

DATA STRUCTURE

Data structure is a particular way of organizing data in a computer so that we can use effectively.

Eg:-

We can store a list of items having the same data type using the array data structure.

⇒ Types of data structure :-

① Linear Data Structure

② Non-Linear Data Structure

(i) Linear Data Structure

- ① Array
- ② Linklist
- ③ Stack
- ④ Queue
- ⑤ Tree

(ii) Non-Linear D.S

- ⑥ Graphs

⇒ Difference b/w linear or non-linear D.S -

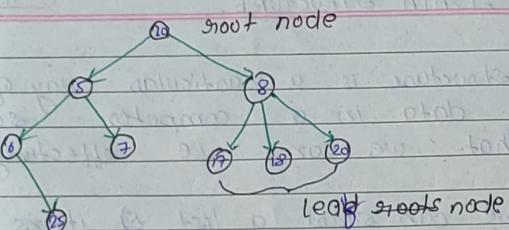
→ Linear D.S :- A linear data structure can grow in a sequential organized form.

Examples of linear data structure :-
linked list, stack, queue, array, etc.



link list

→ Nonlinear D.S :- In a nonlinear data structure there is no sequential organized way of group.



lead node :- A node without any child.

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linear ds

Non linear ds

- (i) Data structure are arranged in linear order where each and every element are attached to its previous and next adjacent.
- (ii) Single level is involved.
- (iii) Memory is not utilized in an effective way.
- (iv) Examples are array, stack, linked list and queue.
- (v) Its implementation is easy.
- (vi) Applications of linear ds

Data structure are mainly used in application of software development.

Data structure are AI (Artificial Intelligence) and image processing.

1) Array :- Array is linear data structure that is a collection of similar data.

Types of Array :-

- (i) 1-D Array :- int a[10];
'a' is an integer array of size 10 so it can store 10 integers from a[0] to a[9].
- (ii) 2-D Array :- int a[3][3];
'a' is an integer 2-D array (matrix) of 3 rows and 3 cols so it can store $3 \times 3 = 9$ elements from a[0][0] to a[2][2].
- ⇒ Cmp programme inside Array
- (1) WAP in C to store 'n' integers in 1-D array and perform:-
- (a) Search
- (b) sort
- (c) delete an element
- (d) display array in reverse order
- (e) sum and avg of array element
- (f) find max and 2nd max array element
- (g) ...

- 2) Add and Multiply two 2D matrix (2-D array)
- 3) Transpose of a matrix
- 4) Right and left Diagonal of a matrix?
- 5) Row and column major.
- 6) Dynamic Array
- 7) primitive and non-primitive Data structures
- 8) static / dynamic Data structures
- 9) sparse matrix

Sparse Matrix

A matrix can be defined as two-dimensional array having 'm' columns and 'n' rows representing m*n matrix.

Sparse matrices are those matrices that have the majority of their elements equal to zero. In other words, the sparse matrix can be defined as the matrix that has a greater number of zero elements than the non-zero elements.

- **storage :-** As we know a sparse matrix that contains lesser non-zero elements than zero so less memory can be used to store elements. It evaluate only the non-zero elements.
- ② computing time will be reduced.
- **Computing time :-** In the case of searching n sparse matrix, we need to traverse only the non-zero elements rather than traversing all the sparse matrix elements. It saves computing time by logically computing time by logically designing a data structure traversing non-zero elements.

⇒ Sparse Matrix Representation:-

- **Array Representation.**
- **linked List Representation.**

⇒ Array Representation:-

0	1	2
0	0	13
1	2	0
2	3	0

Row	col	value
0	2	13
1	0	2
2	0	3

Q) w-a-p in C to represent sparse matrices using Array

main()

{

int i, j, m, c, z=0, nz=0, m=0, n=0;

printf("Enter rows and columns");
scanf("%d%d", &m, &n);

```
int a[m][n];
for(i=0; i<m; i++)
{
    for(j=0; j<n; j++)
        scanf("%d", &a[i][j]);
}
```

3

printf("In Matrix insertion");

```
for(i=0; i<m; i++)
{
    for(j=0; j<n; j++)
}
```

if(a[i][j]==0)

z++;

else

nz++;

printf("%d", a[i][j]);

3

printf("\n");

int b[nz][3];
if(z>nz)

{

for(i=0; i<z; i++)

{

for(j=0; j<c; j++)

{

if(a[i][j] != 0)

{

b[m][n] = i;

printf("%d", b[m][n]);

b[m][n+1] = j;

printf("%d", b[m][n]);

b[m][n+1] = a[i][j];

printf("%d", b[m][n]);

printf("\n");

m++;

n=0;

}

3

3

3

3

else

printf("In Sparse values are not more than non zero values so sparse

Matrix not possible");

3

3

3

** Stack :- It is linear data structure that works on LIFO manner.

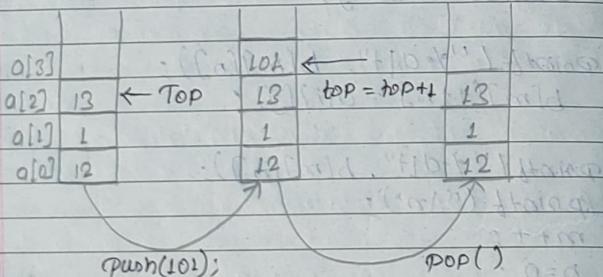
LIFO :- Last In First Out.

→ Operation on stack :-

a) push :- Insert a new element from the end.

b) pop :- delete from the end.

c) peek :- search or traversal.



Note:- In stack insertion and deletion both from top.

→ we can implement stack by two ways:-

a) Array b) link list.

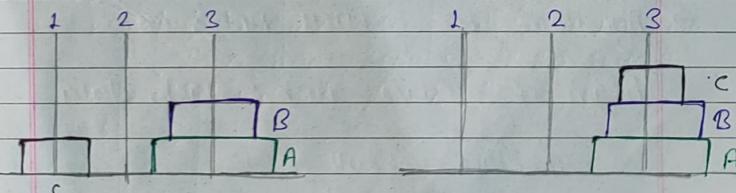
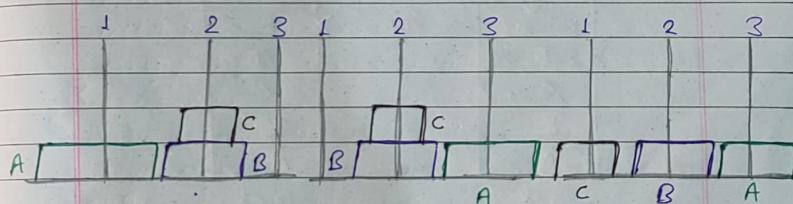
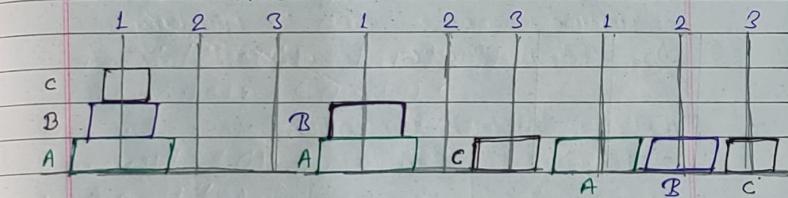
→ stack Application:-

○ ○ ○ a) Tower of Hanoi

POCO X3 BY HUAWEI Poco X3 and Poco X3 Pro conversion.

⇒ Tower of Hanoi :- Tower of Hanoi is a mathematical puzzle where we have three rods and n disks. The objective of the puzzle is to move the entire stack to another rod, obeying the following simple rules:

- Only one disk can be moved at a time.
- Each move consists of taking the upper disk from one of the stacks and placing it on top of another stack.
- No disk may be placed on top of a smaller disk.



so many students
and also some visitors
and students from other schools
and some of them
are very good
and some are not so good
but all of them
are very friendly
and helpful
and we have a lot of fun
and we play for hours
and we have a lot of fun
and we play for hours
and we have a lot of fun
and we play for hours

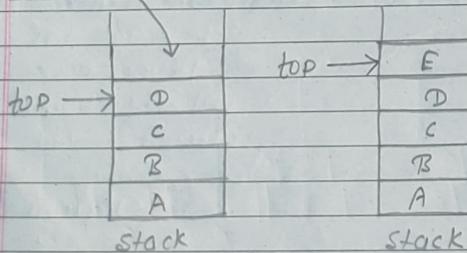
⇒ push operation:

Add the element from the top in a stack is known as push operation.

⇒ push operation involves a series of steps:-

- 1) checks if the stack is full.
- 2) if the stack is full, produce an error and exit.
- 3) If the stack is not full, increments top to point empty space.
- 4) Adds data element to the stack location, where top is pointing.
- 5) Return success.

Push operation



→ Algorithm for PUSH Operation:-

begin procedure push : stack, data

```

if stack is full
    return null
endif

```

top ← top + 1
stack [top] ← data

end-procedure.

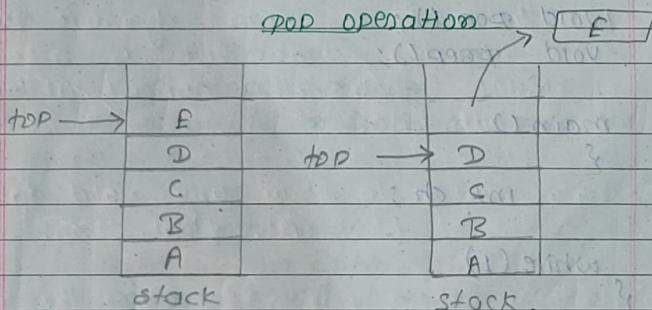
⇒ POP Operation

Remove the element from the top in a stack is known as POP operation.

→ A POP operation may involves the following steps:-

- 1) check if the stack is empty
- 2) if the stack is empty, produce an error and exit.
- 3) if the stack is not empty accesses the data element at which top is pointing.
- 4) Decreaser the value of top by 1.
- 5) Return success.

POP operation



→ Algorithm for POP operation:-

begin procedure POP : stack

if stack is empty
return null

endif

data ← stack[top]

top ← top - 1

return data

end procedure

8) write in C to implement stack

```
#define max 50
int stack[max];
int top = -1;
void push();
void pop();
void peek();
```

main()

{

int ch;

while(1)

printf("In Push:1 In Pop:2 In Display:3
In Exit:4");

scanf("%d", &ch);

switch(ch)

{

case 1:

push();

break;

case 2:

pop();

break;

case 3:

peek();

break;

case 4:

exit(0);

break;

void push()

{

int data;

if (top == max-1)

printf("In Stack is overflow");

else

{

top = top + 1;

printf("In Enter data");

scanf("%d", &data);

stack[top] = data;

3

void pop()

{

if (top == -1)

printf("In stack is under flow");

else

{

printf("In stack pop data = %d",
stack[top]);

top = top - 1;

3

void peek()

{

int i;

printf("In stack Elements \n");

for (i = top; i >= 0; i--)

printf("%d\n", stack[i]);

3

** Link List :- It is linear dynamic data structure, link list is a collection of nodes, each node consist at least two parts.

a) Data part :- To store any valid data like int, float, char.

b) Address part :- pointer to store the address of next node So the last node address part filled with NULL.

→ Types of link list -

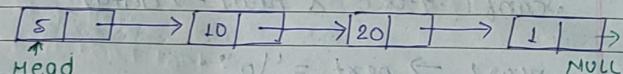
a) Single link list

b) circular link list

c) double link list

d) double circular link list.

A) Single link list :-



B) WAP in C to create and display single link list :-

struct node

{ int data;

struct node *next; }

typedef struct node s;

main()

{

s *start, *new, *temp;

int n, i;

printf("In Enter no. of nodes u want to create");

scanf("%d", &n);

start = (s *) malloc(sizeof(s));

printf("In Enter data");

scanf("%d", &start->data);

start → next = '10';
 t = start;
 for(i=1; i<n; i++)
 {
 new1 = (s*) malloc(sizeof(s));
 printf("Enter data : ");
 }

scanf("%d", &new1→data);

new1 → next = '10';

t → next = new1;

t = new1;

printf("In link list elements : In ");
 for(t=start; t; t=t→next)
 printf("%d", t→data);

Q) WAP in C to insert element in single link list?

struct node * start, * new1;

int data;

struct node * insert;

3:

typedef struct node s;

*start, *new1, *t; bok

Void insert()

void display()
main()

int ch;
 while(1)
 {
 printf("In Insert : 1 In Display : 2 In
 Exit : 3 In ");
 scanf("%d", &ch);
 }

switch(ch)

case 1: /* single into dual */
 insert(); t = start; t→next = t;
 break;
 case 2: /* dup. node */
 display();
 exit(0); // wrong
 break;
 case 3: /* exit() */
 exit(1919); // meaning will not
 change it still exit(), no. doesn't
 matter.

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display() function
 अब यहि t का next का access करते हैं तो use
 $t \rightarrow \text{next} = '10'$ in condition, bcoz if you use $t! = 0$
 else then t का value update हो जाएगा 0 से
 अपने बीच $t = 0$ से भी t का $\text{t} \rightarrow \text{next}$
 new1 = (s*) malloc(sizeof(s)); possible होता है
 printf ("\\n Enter data: ");
 scanf ("%d", &new1 -> data);
 new1 -> next = '10';
 $t \rightarrow \text{next} = \text{new1};$ अब t का last जगह 0
 $t = \text{new1};$ नयी डिक्टी + off value

3 void display()
 {
 printf ("In link list elements : %n");
 for (t = start; t != next; t = t->next)
 printf ("%d : %u ->", t->data, t->next);
 printf ("%d : %u", t->data, t->next);
 }

~~Temp due:-~~

- 1) sort the link list element using selection sort?
 - 2) search an element inside link list using binary search?
 - 3) split the link list into mid point and create two separate link list?
 - 4) display the prime no. inside the link list?

→ Insert, Display, Primes, sort, search.

struct node

25

```
int data ;
```

struct node *next;

3; *mit Ciao.*

```
typedef struct node
```

start, new1, +

void insert();

void display();

void sort();

void search();

void Dims();

main()

3. $\frac{1}{2} \times 10^{-10} \text{ m}^2$

int ch;

while (1) {
 S : (idle, 1000);

point ("In Tnseat".

Exit: ? In

In search : b

scanf ("%d", &ch);

switch(ch)

15 $\cdot ((2) \cdot (3) \cdot 8 \cdot (2)) \cdot 0$

case 1: about

: (atob) insert();

break;

case 2:

```
display();  
break;
```

case 3:
exit(0);

case 9:
prime();
break;

case 8:
search(); sort();
break; char temp[10];

case 6:
search(); cout << "found";
break;

3
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void insert()
if (start == '10')

start = (S*) malloc (sizeof (S));
printf ("In Enter data");
scanf ("%d", &start->data);
if (start->next == '10'; start->next = '10'; start);
t = start; newst = start->next;

3
else
new1 = (S*) malloc (sizeof (S));

printf ("In Enter data");
scanf ("%d", &new1->data);
new1->next = '10';
t->next = new1;
t = new1;

Void display()

printf ("In Link List Elements: ");

for (t = start; t->next != '10'; t = t->next)

printf ("%d", t->data), t->next);
printf ("%d", t->data), t->next);

3

void prime()
{

int l, f = 0; printf ("In Link List Only with prime
data: ");

for (t = start; t; t = t->next)

for (i = 1; i <= t->data; i++)

if (t->data % i == 0) f++;

if (f == 2)
printf ("%d", t->data), t->next);

3
3
if (i <= start->i)

("break loop"); f = 0; start = t->next;

3
3
("break loop"); f = 0; start = t->next;

f++;
if (f == 2) break;

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```

void const()
{
    int i, j;
    int b;
    float start; element = 10; l = i + n;
    for (j = l - 1; j > start; j = j - n)
    {
        if ((data) > j->data)
        {
            t = l->data;
            l->data = j->data;
            j->data = t;
        }
    }
}

void Search()
{
    int Key, l = 0;
    printf("Enter data for search");
    scanf("%d", &Key);
    for (l = start; l->next != 10; l = l->next)
    {
        if (l->data == key)
        {
            printf("data found");
            f++;
            break;
        }
    }
}

```

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Q

```

if (l == 0) - search = false;
printf("data not found");

```

Ans Ques

D) Represent a polynomial eqn using Link List.

eqn: $8x^8 + 12x^2 + 1x + 12$

$[8][3][12][2] \rightarrow [4][1] \rightarrow [12][0]$

struct Node

int C, P;

struct Node *next;

typedef struct Node *ptr;

start, known, xt;

main()

```

ptr *start * known * xt;
start = (8*) malloc(sizeof(8));
printf("Enter co-efficient & powers");
scanf("%d%d", &start->c, &start->p);
start->next = 10;
t = start;
for (int i = 1; (i < 8); i++)
{
    new1 = (8*) malloc(sizeof(8));
    printf("Enter co-eff & po");
    scanf("%d%d", &new1->c, &new1->p);
    new1->next = 10;
    t->next = new1;
    t = new1;
}

```

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Ques:

```

newl → next = '10';
t → next = newl;
t = newl;
for(t = start; t; t = t → next)
    printf("%d : %d", t → data);

```

Sol:

create a link list and split the link list into mid point and create two separate link list.

Struct Node

```

int data;
struct Node *next;

```

3;

```

typedef struct Node S;
S *start, *newl, *t, *start2, *start3,
    *t1, *t2;
main()
{
    int n, i;
    printf("In Enter no. of nodes");
    scanf("%d", &n);
    start1 = (S*) malloc (sizeof(S));
    printf("In Enter data");
    scanf("%d", &start1 → data);
    start1 → next = '10';
    t = start1;

```

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Ques:

```

for(i = 1; i < n; i++)
{
    newl = (S*) malloc (sizeof(S));
    printf("In Enter data");
    scanf("%d", &newl → data);
    newl → next = '10';
    t → next = newl;
    t = newl;
}

```

3;

```

int count = 1;
for(t = start + 1; t; t = t → next)
    printf("%d", t → data);
for(t = start + 1; t; t = t → next)
{
    if(count == 1)
        start2 = (S*) malloc (sizeof(S));
    start2 → data = t → data;
    start2 → next = '10';
    t1 = start2;
    start2 = start2 → next;
    else
        newl = (S*) malloc (sizeof(S));
    newl → data = t → data;
    newl → next = '10';
    t1 → next = newl;
    t1 = newl;
}

```

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```

if(count >= n/2)
    break;
    count++;
}
int count1 = 1;
for(t1 = t → next; t1; t1 = t1 → next)
{
    if(count1 == 1)
        start3 = (s*) malloc(sizeof(s));
    start3 → data = t1 → data;
    start3 → next = '10';
    t2 = start3;
    else
        {
            new1 = (s*) malloc(sizeof(s));
            new1 → data = t1 → data;
            new1 → next = '10';
            t2 → next = new1;
            t2 = new1;
        }
    count1++;
}
printf("\n");
for(t = start3; t; t = t → next)
    printf("%d", t → data);
    printf("\n\n");
for(t = start3; t; t = t → next)
    printf("%d", t → data);
    printf("\n\n");

```

POCO X3, BY PANKIT

Raw Major and column major order

Q) Addition of two polynomial eqn. using $\sin(x)$?

2-D array compiler can flow view major and column major to assign address.

Note:- Array always created in a single dimension in memory because memory is linear and here single integer array.

Raw and column major order- In computing row and column major orders are method for storing multidimensional arrays in linear storage such as random access memory.

⇒ Raw Major of 2-D Array :-

array :-
 $\text{int arr}[3][4]$

	0	1	2	3
0	100	102	104	106
1	108	110	112	114
2	116	118	120	122

⇒ Raw Major :-

000	001	002	003	010	011	012	013	020	021	022	023
100	102	104	106	108	110	112	114	116	118	120	122

$$\text{Address } \text{int}(a[i][j]) = l_0 + [i \times n + j] \times w$$

Q) When index starts from 0?

$$\text{Address of } \text{int}(a[i][j]) = l_0 + [(i-1) \times n + (j-1)] \times w$$

When index starts from 1?

where, l_0 is base address

i is index of row

j is index of column

n = no. of column

w = size of data type.

Q) Find the raw major of 2-d array
 $\text{int arr}[2][2]$

$$\text{but formula} = l_0 + [i \times n + j] \times w$$

$$= 100 + (2 \times 2 + 1) \times 2$$

$$= 100 + (8 + 1) \times 2$$

$$= 100 + 18$$

$$= 118$$

⇒ Column major :-

$$\text{add } \text{int}(a[i][j]) = l_0 + (j \times m + i) \times w$$

for index starts from 0.

$$\text{add } \text{int}(a[i][j]) = l_0 + (j-1) \times m + (i-1) \times w$$

for index starts from 1.

where, m = no. of rows

l_0 = base address

i = row index

j = column index

w = size of data type.

8) find the column major of $\text{add}(a[1][2])$
where index starts from 0:

$$\begin{aligned} &= s_0 + (j \times m + i) \times w \\ &= 100 + (2 \times 8 + 1) \times 2 \\ &= 100 + (7 \times 2) \\ &= 114 \end{aligned}$$

⇒ Finding the row major of single dimensional array:

int a[5].



add: 10 12 14 16 18

$\text{add}(a[i]) = \text{base add} + i \times \text{size of data type}$

= $s_0 + i \times w$ (for array index starts from 0)

= $s_0 + (i-1) \times w$ (for array index starts from 1)

where, $s_0 = \text{base add}$

$i = \text{array index whose address we want to find.}$

$w = \text{size of data type.}$

$\text{add}(a[3]) = 10 + i \times w$ consider index starts from 0.

$$= 16$$

* Sparse Matrix 'Imp' Using linked list Ax

23

$$\begin{aligned} \text{add}(a[4]) &= s_0 + (i-1) \times w \quad \text{consider array index starts from 1.} \\ &= 10 + (4-1) \times 2 \\ &= 16 \end{aligned}$$

8) Implement sparse matrix using linked list?

main()

{

int a[3][3] = {{0, 0, 0}, {0, 1, 0}, {0, 0, 3}};
int i, j, c=0, C=0, x=0;

for (i=0; i<3; i++)

{
for (j=0; j<3; j++)

if (a[i][j] != 0)
c++;

else

C++;

3

if (C > c)

struct node

{

int r, c, v;

struct node *next;

};

typedef struct node S;

S *start, *new1, *t;

for ($t = \text{start}$; $t \rightarrow \text{next}_t \neq \text{'10'}$; $t = t \rightarrow \text{next}$)

printf ("%d %d %d %d", $t \rightarrow r$, $t \rightarrow c$, $t \rightarrow v$);

printf ("%d %d %d %d", $t \rightarrow r$, $t \rightarrow c$, $t \rightarrow v$);

else

{

printf ("since non-zero values are more than zero values so sparse matrix is not possible");

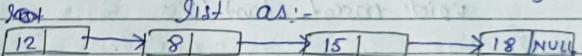
}

* Insert a new node in a existing link list:-

1) Insert node at start

⇒ Algo:-

consider we have an existing link



Step1 :-

Create a new node:-

$\text{new1} = (\text{s}*) \text{malloc}(\text{sizeof}(\text{s}))$;

printf ("enter data:");

scanf ("%d", &new1->data);

Step2 :- Make new Node as start node:-

$\text{new1} \rightarrow \text{next} = \text{start};$

for ($i = 0$; $i < 3$; $i++$)
 {
 for ($j = 0$; $j < 3$; $j++$)
 {
 if ($\text{a}[i][j] \neq 0$)
 {
 $x++$;
 if ($x == 1$)
 {
 $\text{start} = (\text{s}*) \text{malloc}(\text{sizeof}(\text{s}))$;
 $\text{start} \rightarrow r = i$;
 $\text{start} \rightarrow c = j$;
 $\text{start} \rightarrow v = \text{a}[i][j]$;
 $\text{start} \rightarrow \text{next} = \text{'10'}$;
 $t = \text{start}$;
 }
 else
 {
 $\text{new1} = (\text{s}*) \text{malloc}(\text{sizeof}(\text{s}))$;
 $\text{new1} \rightarrow r = i$;
 $\text{new1} \rightarrow c = j$;
 $\text{new1} \rightarrow v = \text{a}[i][j]$;
 $\text{new1} \rightarrow \text{next} = \text{'10'}$;
 $t \rightarrow \text{next} = \text{new1}$;
 $t = \text{new1}$;
 }
 }
 }
 }
 }
 }
 printf ("In sparse matrix : In ");

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Step 3:- Make the new node as start:-
 $\text{start} = \text{new1};$

Now the link list is:-



[2]
start

where,

struct node {

int data;

struct node *next;

3;
typedef struct node S;
S *start, *new1;

function:-

void insert_start()

{
new1 = (S*) malloc (sizeof (S));
printf ("Enter data");
scanf ("%d", &new1->data);
new1->next = '0';
new1->next = start;
start = new1;
}

3

Step 3:- Insert node at end:-

→ Algo:-

consider we have an existing link

list as:-



start

Step 1:-

Create a new node:-

$\text{new1} = (\text{S}*) \text{malloc}(\text{sizeof}(\text{S}))$;

$\text{printf} ("Enter data")$;

$\text{scanf} ("%d", \&\text{new1} \rightarrow \text{data})$;

$\text{new1} \rightarrow \text{next} = '0'$;

Step 2:- Make new node as start node:-

$\text{new1} \rightarrow \text{next} = \text{start}$;

Step 3:- Make the new node as start:-

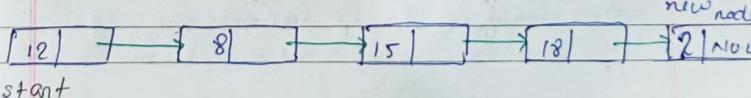
Step 2:- Move a pointer and terminate at last node so it hold the address of last node:-

for (t = start; t->next != '0'; t = t->next)
3

Step 3:- Add the new node as last node:

$t \rightarrow \text{next} = \text{new1}$;

Now, the link list is:-



start

function :-

```
void insert_end()
```

```
{  
    new1 = (s*) malloc(sizeof(s));  
    printf("In Enter data");  
    scanf("%d", &new1->data);  
    new1->next = '10';
```

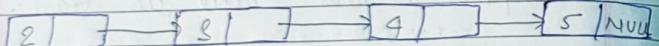
```
for(t=stant; t->next != '10'; t=t->next);  
    t->next = new1;
```

3

3) Insert Node at specified position (sp) :-

⇒ Algo :-

consider we have an existing
link list :-



Step 1 :- Create a New node :-

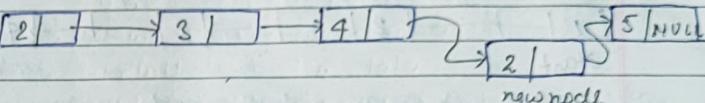
```
new1 = (s*) malloc(sizeof(s));  
printf("Enter data");  
scanf("%d", &new1->data);  
new1->next = '10';
```

Step 2 :- printf("In enter node data after which
U want to add new node");
scanf("%d", &k);

Step 3 :- Insert new node at specified position:

```
for(t1 = stant; t2 = t1->next; t1->data1 = k;  
    t1 = t1->next, t2 = t2->next);  
    t->next = new1;  
    new1->next = t2;
```

⇒ So if k=4 then link list :-



⇒ function :-

```
void insert_sp()
```

```
{  
    int k;  
    s *t1, *t2;
```

```
new1 = (s*) malloc(sizeof(s));  
printf("In enter data");  
scanf("%d", &new1->data);  
new1->next = '10';
```

printf("In Enter node data after which
you want to add new node");
scanf("%d", &k);

```
for(t1 = stant, t2 = t1->next; t1->data1 = k;  
    t1 = t1->next, t2 = t2->next);  
    t1->next = new1; t2->next = new1->next;  
    new1->next = t2;
```

3

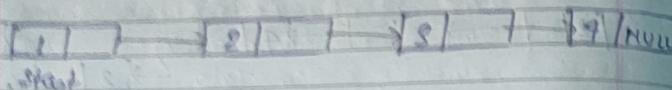
Delete Node

>Delete a node from an existing link list

a) Delete node from start (delete start node)

algo:-

consider we have an existing link list
as :-



step 1 :- store the address of start node

in a temp variable (t)

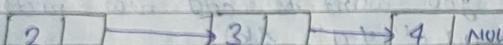
$t = \text{start};$

step 2 :- Move the start to the 2nd node

$\text{start} = \text{start} \rightarrow \text{next};$

step 3 :- Remove the start node: from
 $\text{free}(t);$

Now the link list is as follows :-



→ functions :-

`void delete_start()`

`t = start;`

$\text{start} = \text{start} \rightarrow \text{next};$

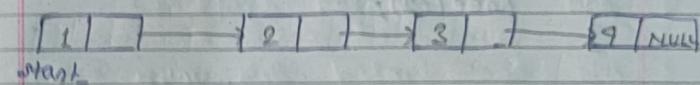
$\text{free}(t);$

3

b) delete end node :-

algo:-

consider we have an existing link list as :-



step 1 :- Make two pointers so that when the loop is terminated

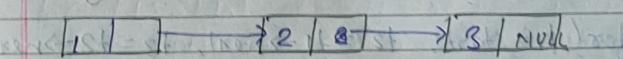
1st pointer at 2nd last node and
end pointer at last node :-

$\text{for } t_1 = \text{start}, t_2 = t_1 \rightarrow \text{next}; t_2 \rightarrow \text{next} != \text{NULL}$
 $t_1 = t_1 \rightarrow \text{next}, t_2 = t_2 \rightarrow \text{next};$

step 2 :- Set the t_1 next to null
 $t_1 \rightarrow \text{next} = \text{NULL};$

step 3 :- delete the last node;

Now the link list is as :-



`start = start + 1; p = p - 1;`

`(current) = start; free(start);`

function :-
void delete_end()

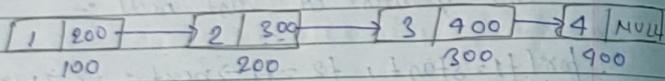
for (
 t1 = start, t2 = t1->next; t2->next != '10';
 t1 = t1->next, t2 = t2->next);

 t1->next = '10';
 free(t2);

3

c) Delete the specified node :-

→ Algo :-
consider we have an existing link
list as -



Step 1 :- int key;
printf("Enter the node data u want to
delete :");
scanf("%d", &k);

Step 2 :- Make three pointers so that when
the loop is terminated, t1 will at just
before the key node, t2 at key node
and t3 at just after the key node.

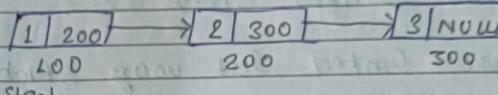
for (t1 = start, t2 = t1->next, t3 = t2->next;
 t2->data != key; t1 = t1->next,
 t2 = t2->next, t3 = t3->next);

Step 3 :- Assign the address of t2 to t1 ;

t1->next = t2;

Step 4 :- delete the key node;
free(t2)

Step Now the link list (if key = 3)



start.

→ function :-

void delete_sp()

{
 s * t1, * t2, * t3;
 int key;

 printf("In Enter node data u want to
 delete ");

 scanf("%d", &key);

 for (t1 = start, t2 = t1->next, t3 = t2->next;
 t2->data != key, t1 = t1->next, t2 = t2->next,
 t3 = t3->next);

 t1->next = t3;

 free(t2);

3

1

- 1) Find the middle element of a singly linked list in one pass?
- 2) Delete the duplicate data nodes in a linked lists.
- 3) Reverse the linked list?
- 4) Add two linked lists?
- 5) Add two linked list using stacks?
- 6) print alternate node data?
- 7) print even & odd node data?
- 8) Merge two sorted linked list?
- 9) print nth node data entered by user?

2nd method

```

function delete from pos()
{
    struct node *nextnode, *head, *temp;
    int pos, i=1;
    temp = head;
    if (pos < 1 || pos > i)
        point("enter position");
    scanf("%d", &pos);
    while (i < pos - 1)
        {
            temp = temp ->next;
            i++;
        }
    temp = temp ->next;
}

```

nextnode = temp ->next;
 temp ->next = nextnode ->next;
 free(nextnode);

3

⇒ The following are the fields in the linked list:-

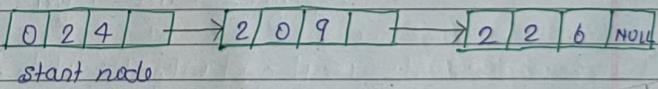
Row :- It is an index of row where a non-zero element is located.

column :- It is an index of column where a non-zero element is located.

value :- It is the value of the non zero element which is located at the index (row, column).

Next node :- It stores the address of the next node.

0	1	2
0	0	4
1	0	0
2	9	0
		6



start node

1. What is the relationship between the number of plants and the amount of rainfall?
Ans. There is a positive correlation between the number of plants and the amount of rainfall.
2. What is the relationship between the number of plants and the amount of sunlight?
Ans. There is a positive correlation between the number of plants and the amount of sunlight.
3. What is the relationship between the number of plants and the amount of water?
Ans. There is a positive correlation between the number of plants and the amount of water.
4. What is the relationship between the number of plants and the amount of fertilizer?
Ans. There is a positive correlation between the number of plants and the amount of fertilizer.

1. What is the relationship between the number of plants and the amount of rainfall?
Ans. There is a positive correlation between the number of plants and the amount of rainfall.
2. What is the relationship between the number of plants and the amount of sunlight?
Ans. There is a positive correlation between the number of plants and the amount of sunlight.
3. What is the relationship between the number of plants and the amount of water?
Ans. There is a positive correlation between the number of plants and the amount of water.
4. What is the relationship between the number of plants and the amount of fertilizer?
Ans. There is a positive correlation between the number of plants and the amount of fertilizer.

Circular Singly List

Circular Singly List is a variation of Singly List in which the last element points to the first element.



Q) Create and display circular singly list?

Struct node

```

struct node {
    int data;
    struct node *next;
};

typedef struct node S;
S *start, *t, *new1;
  
```

```

void insert();
void display();
  
```

main()

```

int ch;
while(1)
{
    printf("\n Insert: 1 \n Display: 2 \n");
    scanf("%d", &ch);
}
  
```

Switch (ch)

case 1:

insert();

bbreak;

case 2:

display();

bbreak;

3. (else)

8

(else)

void insert()

```
{
    if (start == '10')
    {
        start = (S*)malloc(sizeof(S));
        printf("Enter data");
        scanf("%d", &start->data);
        start->next = start;
        t = start;
    }
}
```

```

    start = (S*)malloc(sizeof(S));
    printf("Enter data");
    scanf("%d", &start->data);
    start->next = start;
    t = start;
}
  
```

3

else

8

```

    new1 = (S*)malloc(sizeof(S));
    printf("Enter data");
    scanf("%d", &new1->data);
    t->next = start;
    new1->next = start;
    t = new1;
}
  
```

3

else

8

send droopy ()

```

5
private ("In circular list first : last");
for (t = start; t->next != start; t = t->next)
{
    cout << "t->data : " << t->data;
}
cout << "t->data : " << t->data;
cout << "t->next : " << t->next->data;

```

3

$\text{LHS} = \text{RHS}$

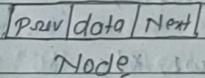
17. $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$

Doubly linked list

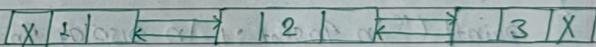
Doubly linked list is a complex type of linked list in which a node contains a pointer to the previous as well as the next node in the sequence. Therefore, in a doubly linked list, a node consists of three parts:

- 1) node data
- 2) pointer to the next node (forward pointer)
- 3) pointer to the previous node (backward " ")

- A sample node in a doubly linked list is shown in the figure:-



- A doubly linked list containing three nodes having numbers from 1 to 3 in their data part is shown:-



doubly linked list.

⇒ Node of a doubly linked list:-
struct Node {

int data;

struct Node * fp;

struct Node * bp;

};

Q) W.R.P in C to implement (create & display) the doubly linked list?

Struct Node

```
int data;  
struct Node *fp, *bp;
```

};

```
typedef struct Node S;
```

```
void insert();  
void display();  
void display_rev();
```

S* start, *new1, *t;

main()

```
{  
    int ch;  
    while (1)  
    {
```

```
        printf ("In Insert: 1 In display 2  
        Reverse Order: 2 In Display : 3 \n");
```

```
        scanf ("%d", &ch);
```

```
        switch (ch)
```

```
{
```

```
    case 1:
```

```
        insert();  
        break;
```

case 2:
display_rev();
break;

case 3:
display();
break;

3

```
void insert()  
{
```

```
if (start == '\0')
```

```
{  
    start = (S*) malloc (sizeof (S));
```

```
    printf ("In Enter data");  
    scanf ("%d", &start->data);
```

```
    start->fp = '\0';
```

```
    start->bp = '\0';
```

```
t = start;
```

3

```
else
```

```
{  
    new1 = (S*) malloc (sizeof (S));
```

```
    printf ("In Enter data");  
    scanf ("%d", &new1->data);
```

```
    new1->fp = '\0';
```

```
    new1->bp = '\0';
```

```
t->fp = new1;
```

```
new1->bp = t;
```

```
t = new1;
```

3

```

void displayRev()
{
    printf("In Reverse order: In");
    for( ; t->bp!=NULL; t=t->bp),
    {
        printf("%d", t->data);
        printf("%d", t->data);
    }
}

```

```

void display()
{
    printf("In Elements : In");
    for( t=start; t->fp!=NULL; t=t->fp)
    {
        printf("%d", t->data);
        printf("%d", t->data);
    }
}

```

B) Add two more opgns eg: using linked list

Stack Implementation

→ WAP in C to perform all the operation of stack using linked list

- a) push
- b) pop
- c) peep (Traversal)

struct Node

{ int data;

struct Node *next;

};

typedef struct Node S;

S *start, *top, *new, *t1, *t2;

void push();

void pop();

void peep();

main()

```

{
    int ch;
    while(1)
    {
        printf("1)push : 2)pop : 3)peep : 4)exit : ");
        scanf("%d", &ch);
        switch(ch)
        {
            case 1:
                push();
                break;
            case 2:
                pop();
                break;
            case 3:
                peep();
                break;
            case 4:
                exit(0);
        }
    }
}
```

printf("In push : 1 In pop : 2 In peep : 3 In

scanf("%d", &ch);

switch(ch)

{

case 1:

push();

break;

case 2:

pop();

break;

Queue

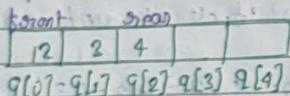
It is linear data structure that works on FIFO manner, where FIFO means "First In First Out".

Implementation:

- 1) Array Imp (static queue)
- 2) Link List Imp (dynamic queue)

⇒ Types of Queue:-

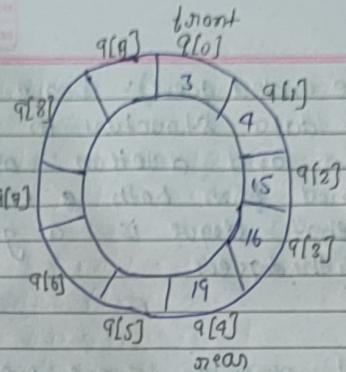
1) Straight Queue (Linear Queue):



⇒ In linear queue insertion always happens from rear end and deletion from front.

2) Circular Queue: In circular queue all the nodes are represented as circular. It is similar to the linear, except that the last element of the queue is as ring buffer as all the ends are connected to another ends.

⇒ The circular queue can be represented as:-



3) Priority Queue: A priority queue is another special type of queue data structure in which each element has some priority associated with it. Based on the priority of the element, the elements are arranged in a priority queue. If the elements occur with the same priority, then they are served according to the FIFO principle.

⇒ linked list data structure of priority queue:-

struct node {

int data, pno; } linked list Representation
struct node *next;

};

⇒ Array data structure:-

struct C-queue

{ int data;
int pno;

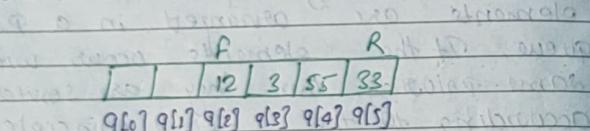
3 c q[10];

Q) Deque (Double ended queue):- Deque is a linear data structure in which the insertion and deletion operation are performed from both ends. we can say that deque is a generalizing version of the queue.

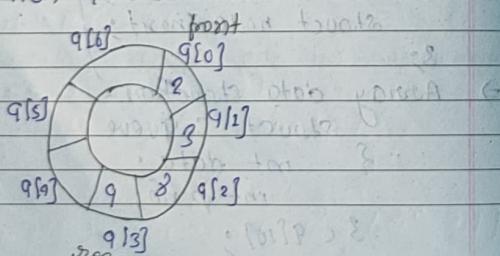
v.IMP

Q) Advantage of circular queue over the linear queue?

Ans) consider a case in linear queue (Array implemented) where, there are some vacant space available from the front end but full space at the end i.e. rear = max-1.



Since rear is on max-1 so we can not insert any new elements, that creates wastage of memory area. To solve this problem we use the circular queue.



Q) Create a linear queue using array and perform:-

a) insert element from rear (Algorithm) (College)

b) delete from front (Algo) college

a) #define max 10

int n = -1;

int f = -1; int q[max];

void insert(int);

void delete();

void display();

main()

f

int ch, data;

while(1)

{

printf("1 In Insert: 2 In Delete: 3 In Display:
3\n"),

scanf("%d", &ch);

switch(ch)

{

case 1:

printf("In Enter data");

scanf("%d", &data);

insert(data);

break;

case 2:
 delete();

 break;

case 3:
 display();
 break;

3

3

void insert(int x)

{

 if ($r = max - 1$)
 printf("In Queue is full");

 else if ($r == -1 \& f == -1$)

{

$r = 0$;

$f = 0$;

$q[r] = x$;

3

 else

$r++$;

$q[r] = x$;

3

void delete()

{

 if ($r == -1 \& f == -1$)

 printf("In Queue is empty");

 else if ($r == 0 \& f == 0$)

 printf("In Deleted Data : %d", q[f]);

$f = -1$;

$r = -1$;

3

else

 printf("In Deleted Data : %d", q[f]);

$f = f + 1$;

3

void display()

{

 int i;

 printf("In Queue elements are: In");

 for (i = f; i <= r; i++)

 printf("%d", q[i]);

3

Algo

Q) write in C++ to implement queue using linked list?

Using namespace std;
`#include<iostream>`

struct node

{

int data;

struct node *next;

};

`typedef struct node S;`

`S *f, *n, *newl, *l;`

`void insert(int);`

`void delete();`

`void display();`

`main()`

{

`int ch, d;`

`while(1)`

{

`cout << "In Insert : 1 In delete : 2 In`

`display : 3 In 4 : 4`

`cin >> ch;`

`Switch(ch)`

{

`case 1 :`

`(cout << "In Enter data");`

`cin >> d;`

new syntax

`ptr = new type;`

or:

`*s = new S;`

delete syntax

`delete ptr;`

one - delete t;

insert(d);
 break;
 case 2 :
 deleteL();
 break;
 case 3 :
 display();
 break;

3

void insert(int x)
 {
 if (s == NULL && f == NULL)
 {
 f = new S;
 f->data = x;
 f->next = NULL;
 s = f;

3

else {
 new1 = new S;
 new1->data = x;
 new1->next = NULL;
 s->next = new1;
 s = new1;

3

void deleteL()

3

if (s == NULL && f == NULL)
 cout << "In Queue is empty";

else {
 t1 = f;
 f = f->next;
 delete t1;

3

void display()

3

cout << "In Queue elements";

for (t1 = f; t1->next != NULL; t1 = t1->next)

cout << t1->data << " ";

cout << t1->data;

3

Q) write in C to implement queue using
link list 2

circular

Using namespace std;

#include <iostream>

struct node

{

int data;

struct node * next;

};

typedef struct node;

s * s, * s1, * s2;

void insert(int);

void display();

void deleteL();

#define max 10;
 int q[max];
 int r = -1;
 int f = -1;
 void delete();
 void insert();
 void display();

 main()
 {
 int ch;
 while(1)
 {
 printf("In Insert 1 In Delete 2 In
 display : 3\n");
 scanf("%d", &ch);

 switch(ch){
 case 1:
 insert();
 break;
 case 2:
 delete();
 break;
 case 3:
 display();
 break;
 }
 }
 }

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void Insert()
 {
 int d;
 if (r == max - 1)
 printf("In Queue is full");

 else if (r == -1 && f == -1)
 {
 printf("Enter data");
 scanf("%d", &d);
 r = f = 0;
 q[r] = d;
 }
 else {
 printf("Enter data");
 scanf("%d", &d);
 r = r + 1;
 q[r] = d;
 }
 }

void delete()
 {
 int i;
 if (r == -1 && f == -1)
 printf("In Queue is empty so can
 not delete data");
 else {
 printf("In Deleted data : %d", q[f]);
 for (i = f; i <= r; i++)
 {
 q[i] = q[i + 1];
 }
 }
 }

$s_2 = s_1 - 1;$

3

3

void display()

{

int i;

printf("In Queue elements are: %s",

for(i=1; i<=n; i++)

{

printf("%d\t", q[i]);

}

3

** Infix to postfix Using stack

Operator precedence

1. ()

2. ^

3. / *

4. + -

Associativity

1. ()

Right \rightarrow left } pop outleft \rightarrow Right } popleft \rightarrow Right } out

Rules for conversion:

1. If the lower priority operator enters in the stack then pop out the higher priority operator from the stack.
2. If two equal priority operators are in stack then check the associativity, if the Assoc. is left to Right then pop out otherwise stay in the stack.
3. If the closing parenthesis come then pop out all the operators between parenthesis.

Q.) Infix to postfix conversion:-

 $K+L-M*N+(O^P)* W/U/V*T+Q$

Infix exp'	stack	postfix exp'
K		K
+	+	K
L	+	KL
-	-	KL+

M	-	$KL + MN$
*	-*	$KL + MN$
N	-*	$KL + MN$
+	+	$KL + MN * -$
(+()	$KL + MN * -$
O	+()	$KL + MN * - O$
^	+(^)	$KL + MN * - O ^$
P	+(^)	$KL + MN * - O P$
)	+^	$KL + MN * - O P ^$
*	**	$KL + MN * - O P N$
W	**	$KL + MN * - O P N W$
I	+	$KL + MN * - O P ^ W * X$
U	+	$KL + MN * - O P ^ W * U$
V	+	$KL + MN * - O P ^ W * U / V$
*	++	$KL + MN * - O P ^ W * U / V / V$
T	++	$KL + MN * - O P ^ W * U / V / T$
+	+	$KL + MN * - O P ^ W * U / V / T * +$
B	+	$KL + MN * - O P ^ W * U / V / T * + Q$

$$= KL + MN * - O P ^ W * U / V / T * + Q +$$

Ans

Rule 1:- In the conversion of Infix to postfix
the lower priority operator can be followed
by the higher priority operators in the
stack.

Rule 1.1:- In the stack of infix to postfix conversion
the higher precedence operators never be
followed by lower precedence operators.

$$8) a+b*(c \wedge d - e)^{(f+g*h)} - i$$

Infix Input	Stack	Postfix
a	-	a
+	+	a)
b	+	ab
*	**	ab
(+*(ab
c	+*(abc
^	+*(^	abc
d	+*(^	abcd
-	+*(-	abcdn
e	+*(-	abcdne
)	+*	abcdne-
^	+*^	abcdne-
(+*^(abcdne-
f	+*^(abcdne-f
+	+*^(+	abcdne-f
g	+*^(+	abcdne-fg
*	+*^(+*	abcdne-fg*
h	+*^(+*	abcdne-fgh
)	+*^*	abcdne-fgh*
-	-	abcdne-fgh*+^*+
i	-	abcdne-fgh*+^*+i

$$= abcd^ne-fgh*f^+*+i$$

Ans

Q) $a + (b * c (d \cdot e f) * g) * h$

Input	Stack	Postfix
a		a
+	+	a
(+()	o
b	+()	ab
*	+(*)	ab
c	+(*)	abc
(+(*)	abc
d	+(*)	abcd
/	+(*)()	abcd
e	+(*)()	abcde
^	+(*)(^)	abcde
f	+(*)(^)	abcdef
)	+(*)	abcdef^n/
*	+(*)	abcdef^n/*
g	+(*)	abcdef^n/*g
)	+	abcdef^n/*g*
*	+	abcdef^n/*g*
h	+	abcdef^n/*g*h

$$= abcdef^n/*g*h**+$$

Converting Infix to postfix

Step 1:- Reverse the Infix expression i.e $A+B*C$ will become $C*B+A$. Note while reversing each ' $($ ' will become ' $)$ ' and each ' $)$ ' become ' $($ '.

Step 2:- Obtain the nearly postfix expression of the modified expression i.e $C*B+A$.

Step 3:- Reverse the postfix expression, Hence in our example postfix will $+A*B*C$.

Q) Infix

$$A + B * C \quad \text{Postfix} = ?$$

⇒ Reversing $C * B + A$

⇒ finding postfix of the modified exp :-

Input	Stack	Postfix
*	*	
*	*	C
B	*	CB
+	+	CB*
A		CB*A
		CB*A+

⇒ Again reversing for postfix

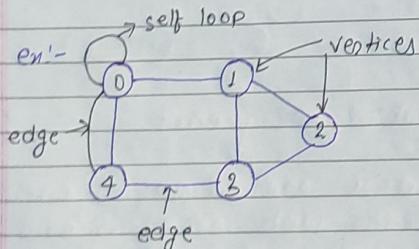
$$= +A*B*C$$

Graph

A graph is a collection of two sets V and E where V is finite non-empty set of vertices and E is a finite non-empty set of edges.

- Vertices are nothing but the nodes in the graph.
- Two adjacent vertices are joined by edges.
- Any graph is denoted as

$$G = \{V, E\}$$



Tree

A tree is a finite set of one or more nodes such that:

- 1) There is a specially designed node called root.
- 2) The children of the parent node (root) are known as subtrees.

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root node

Level 2

Level 1

Level 0

\therefore Height = 2 Leaf nodes : Having no any child Node.

Note:- If the number of nodes is n then no. of edges must be $n-1$ in the tree.

8) Diff between Graph & Tree

Graph

1. There is no unique node called root in graph.

Tree

1. There is a unique node called root in trees.

9) A cycle can formed. 2. There will not any cycle.

3. App: For finding shortest path in networking graph is used.

3. App: For game trees decision the tree is used.

9) Two major types directed and undirected graph.

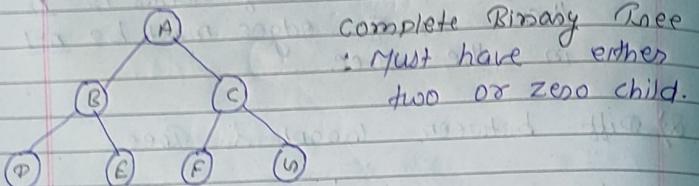
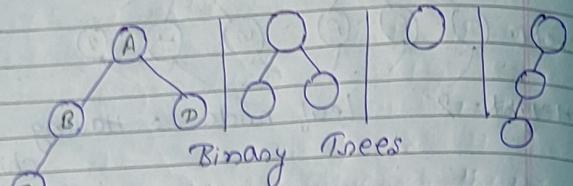
9) Two major type are binary tree and binary search tree.

5) More complex

5) less complex.

Binary Tree

where a parent node have atmost two child.



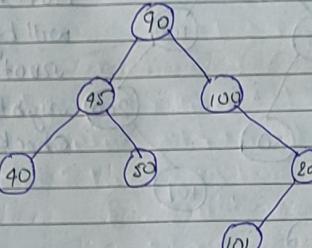
Binary search Tree (BST)

Binary search tree is a node-based binary tree data structure which has the following properties:-

- The left subtree of a node contains only nodes with keys less than the node's key.
- The right subtree of a node contains only nodes with keys greater than the node's key.
- The left and right subtrees each

must also be a binary search tree.

Note:- There must be no any duplicate nodes.



Binary search Tree

Inorder (LR'R) :- 40, 45, 50, 90, 100, 101, 200

↳ It's also refer as Tree root

preorder (R'LR) :- 90, 45, 40, 50, 100, 200, 101

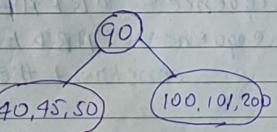
postorder (LRR') :- 40, 50, 45, 101, 200, 100, 90.

Q) construct the B.S.T by following Inorder & preorder:-

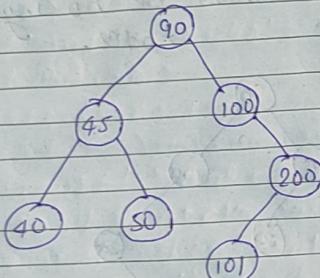
Inorder: 40, 45, 50, 90, 100, 101, 200

preorder: 90, 45, 40, 50, 100, 200, 101

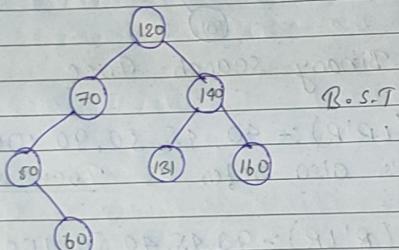
8 steps



Step 2: In Preorder 45 comes at first position in 90, 45 & 50, 100 comes closer.



Note:- if two no. will bigger than the root node for right side then check the preorders.



Inorder (LR'R): 50, 60, 70, 120, 131, 140, 160

Preorder (RLR'R): 120, 70, 50, 60, 140, 131, 160

Postorder (LRR'L): 60, 50, 70, 131, 160, 140, 120

Q.) Let us consider the below traversals:-

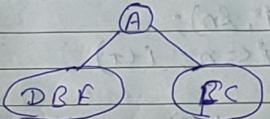
Inorder sequence - D R F A F C

Preorder sequence - A B D E C F

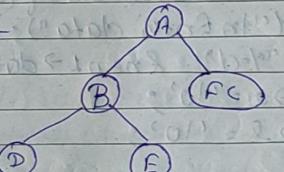
construct the R-S-T.

Soln) Here no any kind of numbering is given so we v preorders then Inorder to check sequence.

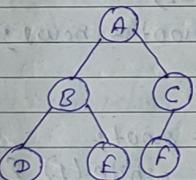
Step 1:-



Step 2:-



Step 3:-



Q) W.A.P in C to create and display BST?

struct node

{

int data;

struct node *r, *l;

};

typedef struct node s;

s *newl, *l, *root;

main()

{

```
    int i, n;      no. of  
    printf("Enter number:");  
    scanf("%d", &n);  
    for(i=1; i<=n; i++)
```

{

```
        new1 = (s*) malloc(sizeof(s));  
        printf("Enter data:");  
        scanf("%d", &new1->data);  
        new1->r = '10';  
        new1->l = '10';
```

if (i == l)

```
    root = new1;
```

else

{

```
t = root;
```

while(1) {

```
    if(new1->data > t->data)
```

{

```
        if(t->r == '10')
```

{

```
            t->r = new1;
```

```
            break;
```

3

else {

```
        if(t->l == '10')
```

{

```
            t->l = new1;
```

```
            break;
```

3

else (1st alternation binv)

{

```
t = t->l;
```

3

3

```
printf("In Inorder: \n");  
inorder(root);
```

```
printf("In Preorder: \n");  
preorder(root);
```

```
printf("In Postorder: \n");  
postorder(root);
```

3

void inorder(s *t)

{

```
if(t == '10')
```

```
    return;
```

inorder(t->l);

```
printf("%d ", t->data);
```

inorder(t->r);

3

void preorder(s *t)

{

```
if(t == '10')
```

```
    return;
```

```
printf("%d ", t->data);
```

inorder(t->l);

inorder(t->r);

3

void Postorder(s *t)

{
if ($t == \text{NULL}$)

return;

Inorder($t \rightarrow \text{left}$);

Inorder($t \rightarrow \text{right}$);

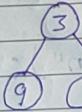
printf("%d %d", t->data);

}

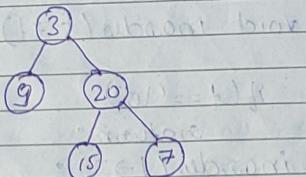
8) Inorder [9, 2, 15, 20, 7]

preorder [3, 9, 20, 15, 7]

step 1:



step 2:



This became a tree because in the left child node of root is greater than the root node.

Ques

Note:- If a binary tree is given and the Inorder of this tree is sorted then its must be Binary search tree. Otherwise given tree is not BST.

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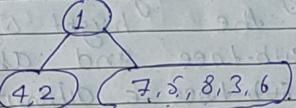
Ques (2) Given post order traversal

inorder: {4, 2, 1, 7, 5, 8, 3, 6}

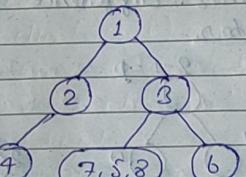
preorder: {1, 2, 4, 3, 5, 7, 8, 6}

construct Binary Tree

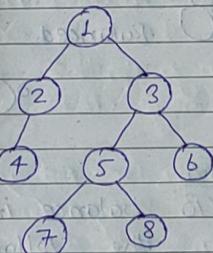
Step 1:



Step 2:

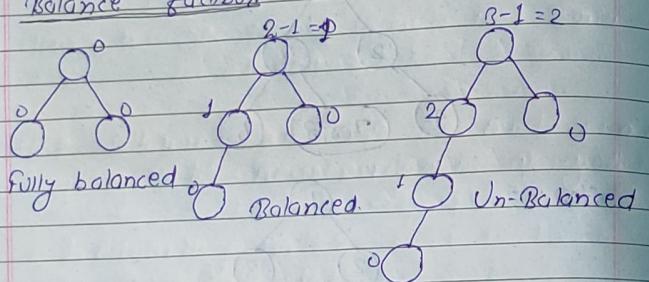


Step 3:



AVL Tree (Height Balance Tree)

Named after their inventor Adelson, Velski and Landis. AVL Trees are height balancing binary search tree. AVL tree checks the height of the left and right sub-tree and assures that the height sub-tree c difference is not more than 1. This difference is called the Balance factor.



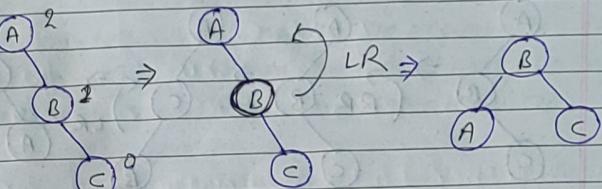
* AVL Rotation

To balance itself, an AVL tree may perform the following four kinds of rotations:-

- Left rotation
- Right rotation
- Left-right rotation
- Right-left rotation.

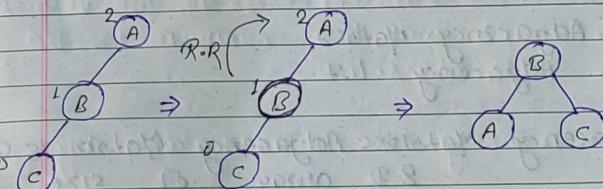
1) Left rotation: If a tree became unbalanced from the left hand side when a node is inserted into the left

subtree then left rotation will require



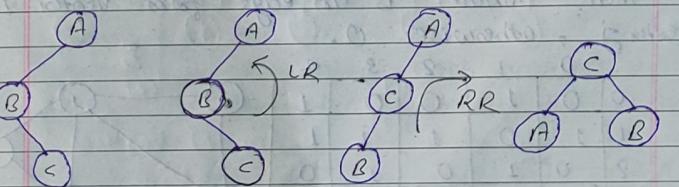
Right un-balanced left rotation Balanced Tree.

2) Right rotation: If a tree became unbalanced from the left hand side when a node is inserted into the left subtree, then right rotation will be required.



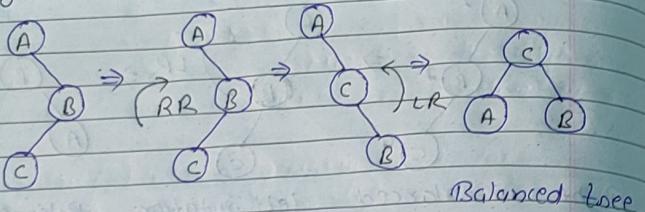
Left-unbalanced Right rotation Balanced tree.

3) Left-right rotation:



Balanced Tree

4) Right-left Rotation:-



Q) How to represent graph in Data structure?

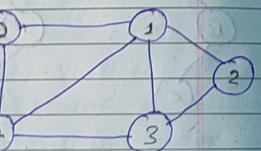
Ans The following two are the most common used Representations of graphs

1. Adjacency Matrix
2. Adjacency List

1) Adjacency Matrix: Adjacency Matrix is a 2D array of size

$V \times V$ where V is the number of vertices in a graph. Let the 2D array be $\text{adj}[i][j]$, a slot $\text{adj}[i][j] = 1$ indicates that there is an edge from vertex i to vertex j , otherwise 0.

	0	1	2	3	4
0	0	1	0	0	1
1	1	0	1	1	1
2	0	1	0	1	0
3	0	1	1	0	1
4	1	1	0	1	0



2) Adjacency list:-

An array of lists is used. The size of the array is equal to the number of vertices. The weights of edges can be represented as lists of pairs.

0	$\rightarrow [1] \rightarrow [4] \rightarrow [N]$
1	$\rightarrow [0] \rightarrow [4] \rightarrow [B] \rightarrow [2] \rightarrow [N]$
2	$\rightarrow [1] \rightarrow [3] \rightarrow [N]$
3	$\rightarrow [1] \rightarrow [2] \rightarrow [N]$
4	$\rightarrow [3] \rightarrow [0] \rightarrow [1] \rightarrow [N]$

1) Adjacency Matrix:-

it is a matrix $A[n][n]$ where n is no. of vertices &

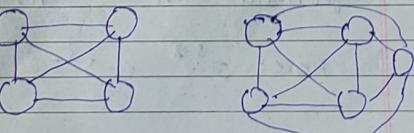
$$\begin{cases} a[i][j] = 1 & \text{if } i \text{ and } j \text{ are adjacent} \\ = 0 & \text{otherwise} \end{cases}$$

time complexity = $O(n^2)$

where n = no. of vertices.

• And Adjacency Matrix is used for dense graph.

dense graph:- when each vertex is connected with all the vertices like

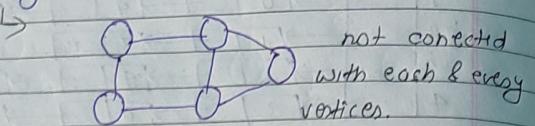


Time complexity of Adjacency list is

$$= O(n+e)$$

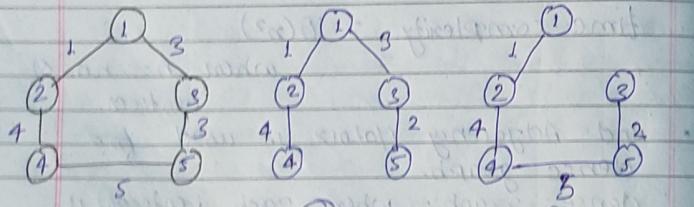
where e is the edge which we use twice in undirected graph.

- Adjacency list is generally used for sparse graph.



* **Spanning Tree**:- A spanning tree is a tree that connects all the vertices of a graph with the minimum possible no. of edges.

Note:- Spanning tree never contains any cycle.



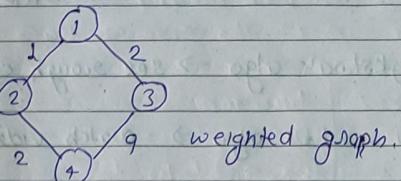
$$\text{formula} = n^{(n-2)} \quad n: \text{no. of vertices}$$

Here $5^{5-2} = 5^3 = 125$ spanning trees can be possible.

Note:- If a graph is a complete graph with n vertices then total number of spanning trees is $n^{(n-2)}$ where n is the number of nodes in the graph.

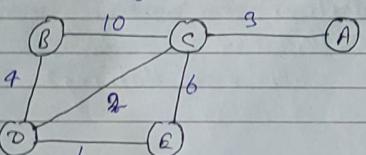
* **Minimum Spanning Trees**:- The minimum spanning trees is the tree whose sum of the edges is minimum.

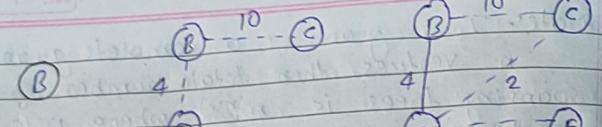
* **Weighted Graph**:- A weighted graph is a graph in which each branch is given a numerical weight.



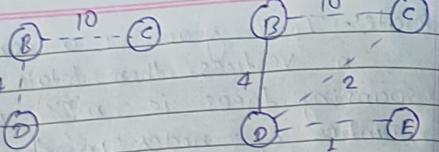
Prim's Algorithm

Prims algorithm starts with the single node and explore all the adjacent node with all the connecting edges at a every step. The edges with the minimal weights causing no cycle in the graph got selected.



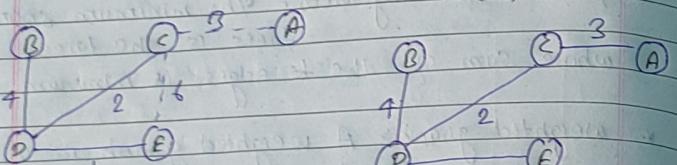


Step 1



Step 2

Step 3



Step 4

Step 5:

Dijkstra's algo → see rough copy/video

Floyd Warshall algo → watch video

HASHING

Hashing is a technique or process of mapping keys/values into the hash table by using a hash function. It is done for faster access to element. The efficiency of mapping depends on the efficiency of the hash function used.

Let a hash function $H(x)$ maps the value x at index $x \% 10$ in an array. For example if the list of values is $[11, 12, 13, 14, 15]$ it will be stored at position $[1, 2, 3, 4, 5]$ in the array or hash table respectively.

$$A = [11, 12, 13, 14, 15] \quad n=5$$

$$H(x) = x \% 10$$

$$\begin{aligned} 11 \% 10 &= 1 \\ 12 \% 10 &= 2 \\ 13 \% 10 &= 3 \\ 14 \% 10 &= 4 \\ 15 \% 10 &= 5 \end{aligned}$$

1	11
2	12
3	13
4	14
5	15

Types of Hashing

- open Hashing (closed addressing)
 - ↳ chaining

2) closed Hashing (open addressing)

↓ ↓ ↓

Linear Probing/searching Quadratic Probing double Hashing

$$\text{ex:- } A = 3, 2, 9, 6, 11, 13, 7, 12$$

$$h(k) = 2k + m$$

$$m = 10$$

where division method is $h(k_i) = k_i \% 10$
 where m is the size of Hash table.

key	location	0	1	2	3	4	5	6	7	8	9
3	$(2 \times 3 + 3) \% 10 = 9$				3	→ []	→ []	→ []	→ []	→ []	→ []
2	$(2 \times 2 + 3) \% 10 = 7$			1	9						
9	1			2							
6	5			3							
11	5			4							
13	9			5	6						
7	7			6							
12	7	2		7	2	→ []	→ []	→ []	→ []	→ []	→ []

Hash table (8 slots)

Tmp Questions (in box) you can see (4)

- what is Hashing?
- what is collision in Hashing?
- Types of Hashing.
- Chaining.

$$8) A = 3, 2, 9, 6, 11, 13, 7, 12$$

Use Division method and open addressing to store these values using linear probing

$$h(k) = 2k + 3, \quad m = 10$$

key	location	$k_i + m$	probes
3	$(2 \times 3 + 3) \% 10 = 9$	9	1
2	$((2 \times 2 + 3) \% 10 = 7$	7	1
9		1	1
6		5	1
11		5	2
13		9	2
7		7	2
12		7	6

Hash table

Array
0 3
1 9
2 12
3
4
5 6
6 11
7 2
8 7
9 3