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## Assignment 5

## AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

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## CBSE Probability Grade 10

Exercise 15.1.10 A piggy bank contains hundred 50 p coins, fifty  $\mathbf{\xi}$  1 coins, twenty  $\mathbf{\xi}$  2 coins and ten  $\mathbf{\xi}$  5 coins. If it is equally likely that one of the coins will fall out when the bank is turned upside down, what is the probability that the coin:

- (i) will be a 50 p coin?
- (ii) will not be a ₹ 5 coin?

**Solution.** Let a random variable  $X \in \{0, 1, 2, 3\}$  denote the possible outcomes of obtaining a random coin from the piggy bank.

X	Outcome	Number
0	50 p	$\Pr(X=0) = \frac{100}{180} = \frac{5}{9}$
1	₹ 1	$\Pr(X=1) = \frac{50}{180} = \frac{5}{18}$
2	₹ 2	$\Pr(X=2) = \frac{20}{180} = \frac{1}{9}$
3	₹ 5	$Pr(X = 3) = \frac{10}{180} = \frac{1}{18}$

TABLE 1

(i) The probability that the coin will be a 50 p coin is given by:

$$\Pr(X=0) = \frac{n(X=0)}{\sum_{i=0}^{3} n(X=i)} = \frac{100}{180}$$
 (1)

$$\therefore \Pr(X = 0) = \frac{5}{9} \approx 0.556$$
 (2)

(ii) The probability that the coin will not be a ₹ 5 coin is given by:

$$\Pr(X \neq 3) = \frac{\sum_{i \neq 3} n(X = i)}{\sum_{i=0}^{3} n(X = i)} = \frac{170}{180}$$
 (3)

$$\therefore \Pr(X \neq 3) = \frac{17}{18} \approx 0.944 \tag{4}$$

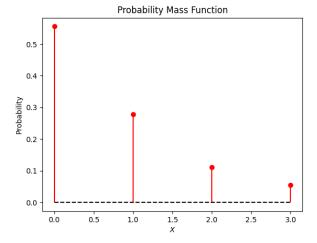


Fig. 1: Plot of the probability mass function