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EE24BTECH11004 - ANKIT JAINAR

- 1) The probability that a relation R from $\{x, y\}$ to $\{x, y\}$ is both symmetric and transitive, is equal to:
 - a) $\frac{5}{16}$
 - b) $\frac{9}{16}$ c) $\frac{11}{16}$
 - d) $\frac{16}{16}$
- 2) The number of values of $a \in \mathbb{N}$ such that the variance of 3, 7, 12, a, 43 a is a natural number is:
 - a) 0
 - b) 2
 - c) 5
 - d) infinite
- 3) From the base of a pole of height 20 meters, the angle of elevation of the top of a tower is 60° . The pole subtends an angle 30° at the top of the tower. Then the height of the tower is:
 - a) $15\sqrt{3}$
 - b) $20\sqrt{3}$
 - c) $20 + 10\sqrt{3}$
 - d) 30
- 4) Negation of the Boolean statement $(p \lor q) \Rightarrow ((\neg r) \lor p)$ is equivalent to:
 - a) $p \wedge (\neg q) \wedge r$
 - b) $(\neg p) \land (\neg q) \land r$
 - c) $(\neg p) \land q \land r$
 - d) $p \wedge q \wedge (\neg r)$
- 5) Let $n \ge 5$ be an integer. If $9^n 8n 1 = 64\alpha$ and $6^n 5n 1 = 25\beta$, then $\alpha \beta$ is equal to:
 - a) $1 + {^n}C_2(8-5) + {^n}C_3(8^2-5^2) + \dots + {^n}C_n(8^{n-1}-5^{n-1})$
 - b) $1 + {^n}C_3(8-5) + {^n}C_4(8^2-5^2) + \dots + {^n}C_n(8^{n-2}-5^{n-2})$
 - c) ${}^{n}C_{3}(8-5) + {}^{n}C_{4}(8^{2}-5^{2}) + \dots + {}^{n}C_{n}(8^{n-2}-5^{n-2})$
 - d) ${}^{n}C_{4}(8-5) + {}^{n}C_{5}(8^{2}-5^{2}) + ... + {}^{n}C_{n}(8^{n-3}-5^{n-3})$
- 6) Let $\mathbf{a} = \hat{i} 2\hat{j} + 3\hat{k}$, $\mathbf{b} = \hat{i} + \hat{j} + \hat{k}$, and \mathbf{c} be a vector such that $\mathbf{a} + (\mathbf{b} \times \mathbf{c}) = 0$ and $\mathbf{b} \cdot \mathbf{c} = 5$. Then, the value of $3(\mathbf{c} \cdot \mathbf{a})$ is:
 - a) 10
 - b) 15
 - c) 20
 - d) 25
- 7) Let y = y(x), x > 1, be the solution of the differential equation $(x 1)\frac{dy}{x} + 2xy = \frac{1}{x 1}$ with $y(2) = \frac{1 + e^4}{2e^4}$. If $y(3) = \frac{e^{\alpha} + 1}{\beta e^{\alpha}}$, then the value of $\alpha + \beta$ is equal to
- 8) Let 3, 6, 9, 12, ... up to 78 terms and 5, 9, 13, 17, ... up to 59 terms be two series. The sum of the terms common to both series is:
 - a) 378
 - b) 405
 - c) 450
 - d) 495
- 9) The number of solutions of the equation $\sin x = \cos^2 x$ in the interval (0, 10) is:

- a) 1
- b) 2
- c) 3
- d) 4
- 10) The total number of four-digit numbers such that each of the first three digits is divisible by the last digit, is equal to
- 11) For real numbers a, b (a > b > 0), let Area $\{(x, y) : x^2 + y^2 \le a^2 \text{ and } \frac{x^2}{a^2} + \frac{y^2}{b^2} \ge 1\} = 30\pi$ and Area $\{(x, y) : x^2 + y^2 \le a^2 \text{ and } \frac{x^2}{a^2} + \frac{y^2}{b^2} \ge 1\} = 30\pi$ and Area $\{(x, y) : x^2 + y^2 \le a^2 \text{ and } \frac{x^2}{a^2} + \frac{y^2}{b^2} \ge 1\}$
- 12) Let f and g be twice differentiable even functions on (-2,2) such that $f\left(\frac{1}{4}\right) = 0$, $f\left(\frac{1}{2}\right) = 0$, f(1) = 1, and $g\left(\frac{3}{4}\right) = 0$, g(1) = 2. Then, the minimum number of solutions of f(x)g''(x) + f'(x)g'(x) = 0 in (-2,2) is equal to
- 13) Let $M = \begin{bmatrix} 0 & -\alpha \\ \alpha & 0 \end{bmatrix}$, where α is a non-zero real number, and $N = \sum_{k=1}^{49} M^{2k}$. If $(I M^2)N = -2I$, then the positive integral value of α is:
 - a) 1
 - b) 2
 - c) 3
 - d) 4
- 14) Let the coefficients of x^{-1} and x^{-3} in the expansion of $\left(2x^5 \frac{1}{x^5}\right)^{15}$, x > 0, be m and n respectively. If r is a positive integer such that $mn^2 = {}^{15}C_r, 2^r$, then the value of r is equal to
- 15) Let f(x) and g(x) be two real polynomials of degree 2 and 1, respectively. If $f(g(x)) = 8x^2 2x$, and $g(f(x)) = 4x^2 + 6x + 1$, then the value of f(2) + g(2) is