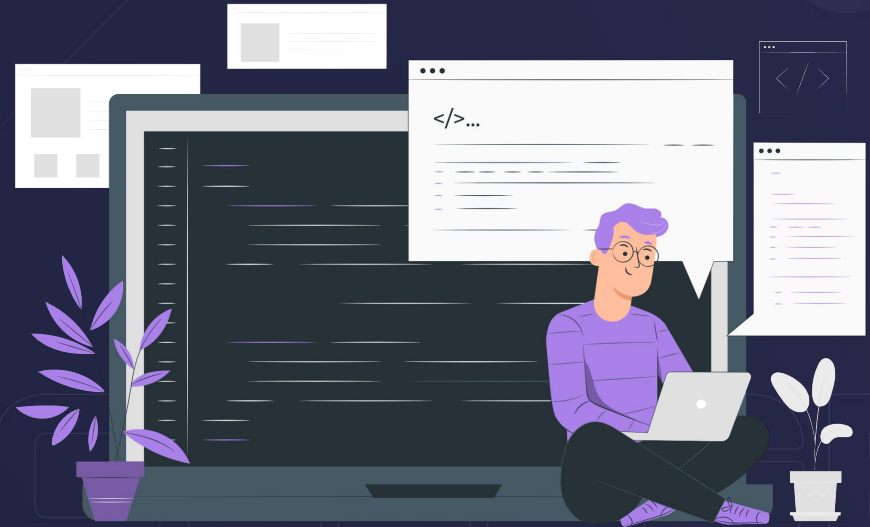


# Lecture – 53

## Binary Trees

### [Traversals]



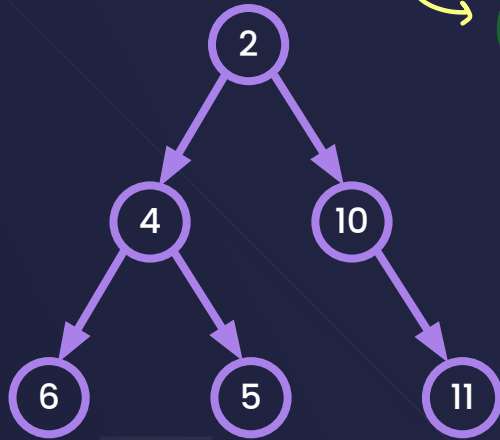
# Recap

- Types of Trees, Terminology, (Size, Sum, Max, height) problems
- Some Leetcode questions

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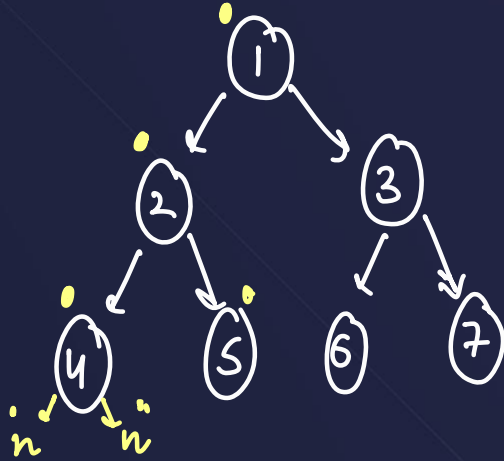
**Traversals** → to visit every node/member/ element

↪ DFS, BFS, Morris Traversal



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# 1. Preorder Traversal



Output

• 1 2 4 5 3 6 7

```
void display(Node* root){
    if(root==NULL) return; // base case
    cout<<root->val<<" "; // work
    display(root->left); // call 1
    display(root->right); // call 2
}
```

# 1. Preorder Traversal

Root Left Right



$\Rightarrow 1 (2 4 5 8 9 10) (3 6 7 11)$

$\Rightarrow 1 2 4 8 5 9 10 (3 6 7 11)$

$\Rightarrow 1 2 4 8 5 9 10 3 6 11 7$

T.C. =  $O(n)$  [where 'n' is the no. of nodes]

S.C. =

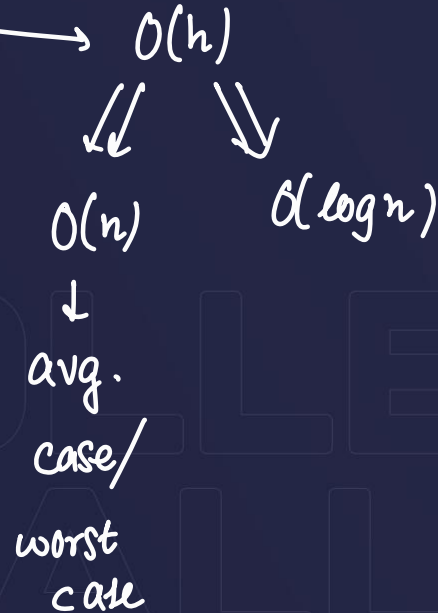
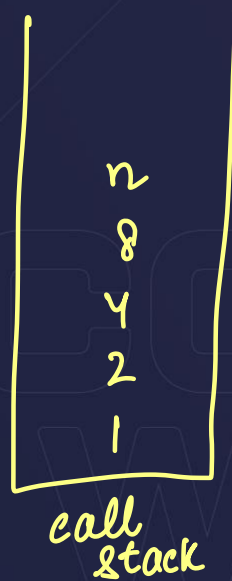
1 2 4 8 5 9 10 3 6 11 7

# 1. Preorder Traversal



T.C. =  $O(n)$  [where 'n' is the no. of nodes]

S.C. =  $O(\text{levels} + 1) \approx O(h + 2) \approx O(h)$



Degenerate

Trees

(Worst Case)



→ Pre/In/Post :  $TC = O(n)$   
 $SC = O(n)$  or  $O(h)$

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# Balanced Trees :



$$S.C. = O(h) = O(\log n)$$

$$1 + 2^1 + 2^2 \dots 2^h = n$$

$$\Rightarrow \frac{1(2^{h+1} - 1)}{2 - 1} = n$$

$$\Rightarrow 2^h = \frac{n+1}{2} \Rightarrow h = \log_2 \left( \frac{n+1}{2} \right)$$



## 2. Inorder Traversal

Left Root Right



$\Rightarrow (2 \ 4 \ 5) \mid (3 \ 6 \ 7)$

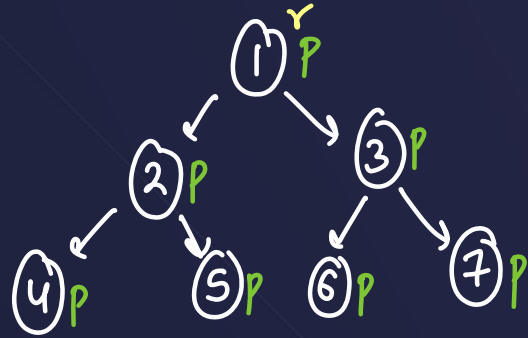
4 2 5 1 6 3 7

4 2 5 1 6 3 7

4 2 5 1 6 3 7

### 3. Postorder Traversal

Left Right Root



$\Rightarrow (2 \ 4 \ 5) \ (3 \ 6 \ 7) \ 1$

$\Rightarrow 4 \ 5 \ 2 \ 6 \ 7 \ 3 \ 1$

# Ques: Binary Tree Preorder Traversal

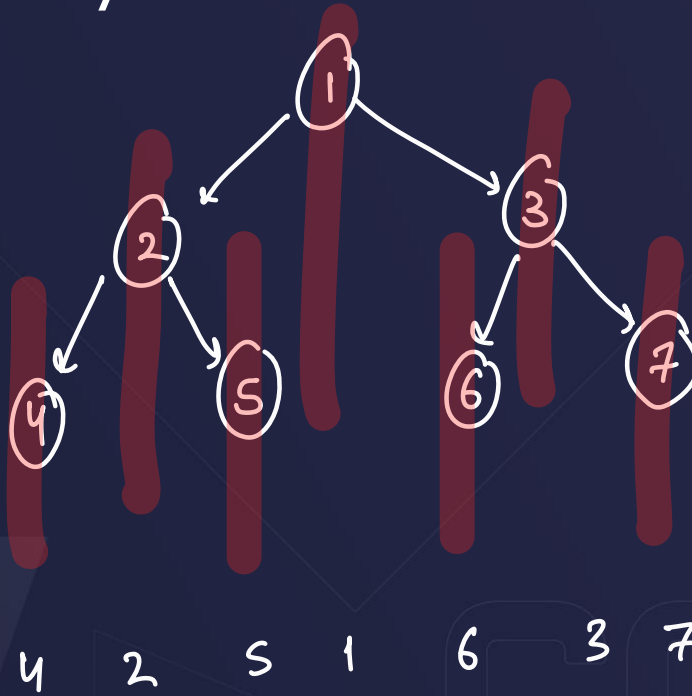
[LeetCode 144]



1 2 4 5 3 6 7  
 ↓  
 preorder

# Ques: Binary Tree Inorder Traversal

[LeetCode 94]



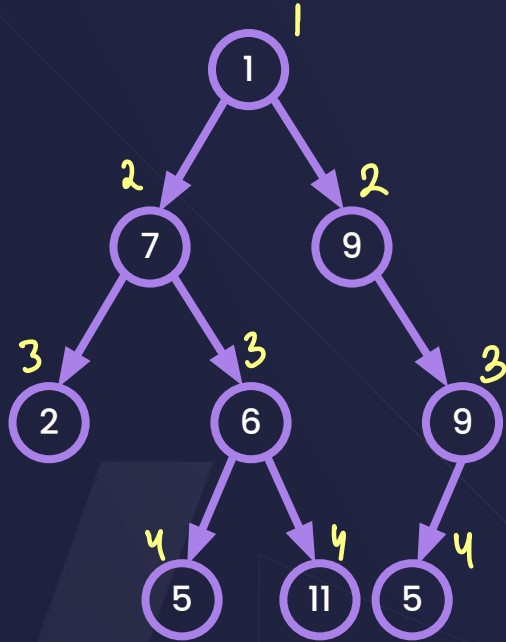
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**Ques:** Binary Tree Postorder Traversal

**[LeetCode 145]**

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Q: Print elements of nth level



$n = 3$

2 6 4

```

void print(root, curr, level){
    if(curr == level) cout << root->val;
    print(root->left, curr+1, level);
    print(root->right, curr+1, level);
}
  
```



$n^{\text{th}}$  Level : Homework  $\rightarrow$  T.C. & S.C

```
void nthLevel(Node* root, int curr, int level){  
    if(root==NULL) return; // base case  
    if(curr==level) cout<<root->val<<" "; // root  
    nthLevel(root->left, curr+1, level); // left  
    nthLevel(root->right, curr+1, level); // right  
}
```

these are needless/extra  
if you have already reached  
the reqd level



# Optimised $n^{\text{th}}$ Level : Homework T.C. & S.C

```
void nthLevel(Node* root, int curr, int level){  
    if(root==NULL) return; // base case  
    if(curr==level){  
        cout<<root->val<<" "; // root  
        return;  
    }  
    nthLevel(root->left, curr+1, level); // left  
    nthLevel(root->right, curr+1, level); // right  
}
```

T.C. =

S.C. =

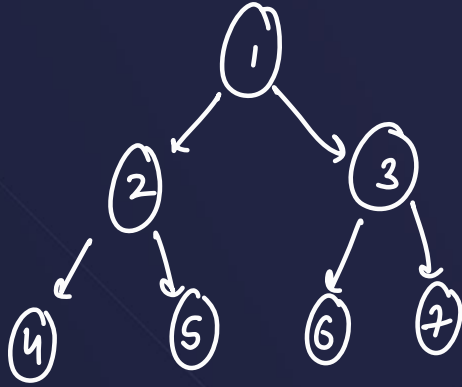
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# Level order traversal (~~BFS~~)

$n^{\text{th}}$  Level (DFS)

loop



$\Rightarrow$  1 2 3 4 5 6 7

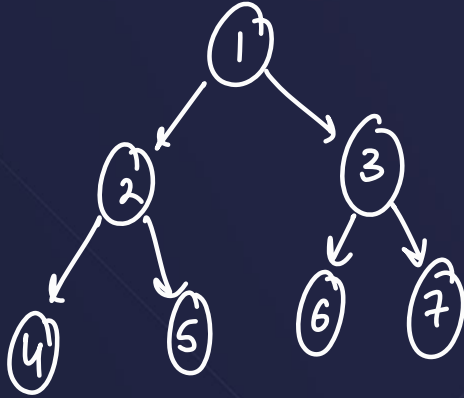
$\Rightarrow$

1

2 3

4 5 6 7

## \*Level order traversal (Right to Left)



⇒

1 3 2 7 6 5 4

or

1

3 2

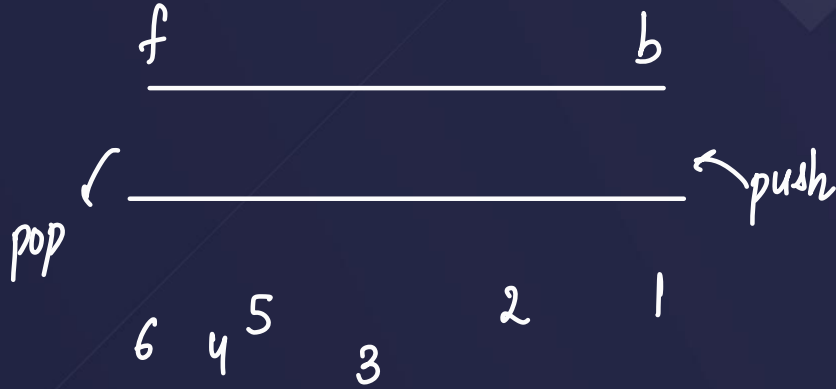
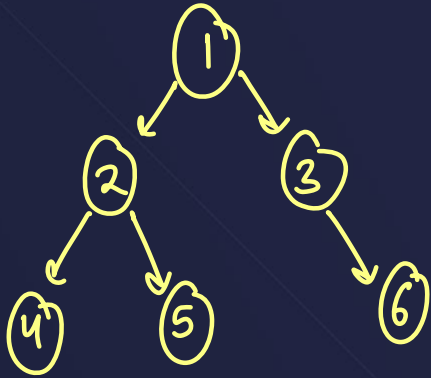
7 6 5 4

Ques: Binary Tree Level Order Traversal

[LeetCode 102]

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# Level order traversal (Using Queue) BFS



queue <Node\*> q;

Steps:

- 1) Node\* temp = q.front(), q.pop(), print
- 2) push temp->left & temp->right to q

1 2 3 4 5 6

# Construct Tree from Level order traversal

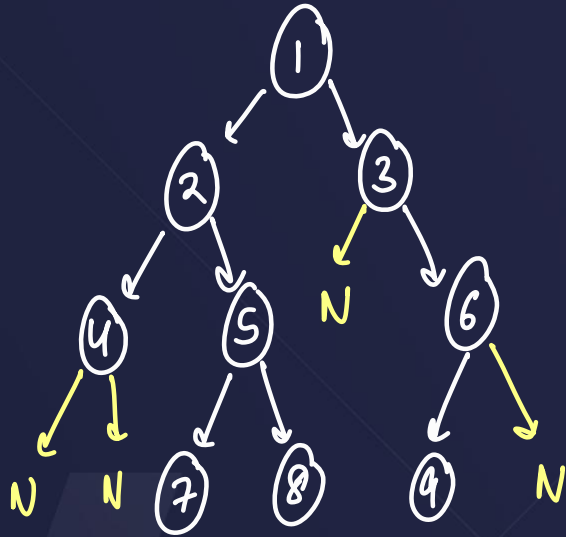
↓

I give an array, For ex → 1 2 3 4 5 6 7

{3, 9, 20, N, N, 15, 7}



# Construct Tree from Level order traversal



$\{ 1, 2, 3, 4, 5, N, 6, N, N, 7, 8, 9, N \}$

# Construct Tree from Level order traversal (queue)

{ 1, 2, 3, 4, 5, N, 6, N, N, 7, 8, 9 }

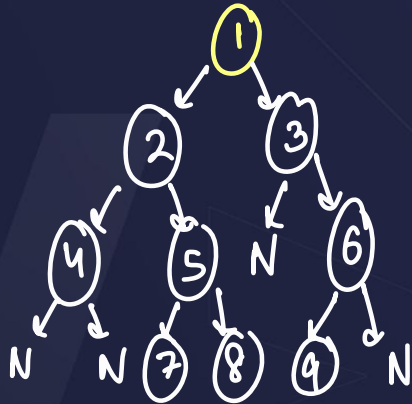
$q$   $i$   $f$   $j$   $b$   


---

 7 8 9  


---

Node\* root = new Node(arr[0])



N → INT\_MIN

Steps : Node\* temp = q.front(), q.pop()

Node\* l = new Node(arr[i])

Node\* r = new Node(arr[j])

temp → left = l

temp → right = r → q.push(l), r

i += 2;

j += 2;

2 3  
 4 5  
 6 9



▶ **THANK YOU** ◀

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