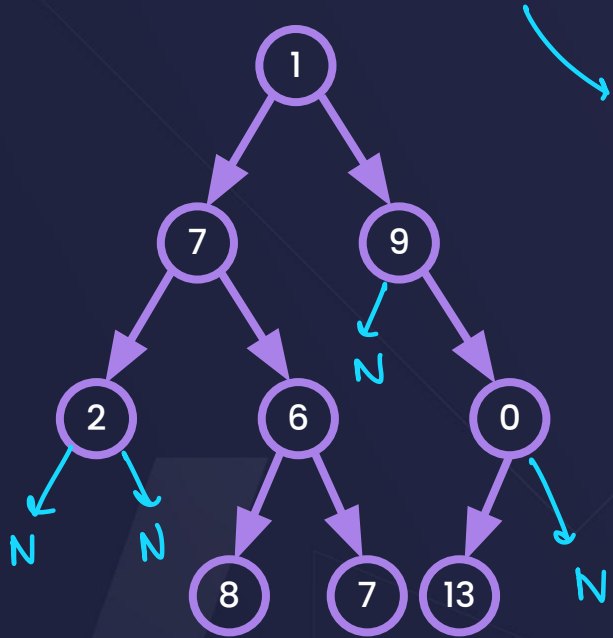
Types of Trees

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1. Generic Trees → multiple children



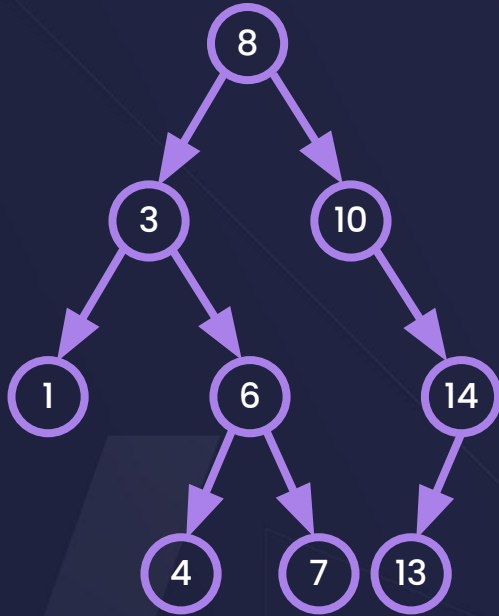
2. Binary Trees → 0, 1, 2 children [upto 2 child nodes]



Every node has a value, &
its left child's address, right child's
address

3. Binary Search Trees : Binary trees

with some special property



Bad me

4. AVL Trees : *Balanced BST's*



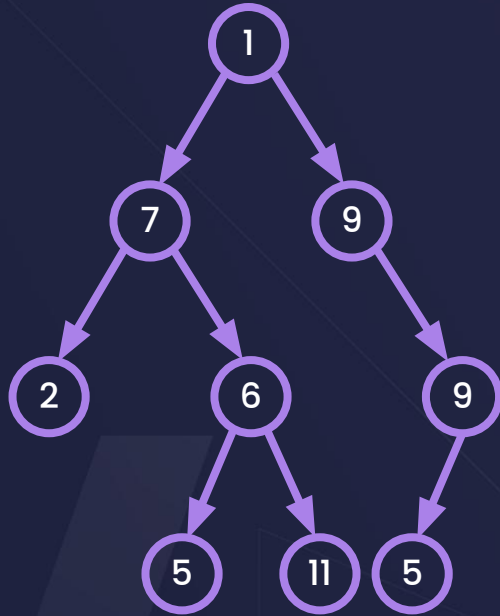
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Applications of tree Data Structure

1. Hierarchical data structure
2. Searching efficiency
3. Sorting
4. Dynamic Data
5. Efficient Insertion and Deletion
6. Easy to implement

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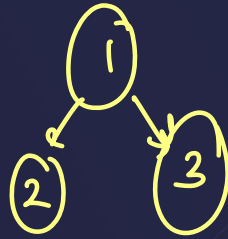
What are Binary Trees? → 0, 1, 2 child nodes



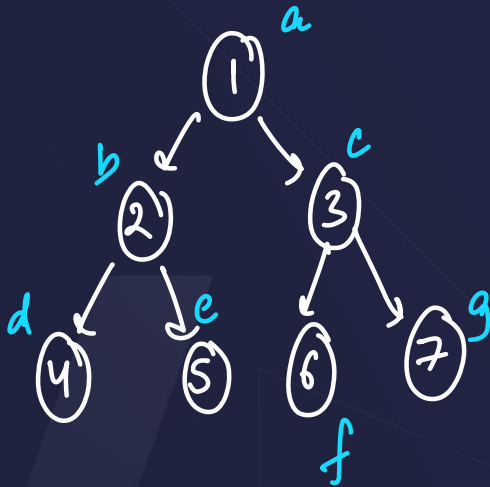
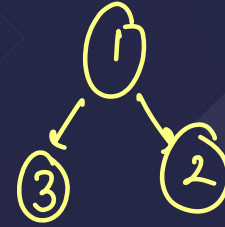
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Implementation

Creating a Node class



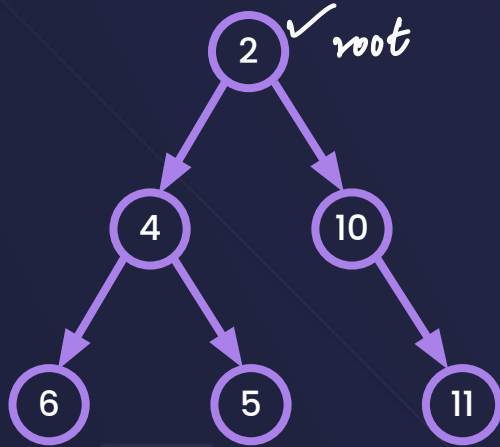
\neq



1 2 4 5 3 6 7

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Display (root of tree) (just like in LL \rightarrow head only)

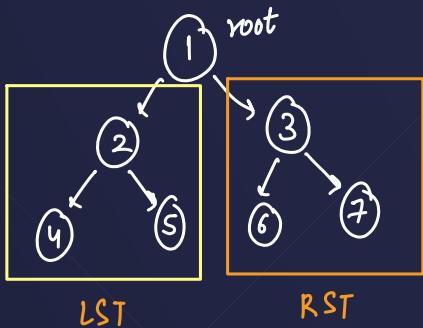


```

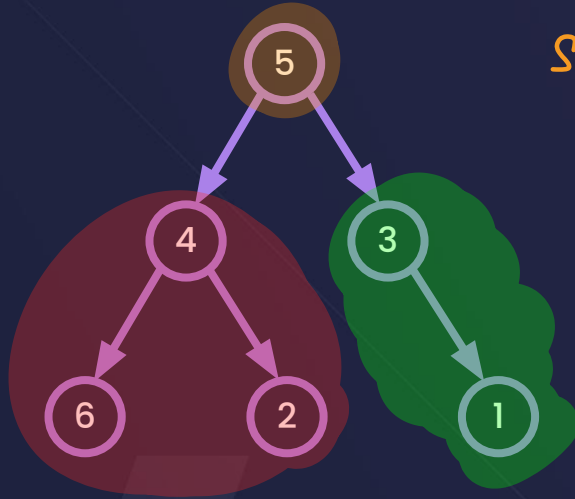
display(head) {
    if (root == NULL) —
        cout << head->val;
    display(head->next);
}
    
```

3

Left - Subtree Δ Right - Subtree



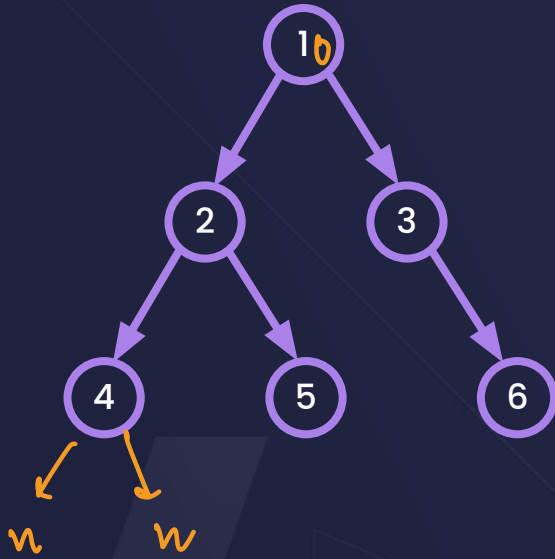
Find sum of tree nodes



$$\text{Sum} = \text{root} \rightarrow \text{val} + \text{LST} + \text{RST}$$

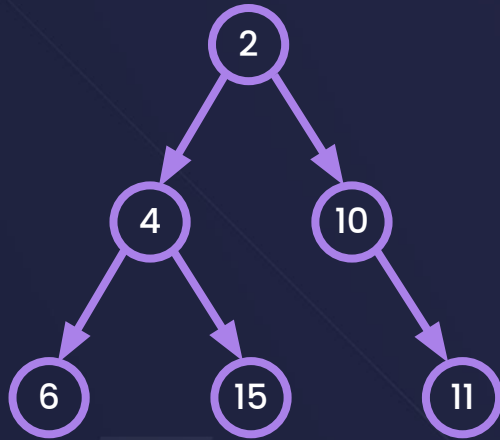
$$\begin{aligned} \text{Sum}(\text{root}) &= \text{root} \rightarrow \text{val} + \text{Sum}(\text{root} \rightarrow \text{left}) \\ &\quad + \text{Sum}(\text{root} \rightarrow \text{right}) ; \end{aligned}$$

Find size of Binary Tree *→ Try it yourself first*



$$\text{Size}(\text{root}) = 1 + \text{size}(\text{root} \rightarrow \text{left}) + \text{size}(\text{root} \rightarrow \text{right})$$

Find node with max value



if (root == NULL) return INT_MIN;

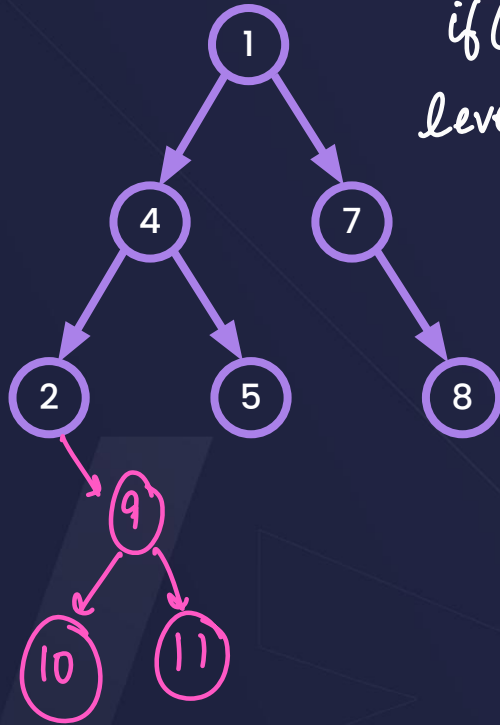
$\text{max}(\text{root}) = \text{max}(\text{root-val}, \text{max}(\text{left}), \text{max}(\text{right}))$

a, b, c
↓

$\text{max}(a, \text{max}(b, c));$

no. of levels

Find height of Binary Tree



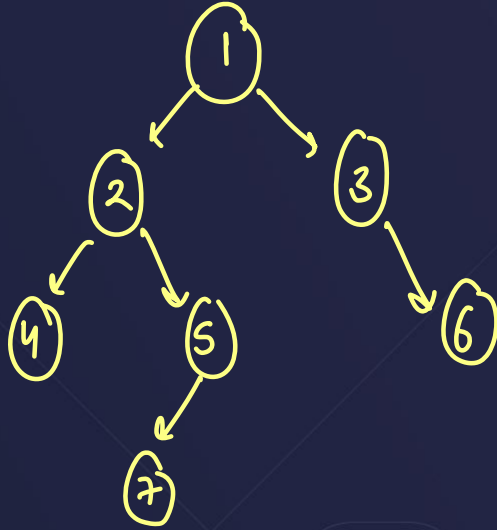
if (root == NULL) return 0;

$$\text{levels}(\text{root}) = 1 + \max(\text{levels}(\text{root} \rightarrow \text{left}), \text{levels}(\text{root} \rightarrow \text{right}))$$

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Ques: Diameter of Binary Tree

[LeetCode 543]

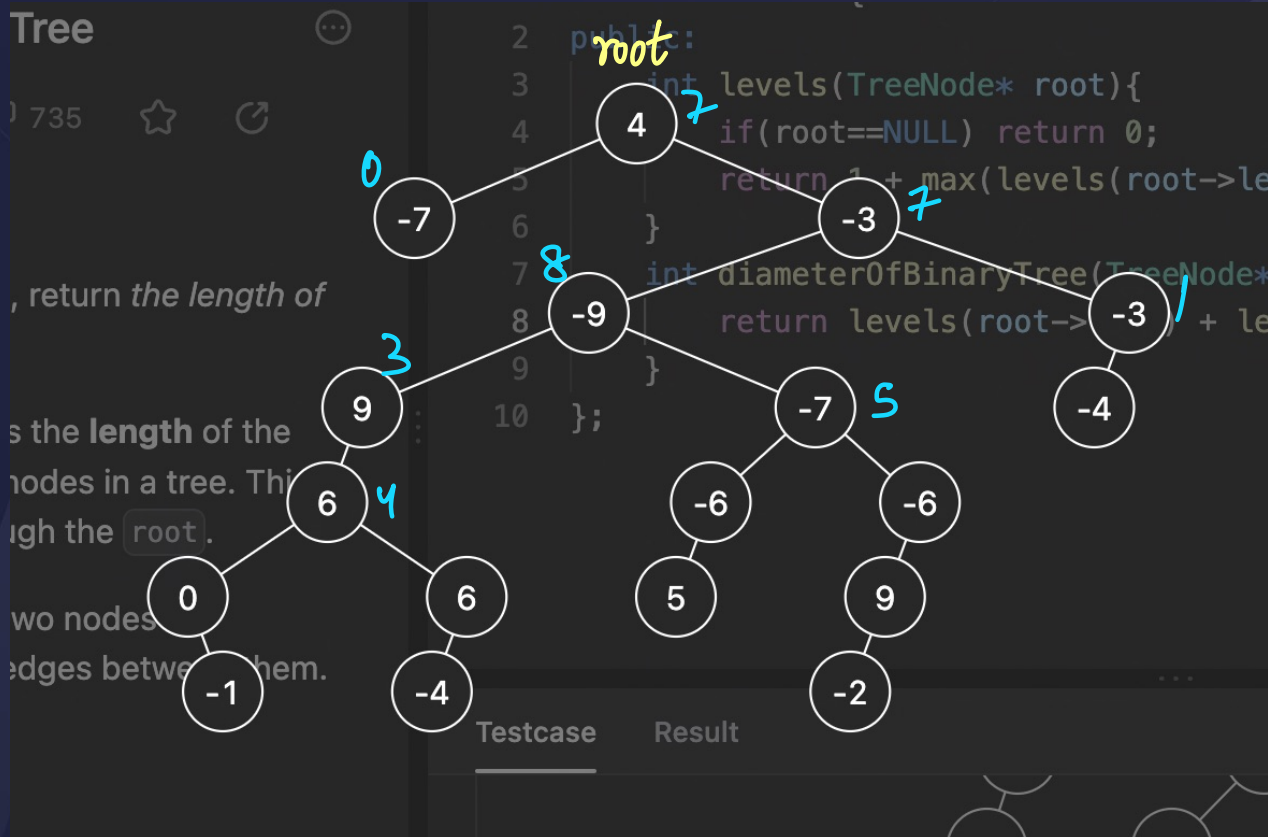


Approach 1: Diameter (longest path b/w any 2 nodes)

= no. of levels in LST + levels (RST)

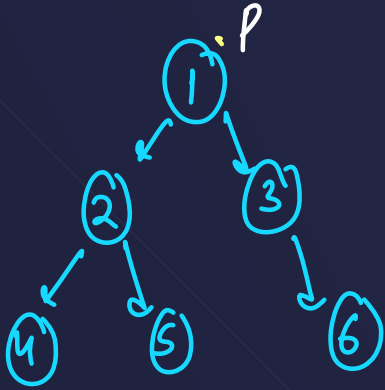
Ques: Diameter of Binary Tree

[LeetCode 543]



Ques: Same Tree

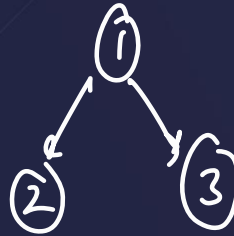
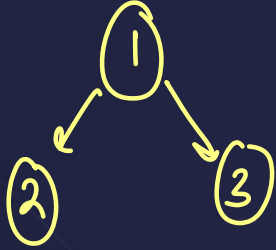
[LeetCode 100]



- 1) if ($p \neq q$) return false;
- 2) bool LSTans = isSameTree($p \rightarrow \text{left}$, $q \rightarrow \text{left}$), \rightarrow
- 3) bool RSTans = isSameTree($p \rightarrow \text{right}$, $q \rightarrow \text{right}$) \rightarrow false
- 4) return true

Ques: Same Tree

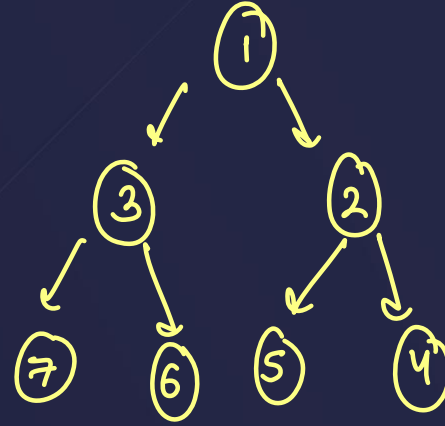
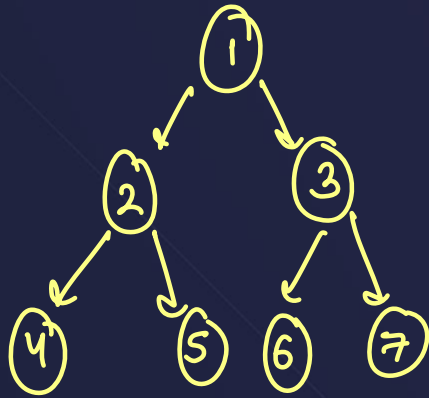
[LeetCode 100]



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Ques: Invert Binary Tree

[LeetCode 226]

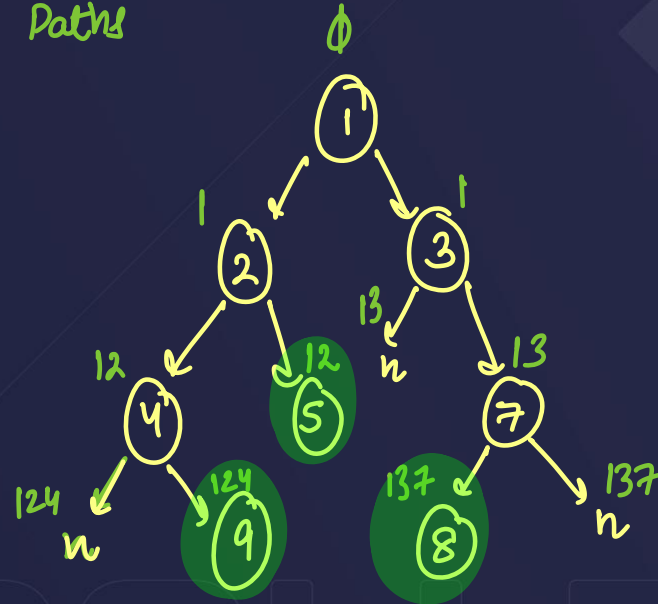
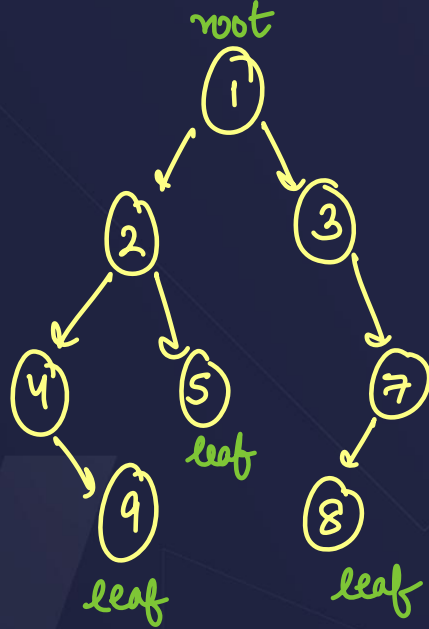


Ques: Binary Tree Paths

[LeetCode 257]

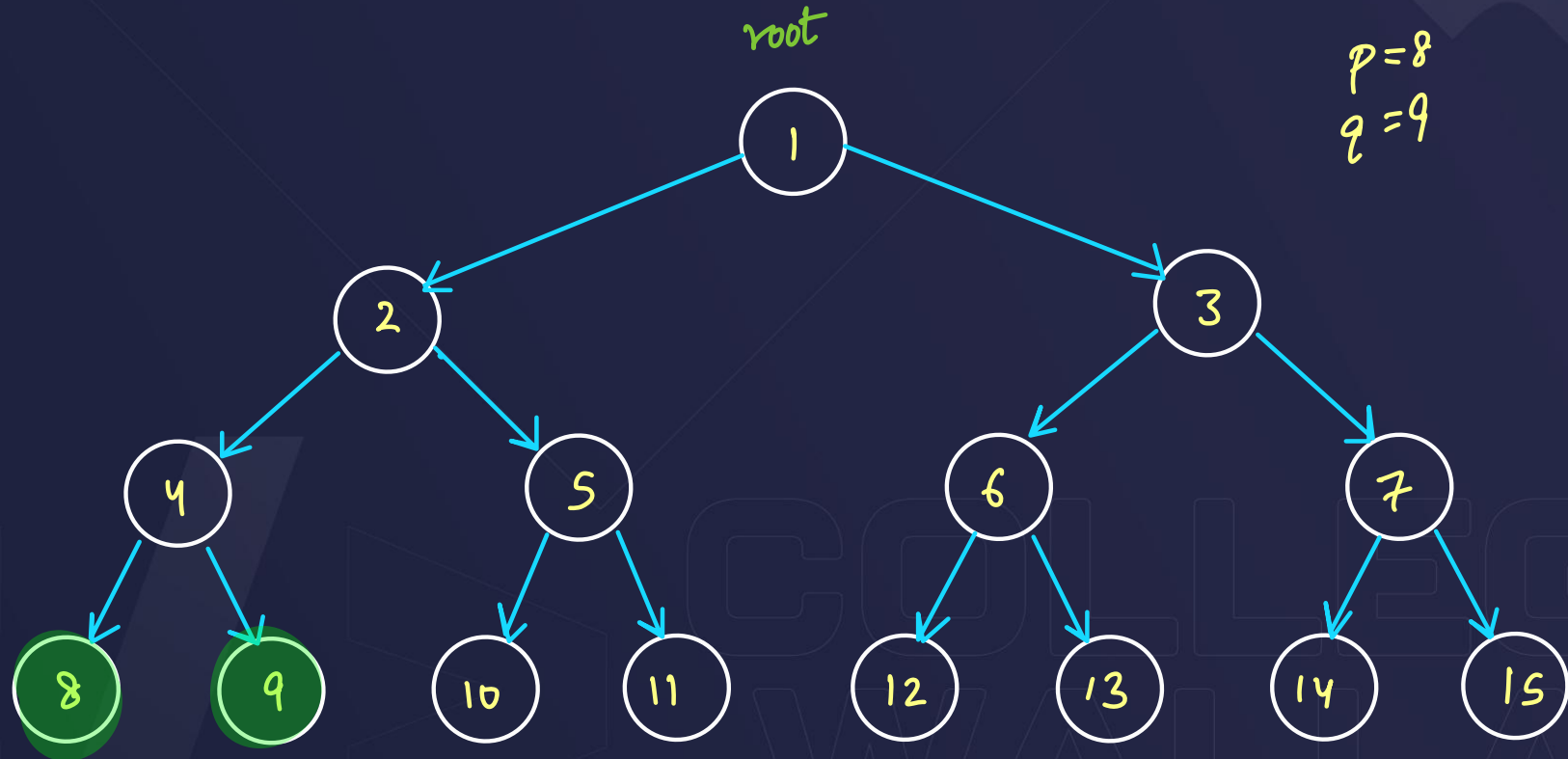
$\emptyset = ""$

Root to Leaf Paths



→ { "1249", "125", "1378" }

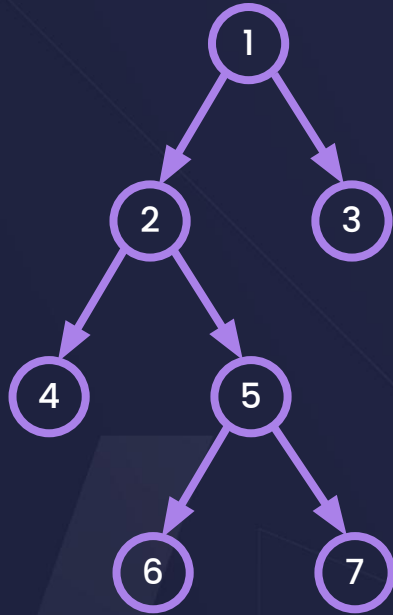
Ques: Lowest Common Ancestor of a Binary Tree (LCA) [LeetCode 236]



Types of Binary Trees

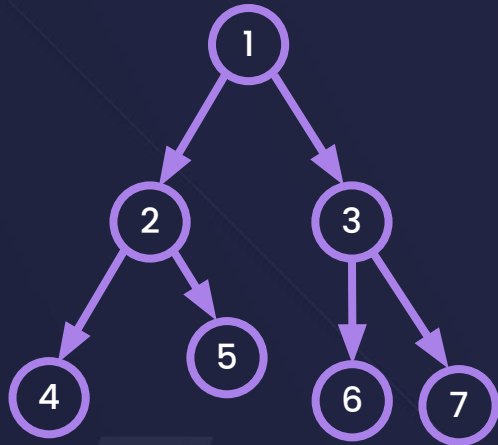
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1. Full Binary Tree (0 or 2)



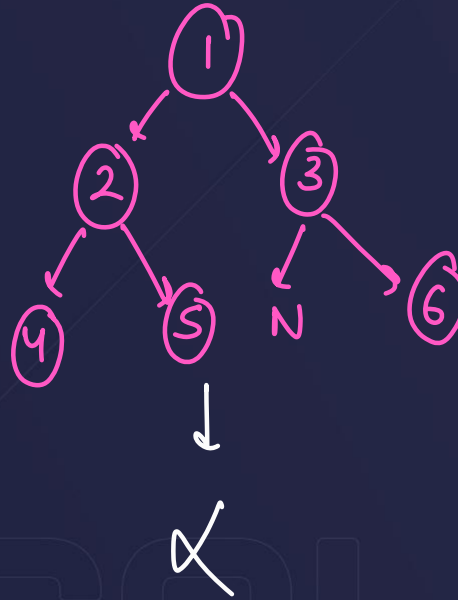
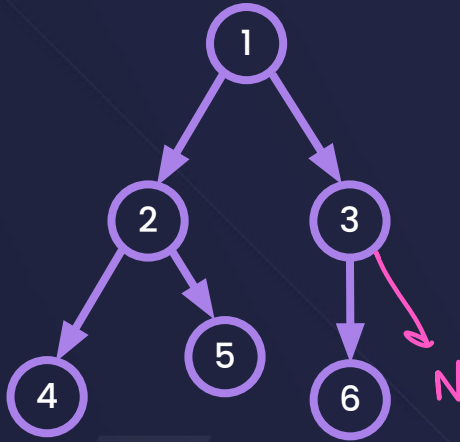
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2. Perfect Binary Tree



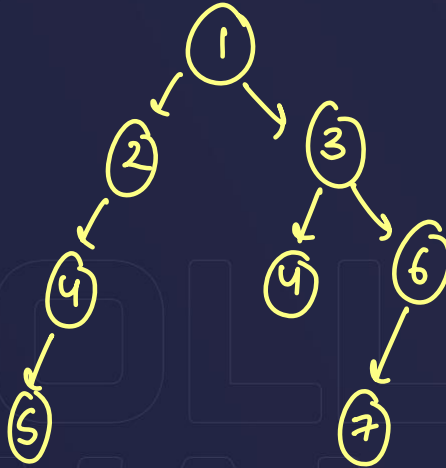
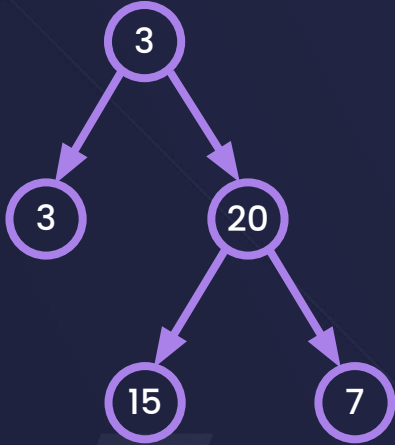
↓
Every Node (except the last level leaf nodes)
has 2 child nodes
the last level has 0 child

3. Complete Binary Tree



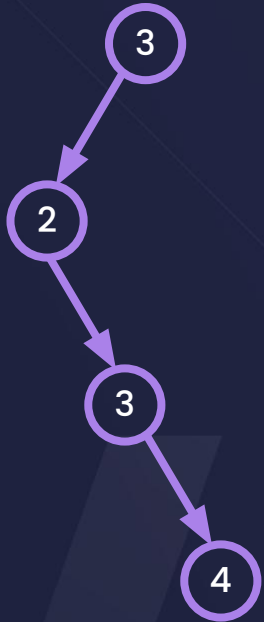
4. Balanced Binary Tree : "Important"

↓
For every node, the difference b/w the levels of LST & RST should be atmost 1.



5. Degenerate and Skewed Binary Trees

↓
0 or 1 child



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Summary

- In this lecture , we studied about the Tree data structure.
- We studied its representation.
- We studied about its terminology.
- We studied about various types of Trees.
- We studied about Binary trees
- We studied about its implementation.
- We studied the various traversals on binary trees.
- We solved some problems on binary trees.
- We studied about the various types of Binary trees.

Next Lecture

- ~~Interview problems on binary trees~~

Traversals in Trees

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▶ **THANK YOU** ◀

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