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NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA
(An Autonomous Institute)

Affiliated to Dr. A.P. J. Abdul Kalam Technical University, Uttar Pradesh, Lucknow

Course: B.Tech. Branch: CSBS

Semester IV Sessional Examination - II Year- (2021- 2022)

Subject Name: Operations Research

Time: 1.15 Hours

[SET- B]

Max. Marks:30

General Instructions:

- This Question paper consists of 3 pages & 5 questions. It comprises of three Sections, A, B, and C
- **Section A** - Question No- 1 is objective type questions carrying 1 mark each, Question No- 2 is very short answer type carrying 2 mark each. You are expected to answer them as directed.
- **Section B** - Question No-3 is Short answer type questions carrying 5 marks each. Attempt any two out of three questions given.
- **Section C** - Question No. 4 & 5 are Long answer type (within unit choice) questions carrying 6 marks each. Attempt any one part a or b.

		<u>SECTION – A</u>	[08Marks]	
1.	All questions are compulsory		(4×1=4)	
	a.	The dual simplex method is applicable to the LPP's that start with i. An infeasible but optimum solution ii. An infeasible solution iii. A feasible but optimum solution iv. A feasible solution	(1)	CO2
	b.	If dual has unbounded solution, primal has i. An infeasible solution ii. An unbounded solution iii. A feasible solution iv. None of the above.	(1)	CO2
	c.	The purpose of the transportation approach for locational analysis is to minimize i. total costs ii. total shipping costs	(1)	CO3

	iii. total variable costs iv. total fixed costs																																																			
d.	The solution to a transportation problem with 'm' rows(supplies) and 'n' columns(destination) is feasible if number of positive allocations are i. m+n ii. mn iii. m+n-1 iv. m+n+1	(1)	CO3																																																	
2.	All questions are compulsory	(2×2=4)																																																		
a.	State Fundamental Duality Theorem.	(2)	CO2																																																	
b.	Write the mathematical form of transportation Problem.	(2)	CO3																																																	
SECTION – B		[10Marks]																																																		
3.	Answer any <u>two</u> of the following-	(2×5=10)																																																		
a.	Define convex set. Prove that the set $S = \{(x_1, x_2) x_1^2 + x_2^2 \leq 4\}$ is a convex set.	(5)	CO2																																																	
b.	Solve the assignment problem represented by the following matrix <table><tr><td></td><td>a</td><td>b</td><td>c</td><td>d</td><td>e</td><td>f</td></tr><tr><td>A</td><td>9</td><td>22</td><td>58</td><td>11</td><td>19</td><td>27</td></tr><tr><td>B</td><td>43</td><td>78</td><td>72</td><td>50</td><td>63</td><td>48</td></tr><tr><td>C</td><td>41</td><td>28</td><td>91</td><td>37</td><td>45</td><td>33</td></tr><tr><td>D</td><td>74</td><td>42</td><td>27</td><td>49</td><td>39</td><td>32</td></tr><tr><td>E</td><td>36</td><td>11</td><td>57</td><td>22</td><td>25</td><td>18</td></tr><tr><td>F</td><td>3</td><td>56</td><td>53</td><td>31</td><td>17</td><td>28</td></tr></table>		a	b	c	d	e	f	A	9	22	58	11	19	27	B	43	78	72	50	63	48	C	41	28	91	37	45	33	D	74	42	27	49	39	32	E	36	11	57	22	25	18	F	3	56	53	31	17	28	(5)	CO3
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D	74	42	27	49	39	32																																														
E	36	11	57	22	25	18																																														
F	3	56	53	31	17	28																																														
c.	Determine an initial basic feasible solution to the following transportation problem using Vogel's method. <table><tr><td></td><td>D₁</td><td>D₂</td><td>D₃</td><td>D₄</td><td>Available</td></tr><tr><td>O₁</td><td>1</td><td>2</td><td>1</td><td>4</td><td>30</td></tr><tr><td>O₂</td><td>1</td><td>3</td><td>2</td><td>1</td><td>50</td></tr><tr><td>O₃</td><td>4</td><td>2</td><td>5</td><td>9</td><td>20</td></tr><tr><td>Required</td><td>20</td><td>40</td><td>30</td><td>10</td><td>100</td></tr></table>		D ₁	D ₂	D ₃	D ₄	Available	O ₁	1	2	1	4	30	O ₂	1	3	2	1	50	O ₃	4	2	5	9	20	Required	20	40	30	10	100	(5)	CO3																			
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SECTION – C		[12Marks]																																																		
4	Answer any <u>one</u> of the following-	(1×6=6)																																																		

	a.	Use dual simplex method to solve the problem: $Min. Z = 6x_1 + x_2$ subject to constraints $2x_1 + x_2 \geq 3,$ $x_1 - x_2 \geq 0,$ $x_1, x_2 \geq 0$	(6)	CO2																																			
	b.	Use Big-M method to Maximize $z = x_1 + 5x_2$ Subject to $3x_1 + 4x_2 \leq 6$ $x_1 + 3x_2 \geq 2$ $x_1, x_2 \geq 0$	(6)	CO2																																			
5.	Answer any <u>one</u> of the following-		(1×6=6)																																				
	a.	Solve the following transportation problem (cell entries represent unit costs): <div style="text-align: right; margin-right: 20px;">Available</div> <table border="1" style="margin-left: auto; margin-right: auto;"><tr><td>5</td><td>3</td><td>7</td><td>3</td><td>8</td><td>5</td><td>3</td></tr><tr><td>5</td><td>6</td><td>12</td><td>5</td><td>7</td><td>11</td><td>4</td></tr><tr><td>2</td><td>1</td><td>3</td><td>4</td><td>8</td><td>2</td><td>2</td></tr><tr><td>9</td><td>6</td><td>10</td><td>5</td><td>10</td><td>9</td><td>8</td></tr></table> <div style="text-align: right; margin-right: 20px;">Required</div> <table style="margin-left: auto; margin-right: auto;"><tr><td>3</td><td>3</td><td>6</td><td>2</td><td>1</td><td>2</td><td>17</td></tr></table>	5	3	7	3	8	5	3	5	6	12	5	7	11	4	2	1	3	4	8	2	2	9	6	10	5	10	9	8	3	3	6	2	1	2	17	(6)	CO3
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2	1	3	4	8	2	2																																	
9	6	10	5	10	9	8																																	
3	3	6	2	1	2	17																																	
	b.	Solve the following unbalanced transportation problem (symbols have their usual meaning): <table style="margin-left: auto; margin-right: auto;"><tr><td></td><td>D_1</td><td>D_2</td><td>D_3</td><td>a_i</td></tr><tr><td>O_1</td><td>4</td><td>3</td><td>2</td><td>10</td></tr><tr><td>O_2</td><td>2</td><td>5</td><td>0</td><td>13</td></tr><tr><td>O_3</td><td>3</td><td>8</td><td>6</td><td>12</td></tr><tr><td>b_j</td><td>8</td><td>5</td><td>4</td><td></td></tr></table>		D_1	D_2	D_3	a_i	O_1	4	3	2	10	O_2	2	5	0	13	O_3	3	8	6	12	b_j	8	5	4		(6)	CO3										
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