

Assignment 5

AI1110: Probability and Random Variables

Indian Institute of Technology Hyderabad

Ankit Saha
AI21BTECH11004

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CBSE Probability Grade 10

Exercise 15.1.10 A piggy bank contains hundred 50 p coins, fifty ₹ 1 coins, twenty ₹ 2 coins and ten ₹ 5 coins. If it is equally likely that one of the coins will fall out when the bank is turned upside down, what is the probability that the coin:

- (i) will be a 50 p coin?
- (ii) will not be a ₹ 5 coin?

Solution. Let a random variable $X \in \{0, 1, 2, 3\}$ denote the possible outcomes of obtaining a random coin from the piggy bank.

X	Outcome	Number
0	50 p	$n(X = 0) = 100$
1	₹ 1	$n(X = 1) = 50$
2	₹ 2	$n(X = 2) = 20$
3	₹ 5	$n(X = 3) = 10$

TABLE 1

- (i) The probability that the coin will be a 50 p coin is given by:

$$\Pr(X = 0) = \frac{n(X = 0)}{\sum_{i=0}^3 n(X = i)} = \frac{100}{180} \quad (1)$$

$$\therefore \Pr(X = 0) = \frac{5}{9} \approx 0.556 \quad (2)$$

- (ii) The probability that the coin will not be a ₹ 5 coin is given by:

$$\Pr(X \neq 3) = \frac{\sum_{i \neq 3} n(X = i)}{\sum_{i=0}^3 n(X = i)} = \frac{170}{180} \quad (3)$$

$$\therefore \Pr(X \neq 3) = \frac{17}{18} \approx 0.944 \quad (4)$$

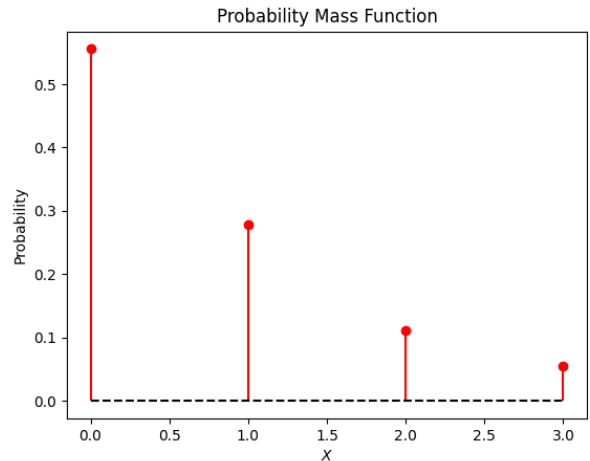


Fig. 1: Plot of the probability mass function