

# Normalization

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## CS 4750 Database Systems

[A. Silberschatz, H. F. Korth, S. Sudarshan, Database System Concepts, Ch.7]  
[Ricardo and Urban, Database Illuminated, Ch.6]  
[ <https://www.w3schools.in/dbms/database-normalization/> ]

# Recap: FD

Consider a student\_lecture relation

S_id	Address	Course	Teaching_assistant
1234	57 Hockanum Blvd	Database Systems	Minnie
2345	1400 E. Bellows	Database Systems	Humpty
3456	900 S. Detroit	Cloud Computing	Dumpty
1234	57 Hockanum Blvd	Web Programming Lang.	Mickey
5678	2131 Forest Lake Ln.	Software Analysis	Minnie

Assume that there is exactly one teaching assistant assigned to each student for every course

1. Determine all functional dependencies of the relation
2. Give an example of a super key and a candidate key

# Recap: FD

Consider a student\_lecture relation

S_id	Address	Course	Teaching_assistant
1234	57 Hockanum Blvd	Database Systems	Minnie
2345	1400 E. Bellows	Database Systems	Humpty
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1234	57 Hockanum Blvd	Web Programming Lang.	Mickey
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1. Determine all functional dependencies of the relation

$S_id \rightarrow Address$

$S_id, Course \rightarrow Teaching\_assistant$

**??**  $Address \rightarrow Course$

Possible (if no student lives in the same address), but probably unrealistic

Assume: there is exactly one teaching assistant assigned to each student for every course

# Recap: FD

Consider a student\_lecture relation

S_id	Address	Course	Teaching_assistant
1234	57 Hockanum Blvd	Database Systems	Minnie
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2. Give an example of a super key and a candidate key

The set of all the attributes is a trivial super key  
(S\_id, Course) is a candidate key

Assume: there is exactly one teaching assistant assigned to each student for every course

# Recap: Attribute Closure

Given a relation R (A, B, C, D, E, F, G) with the following FDs

FDs = { A → BC, E → CF, B → E, CD → EF, A → G }

Find the closure of A (A+)

A → B and A → C

(decompose A → BC)

A → E

(transitive A → B and B → E)

A → CF

(transitive A → E and E → CF)

A → G

(FD given)

Thus, A+ = { ABCEFG }

# General Design Guidelines

- Semantics of attributes should self-evident
- Avoid redundancy – between tuples, relations
- Avoid NULL values in tuples
- If certain tuples should not exist, don't allow them

Database design = process of organizing data into a database model by considering **data needs to be stored** and the **interrelationship of the data**

Database design is about  
**characterizing data** and the **organizing data**

How to describe properties  
we know or see in the data

How to organize data to promote  
ease of use and efficiency

# Normalization

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- Normalization = technique of organizing data in a database
- Two purposes:
  - Eliminating redundant data
    - Avoid storing the same data in multiple tables
  - Ensuring data dependencies make sense
    - Store data logically – only related data in a table, nothing else
- Need to refine schema

# Schema Refinement

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- Constraints, in particular **functional dependencies**, cause problems
- Must understand when and how constraints cause redundancy
- Refinement is needed when redundancy exists
- **Decomposition** – main refinement technique
  - Example: replace ABCD with [AB and BCD] or [ACD and ABD]
  - Judgment call:
    - Is there a reason to decompose a relation?
    - What problems (if any) does the decomposition cause?

# Decomposition

Suppose a relation  $R$  contains attribute  $A_1, \dots, A_n$ . A decomposition of  $R$  consists of replacing  $R$  by two or more relations such that

- Each new relation schema contains a **subset** of the attributes of  $R$  (and no attribute that do not appear in  $R$ )
- Every attribute of  $R$  **appears as an attribute** of at least one of the new relations

## Three potential problems:

Tradeoff: must consider these issues vs. redundancy

- Some queries become more **expensive**
- Given instances of the decomposed relations, we may **not be able to reconstruct the original relation**
- Checking some dependencies may require **joining the the decomposed relations**

# Properties of Decomposition

## Lossless join

- $\text{Employee} = R1 \bowtie R2$  (  $\bowtie$  “natural join” )
- No gain or loose columns / rows
- $R1 \cap R2 \neq \{ \}$
- $R1 \cap R2 \rightarrow R1$  or  $R1 \cap R2 \rightarrow R2$  ( $R1 \cap R2$  is a super key of  $R1$  or  $R2$ )

## Dependency preserving

- Every dependency is in the same relation (thus, when checking a dependency, no need to join tables)

## No redundancy

- For every nontrivial FD, a determinant must be a superkey (solved through the normal forms)

# Lossless-Join Decomposition

Employee

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10

$$\text{Employee} = R1 \bowtie R2$$

No gain or lose columns

R1

computingID	name	year	hours_worked
ht1y	Humpty	4	20
dt2y	Dumpty	3	20
md3y	Mickey	4	15
mn4e	Minnie	4	16
dh5h	Duhhuh	3	10

=

$$\underline{R1 \cap R2 \neq \{ \}}$$

Super key

$\bowtie$

year	hourly_rate
4	12
3	10

# Lossless-Join Decomposition

R1

computingID	name	year	hours_worked
ht1y	Humpty	4	20
dt2y	Dumpty	3	20
md3y	Mickey	4	15
mn4e	Minnie	4	16
dh5h	Duhhuh	3	10

R2

year	hourly_rate
4	12
3	10



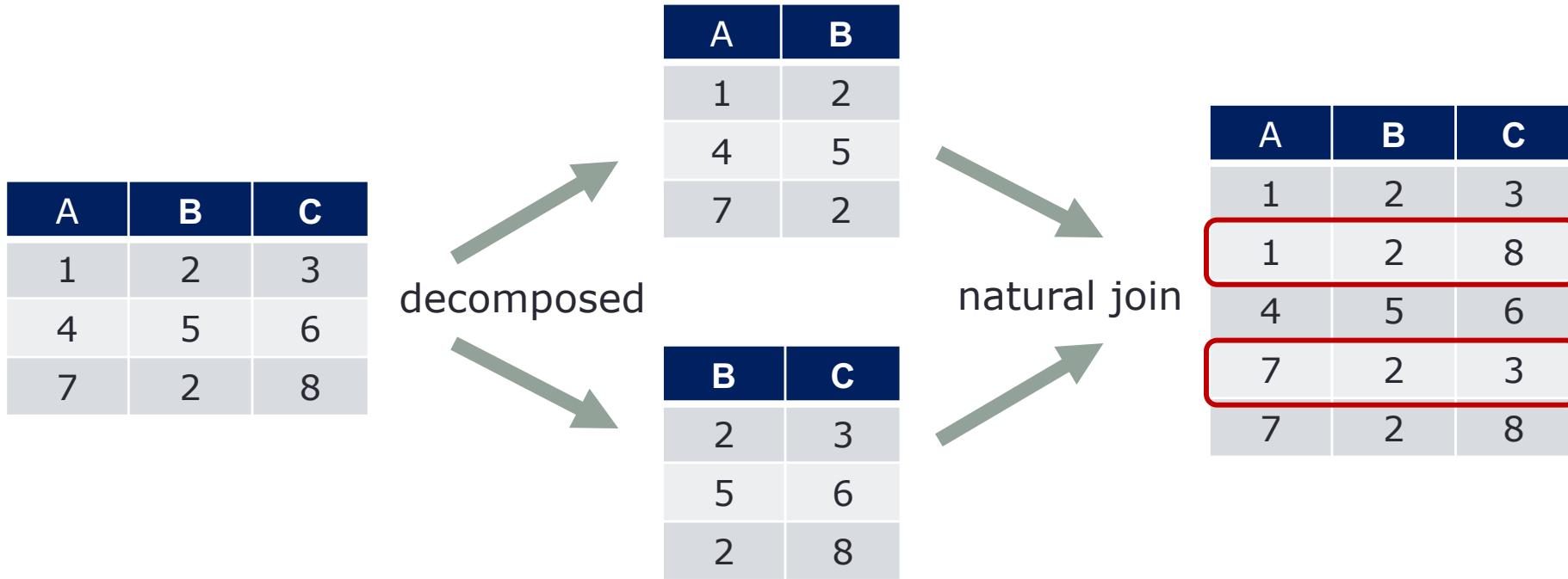
Reconstruct the original relation  
No gain or loose columns / rows

Employee

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
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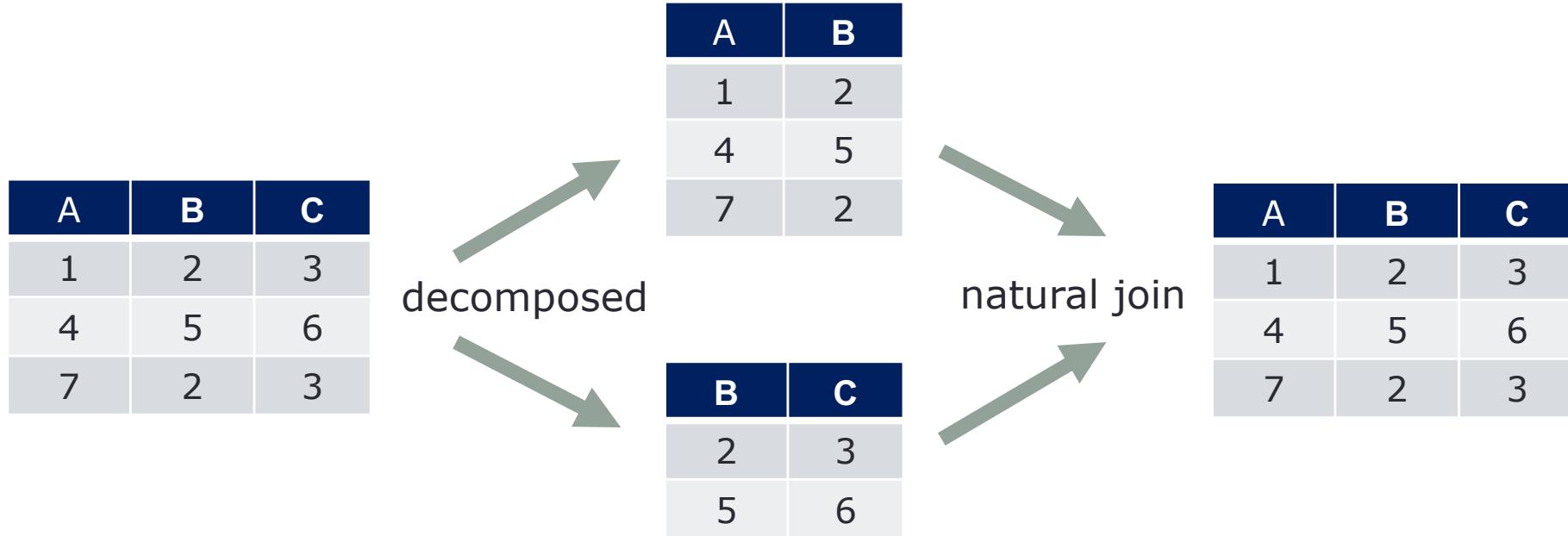
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# Let's Try (1) Lossless Join decomposition?



No

# Let's Try (2) Lossless Join decomposition?



Yes

$$(AB \cap BC) \rightarrow BC$$

# Normalization

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- **1NF**: each column is atomic, flat
- **2NF**: 1NF + no partial dependency -- *[outdated]*
- **3NF**: 2NF + lossless-join + dependency preserving -- *[our focus]*
- **BCNF**: 1NF + lossless join + redundancy free -- *[our focus]*
- **4NF**: no multi-valued dependency -- *[out of CS 4750 scope]*
- **5NF**: 4NF + cannot be further non loss decomposed -- *[out of CS 4750 scope – too complicated]*
- **6NF**: 5NF + every join dependency is trivial -- *[out of CS 4750 scope – somewhat unrealistic]*

# First Normal Form (1NF)

- Every attribute/column has a single (**atomic**) value
- Values stored in a column should be of the same domain
- The order in which data is stored does not matter

computingID	name	phone	department
ht1y	Humpty	111-111-1111	Computer Science, Math
dt2y	Dumpty	222-222-2222	Biology

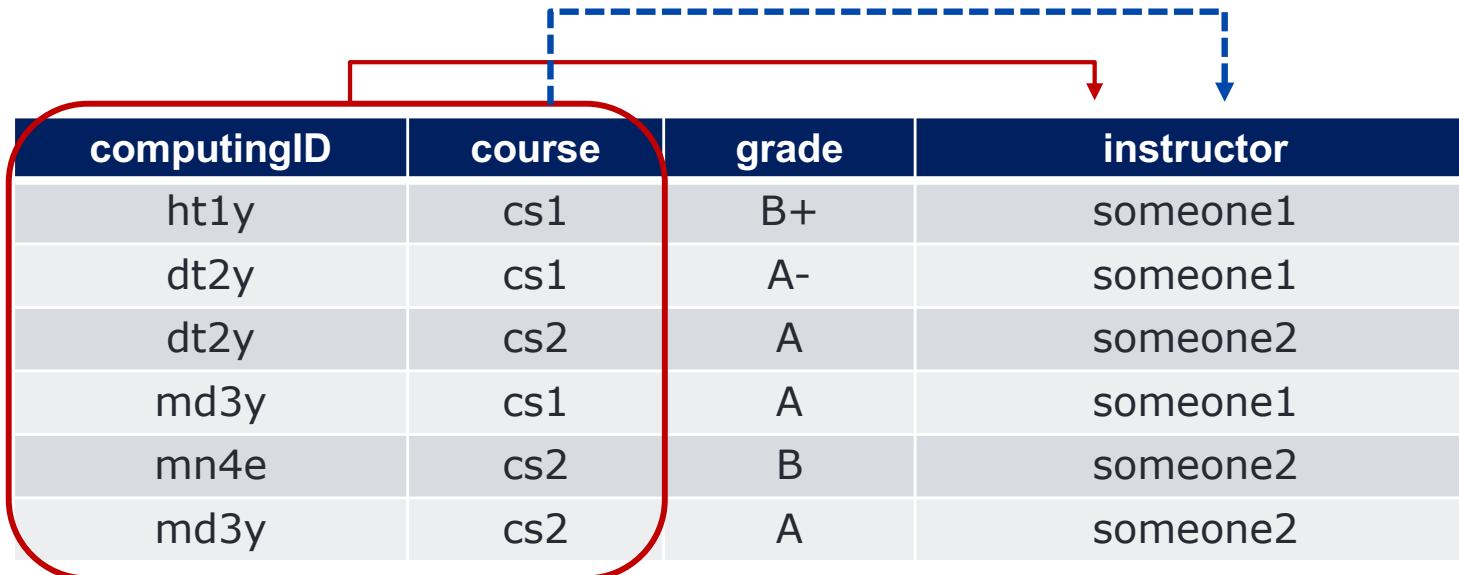
computingID	name	phone	department
ht1y	Humpty	111-111-1111	Computer Science
ht1y	Humpty	111-111-1111	Math
dt2y	Dumpty	222-222-2222	Biology
md3y	Mickey	333-333-3333	Computer Science
mn4e	Minnie	444-444-4444	Computer Science

Suppose we know that a student may be in multiple departments

# Second Normal Form (2NF)

- 1NF + no partial dependency (FDs)

Suppose we also know course → instructor



computingID	course	grade	instructor
ht1y	cs1	B+	someone1
dt2y	cs1	A-	someone1
dt2y	cs2	A	someone2
md3y	cs1	A	someone1
mn4e	cs2	B	someone2
md3y	cs2	A	someone2

Let's simplify the name: R (A, B, C, D), AB is a candidate key  
FDs { AB → C, AB → D, B → D }

Since B is part of a candidate key, D depends on a part of a key  
“Partial dependency”

Note: many-to-many relationship

# Second Normal Form (2NF)

To convert the table into 2NF, decompose the table to remove partial dependency

computingID	course	grade	instructor
ht1y	cs1	B+	someone1
dt2y	cs1	A-	someone1
dt2y	cs2	A	someone2
computingID	course	grade	instructor
ht1y	cs1	B+	
dt2y	cs1	A-	
dt2y	cs2	A	
md3y	cs1	A	
mn4e	cs2	B	
md3y	cs2	A	

Non-key attributes must depend upon the whole of the candidate key

# Third Normal Form (3NF)

- 2NF + lossless-join + dependency preserving
- For every non-trivial dependency, either LHS is a superkey or the RHS consists of prime attributes only

No transitive dependencies

$B \rightarrow D ?$

computingID	course	grade	textbook_id	title
ht1y	cs1	B+	book1	Intro to Python
dt2y	cs1	A-	book1	Intro to Python
dt2y	cs2	A	book2	Intro to Java
md3y	cs1	A	book1	Intro to Python
mn4e	cs2	B	book2	Intro to Java
md3y	cs2	A	book2	Intro to Java

Suppose we want to keep track of textbook\_id and title for the course

Let's simplify the name: R (A, B, C, D, E), AB is a candidate key  
FDs { AB  $\rightarrow$  C, AB  $\rightarrow$  D, D  $\rightarrow$  E }

Since AB  $\rightarrow$  D, D  $\rightarrow$  E, D and E are non keys -- "transitive dependency"

Problem with dependency ... Fix it!

# Third Normal Form (3NF)

To convert the table into 3NF, decompose the table to remove transitive dependency

computingID	course	grade	textbook_id	title
ht1y	cs1	B+	book1	Intro to Python
dt2y	cs1	A-	book1	Intro to Python
dt2y	cs2	A	book2	Intro to Java
computingID	course	grade	course	textbook_id
ht1y	cs1	B+	cs1	book1
dt2y	cs1	A-	cs2	book2
dt2y	cs2	A		
md3y	cs1	A		
mn4e	cs2	B		
md3y	cs2	A		

Ensure data integrity; no transitive dependency;  
dependency is in the same relation

Preserve all FDs but allow anomalies (may have redundancy)

# Boyce-Codd Normal Form (BCNF)

- 1NF + lossless-join + redundant free
- For every non-trivial dependency,  $X \rightarrow A$ ,  $X$  is a **superkey**.

computingID	course	instructor
ht1y	cs1	someone1
dt2y	cs1	someone1
dt2y	cs2	someone2
md3y	cs1	someone3
mn4e	cs2	someone2
md3y	cs2	someone2

All dependencies must be from full key

Suppose we know that  $\text{instructor} \rightarrow \text{course}$

Cannot have a non-key implies a key

Let's simplify the name: R (A, B, C), AB is a candidate key

FDs {  $AB \rightarrow C$ ,  $C \rightarrow B$  }

Since  $C \rightarrow B$ , non-key implies a (part of) key

Not satisfy BCNF -- Fix it!

# Boyce-Codd Normal Form (BCNF)

To convert the table into BCNF, decompose the table to remove non-keys that imply a key – to make all dependencies from a key

computingID	course	instructor
ht1y	cs1	someone1
dt2y	cs1	someone1
dt2y	cs2	someone2
computingID	instructor	inst
ht1y	someone1	som
dt2y	someone1	som
dt2y	someone2	som
md3y	someone3	som
mn4e	someone2	som
md3y	someone2	som

Given

FDs {  $AB \rightarrow C$ ,  $C \rightarrow B$  }

lost FD

instructor	course
someone1	cs1
someone2	cs2
someone3	cs1

Remove redundant data; ensure data integrity; may have dependency across relations (need to join to check dependency)

No transitive FDs, no non-key dependencies, but can lose FDs

# Recap: Normal Forms

**What is the main aspect of 1NF?**

Atomicity

**Which among 3NF and BCNF is dependency preserving?**

3NF

**Which among 3NF and BCNF is redundancy free?**

BCNF

**What is common between 3NF and BCNF?**

Lossless join

# Wrap-Up

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- Properties of Decomposition
  - Lossless join
  - Dependency preserving
  - No redundancy
- Overview of normal forms

## What's next?

- 3NF and decomposition
- BCNF and decomposition