

Language Models

Advanced Smoothing & Evaluation

By Dr. Sriparna Saha

[Ack These slides are taken from IIT Delhi LLM Course](#)

https://openai.com/index/search_gpt-prototype/

Search GPT announced!

OpenAI announces the launch of Search GPT, its AI-powered search engine

SearchGPT will respond to the questions with up-to-date information from the web while giving links to relevant sources.

SearchGPT ●

Q What are you looking for?

→

The service is powered by the GPT-4 family of models.

A new rival to Google and Perplexity?

Advanced Smoothing Algorithms

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Use the count of things we've **seen once**
to help estimate the count of things we've **never seen**

Notation

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Adapted from NLP Lectures by Daniel Jurafsky

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- Rohan 2
- Am 2
- like 1
- to 1
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$$N_1 = 3, N_2 = 2, N_3 = 1$$

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Good Turing Smoothing Intuition

- You are birdwatching in the Jim Corbett National Park and you have observed the following birds: 10 Flamingos, 3 Kingfishers, 2 Indian Rollers, 1 Woodpecker, 1 Peacock, 1 Crane = 18 birds
- How likely is it that the next bird you see is a woodpecker?

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- Assuming so, how likely it is that the new species is Woodpecker?
 - Must be less than $1/18$

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Good Turing Calculations

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- Unseen (Purple Heron or Painted Stork)
 - $C = 0$
 - $\text{MLE } p = 0/18 = 0$
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- P_{GT}^* (unseen) = $N_1/N = 3/18$

- Seen once
 - $C = 1$
 - MLE $p = 1/18$
 - $c^*(\text{Woodpecker}) = 2 * N_2/N_1$
 $= 2 * 1/3 = 2/3$
 - $P_{GT}^*(\text{Woodpecker}) = (2/3)/18 = 1/27$

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Good Turing Estimation

- Numbers from Church and Gale (1991)
- 22 million words of AP Newswire

Count c	Good Turing c^*
0	.0000270
1	0.446
2	1.26
3	2.24
4	3.24
5	4.22
6	5.19
7	6.21
8	7.24
9	8.25

Example from Speech and Language Processing book by Daniel Jurafsky and James H. Martin

Good Turing Estimation

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It looks like $c^* = (c - 0.75)$

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Absolute Discounting Interpolation

- Adjusts the probability estimates for n-grams by discounting each count by a fixed amount (usually a small constant) before computing probabilities

$$P_{\text{Absolute Discounting}}(w_i | w_{i-1}) = \frac{c(w_{i-1}, w_i) - d}{c(w_{i-1})} + \lambda(w_{i-1})P(w_i)$$

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Interpolation weight

unigram

- But considering the regular unigram probability has some limitations, as we will see in the upcoming slides.

Continuation Probability

- **Intuition: Shannon game**
 - My breakfast is incomplete without a cup of ... : coffee/ Angeles?
 - Say, in the corpus “Angeles” more prevalent than “coffee”
 - However, it is important to note that “Angeles” mostly comes after “Los”
- Instead of regular unigram probability, use **continuation probability**.

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 - Regular Unigram probability: $P(w)$: “How likely is w ?”
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- How to compute **continuation probability**?
 - Count how many different bigram types each word completes => Normalize by the total number of word bigram types

$$P_{\text{continuation}}(w) = \frac{|\{w_{i-1} : c(w_{i-1}, w) > 0\}|}{|\{(w_{j-1}, w_j) : c(w_{j-1}, w_j) > 0\}|}$$

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A common word (Angeles) appearing in only one context (Los) is likely to have a low continuation probability.

Kneser-Ney Smoothing

$$P_{KN}(w_i | w_{i-1}) = \frac{\max(c(w_{i-1}, w_i) - d, 0)}{c(w_{i-1})} + \lambda(w_{i-1})P_{\text{continuation}}(w_i)$$

where, λ is a normalizing constant (How to define this?)

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$$\lambda(w_{i-1}) = \frac{d}{c(w_{i-1})} | \{w : c(w_{i-1}, w) > 0\} |$$

Evaluation of Language Models

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- Does our language model prefer good sentences over bad ones?

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- Does our language model prefer good sentences over bad ones?
 - Assign higher probability to “real” or “frequently observed” sentences than “ungrammatical” or “rarely observed” sentences
- Terminologies:
 - We optimize the parameters of our model based on data from a **training set**.
 - We assess the model's performance on unseen **test data** that is disjoint from the training data.
 - An evaluation metric provides a measure of the performance of our model on the test set.

Extrinsic Evaluation

- Measure the effectiveness of a language model by **testing their performance on different downstream NLP tasks**, such as machine translation, text classification, speech recognition.

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- Measure the effectiveness of a language model by **testing their performance on different downstream NLP tasks**, such as machine translation, text classification, speech recognition.
- Let us consider two different language models: A and B
 - Select a suitable evaluation metric to assess the performance of the language models based on the chosen task.
 - Obtain the evaluation scores for A and B
 - Compare the evaluation scores for A and B

Intrinsic Evaluation: Perplexity

Intuition: The Shannon Game

- How well can we predict the next word?
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A better text model is characterized by its ability to assign a higher probability to the correct word in a given context.

Perplexity

The best language model is one that best predicts an unseen test set.

Perplexity is the inverse probability of the test data, normalized by the number of words.

- Given a sentence W consisting of n words, the perplexity is calculated as follows:

$$PP(W) = P(w_1 w_2 \dots w_n)^{-1/n}$$

Perplexity

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Applying Markov Assumption ($n = 2$), i.e. **for bigram LM**:

Minimizing perplexity is the same as maximizing probability.

$$PP(W) = \left(\prod \frac{1}{P(w_i | w_{i-1})} \right)^{1/n}$$

Perplexity and Entropy

Problems of Statistical Language Models

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 - Predicting the next word using a fixed window of previous words.
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- Large vocabulary leads to high memory requirements.
- High computational cost for large n-grams.
- Lack of generalization to unseen word combinations.

The Need for Richer Representations

Requirements:

- **Contextual Understanding:** Need for models that understand context beyond fixed windows.
- **Semantic Similarity:** Ability to capture relationships between words (e.g., synonyms).
- **Scalability:** Models that can scale to large datasets and handle vast vocabularies efficiently.

Moving to Word Embeddings & Neural LM

In the successive lectures, we will see how representing words (actually, tokens) as vectors and transition to neural LMs solve many of those problems.

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In the successive lectures, we will see how **representing words (actually, tokens) as vectors** and **transition to neural LMs** solve many of those problems.

- Move from discrete to continuous representations.
- Capture richer semantic information.
- Enable generalization to unseen data.
- Scale to large datasets.

Timeline in Language Modelling

