#### **B.M.S. COLLEGE OF ENGINEERING**

Basavanagudi, Bengaluru- 560019

### DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING



## LAB REPORT

On

Analysis and Design of Algorithms (23CS4PCADA)

Submitted By:

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In partial fulfilment of

**BACHELOR OF ENGINEERING** 

In

COMPUTER SCIENCE AND ENGINEERING

2023-24

Faculty-In-Charge

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This is to certify that the Lab work entitled "Analysis and Design of Algorithms (23CS4PCADA)" conducted by **ANKIT SINGH BHATTI** (**1BM22CS353**) who is bonafide student at **B.M.S.College of Engineering**. It is in partial fulfilment for the award of **Bachelor of Engineering in Computer Science and Engineering** during the academic year 2023-24. The Lab report has been approved as it satisfies the academic requirements in respect of a Analysis and Design of Algorithms (23CS4PCADA) work prescribed for the said degree.

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## **INDEX**

Sl. No.	Date	Experiment Title	Page No.
1	03-05-2024	Topological ordering of vertices in a given digraph.	1-3
2	17-05-2024	Johnson Trotter algorithm to generate permutations	4-5
3	17-05-2024	Merge Sort technique	6-7
4	24-05-2024	Quick Sort technique	8-9
5	31-05-2024	Heap Sort technique	10
6	07-06-2024	Knapsack problem	11-12
7	14-06-2024	Floyd's algorithm	13-14
8	21-06-2024	Prim's algorithm Kruskal's algorithm	15-19
9	21-06-2024	Fractional Knapsack problem using Greedy technique	20-21
10	05-07-2024	Dijkstra's algorithm	22-23
11	12-07-2024	N-Queens Problem using Backtracking	24-25

## 1. Write program to obtain the Topological ordering of vertices in a given digraph.

```
//C program to implement topological sort using DFS
#include <stdio.h>
int n, a[10][10], res[10], s[10], top = 0;
void dfs(int, int, int[][10]);
void dfs_top(int, int[][10]);
int main()
  printf("Enter the no. of nodes");
  scanf("%d", &n);
  int i, j;
  for (i = 0; i < n; i++) {
     for (j = 0; j < n; j++) {
        scanf("%d", &a[i][j]);
     }
   }
  dfs_top(n, a);
  printf("Solution: ");
  for (i = n - 1; i >= 0; i--) {
     printf("%d ", res[i]);
  return 0;
}
void dfs_top(int n, int a[][10]) {
  int i;
  for (i = 0; i < n; i++) {
     s[i] = 0;
  for (i = 0; i < n; i++) {
     if (s[i] == 0) {
        dfs(i, n, a);
     }
}
void dfs(int j, int n, int a[][10]) {
  s[j] = 1;
```

```
int i;
  for (i = 0; i < n; i++) {
     if(a[j][i] == 1 \&\& s[i] == 0) {
       dfs(i, n, a);
     }
  }
  res[top++] = j;
}
OUTPUT:
Enter the no. of nodes6
001100
0\,0\,0\,1\,1\,0
000101
000001
000001
0\,0\,0\,0\,0\,0
Solution: 1 4 0 2 3 5
//C program to implement topological sort using source removal method
#include<stdio.h>
int a[10][10],n,t[10],indegree[10];
int stack[10],top=-1;
void computeIndegree(int,int [][10]);
void tps_SourceRemoval(int,int [][10]);
int main(){
  printf("Enter the no. of nodes: ");
  scanf("%d",&n);
  int i,j;
  for(i=0;i< n;i++){}
     for(j=0;j< n;j++){
       scanf("%d",&a[i][j]);
     }
  computeIndegree(n,a);
  tps_SourceRemoval(n,a);
  printf("Solution:");
  for(i=0;i< n;i++){
     printf("%d ",t[i]);
  return 0;
```

```
void computeIndegree(int n,int a[][10]){
  int i,j,sum=0;
  for(i=0;i< n;i++){
     sum=0;
     for(j=0;j< n;j++){
       sum=sum+a[j][i];
     }
    indegree[i]=sum;
  }
}
void tps_SourceRemoval(int n,int a[][10]){
  int i, j, v;
  for(i=0;i< n;i++){
     if(indegree[i]==0){
       stack[++top]=i;
     }
  }
  int k=0;
  while(top!=-1){
     v=stack[top--];
     t[k++]=v;
     for(i=0;i< n;i++){}
       if(a[v][i]!=0){
          indegree[i]=indegree[i]-1;
          if(indegree[i]==0){
            stack[++top]=i;
          }
       }
     }
  }
}
OUTPUT:
Enter the no. of nodes: 5
00100
10010
0\ 0\ 0\ 0\ 1
00101
0\ 0\ 0\ 0\ 0
Solution: 1 3 0 2 4
```

## 2. Implement Johnson Trotter algorithm to generate permutations.

```
#include <stdio.h>
#include <stdlib.h>
void swap(int* a, int* b) {
  int temp = *a;
  *a = *b;
  *b = temp;
}
void generatePermutations(int arr[], int start, int end) {
  if (start == end) {
     for (int i = 0; i \le end; i++) {
        printf("%d", arr[i]);
     }
     printf("\n");
   } else {
     for (int i = \text{start}; i \le \text{end}; i++) {
        swap(&arr[start], &arr[i]);
        generatePermutations(arr, start + 1, end);
        swap(&arr[start], &arr[i]); // backtrack
     }
   }
}
int main() {
  int n;
  printf("Enter the number of elements: ");
  scanf("%d", &n);
  int* arr = (int*)malloc(n * sizeof(int));
  printf("Enter the elements: ");
  for (int i = 0; i < n; i++) {
     scanf("%d", &arr[i]);
   }
  generatePermutations(arr, 0, n - 1);
  free(arr);
  return 0;
```

Enter the number of elements: 4

Enter the elements: 1 2 3 4

- 1234
- 1 2 4 3
- 1324
- 1342
- 1432
- 1423
- 2 1 3 4
- 2 1 4 3
- 2314
- 2341
- 2431
- 2413
- 3 2 1 4
- 3 2 4 1
- 5211
- $3\ 1\ 2\ 4$
- 3 1 4 2
- 3 4 1 2
- 3 4 2 1
- 4231
- 4213
- 4321
- 4312
- 4 1 3 2
- 4123

3. Sort a given set of N integer elements using Merge Sort technique and compute its time taken. Run the program for different values of N and record the time taken to sort.

```
//C program to implement merge sort
#include <stdio.h>
#include<time.h>
int a[20],n;
void simple_sort(int [],int,int,int);
void merge_sort(int[],int,int);
int main()
{
  int i;
  clock_t start, end;
  double time_taken;
  printf("Enter the no. of elements:");
  scanf("%d", &n);
  printf("Enter the array elements:");
  for (i = 0; i < n; i++)
     scanf("%d", &a[i]);
  }
  start = clock();
  merge\_sort(a, 0, n - 1);
  end = clock();
  time_taken = (double)(end - start) / CLOCKS_PER_SEC;
  printf("Sorted array:");
  for (i = 0; i < n; i++)
     printf("%d ", a[i]);
  printf("\n");
  printf("Time taken to sort: %f seconds\n", time_taken);
  return 0;
}
void merge_sort(int a[],int low, int high){
  if(low<high){</pre>
     int mid=(low+high)/2;
```

```
merge_sort(a,low,mid);
     merge_sort(a,mid+1,high);
     simple_sort(a,low,mid,high);
  }
}
void simple_sort(int a[],int low, int mid, int high){
  int i=low,j=mid+1,k=low;
  int c[n];
  while(i <= mid \&\& j <= high)\{
     if(a[i] \!\!<\!\! a[j]) \{
        c[k++]=a[i];
       i++;
     }else{
       c[k++]=a[j];
       j++;
     }
  }
  while(i<=mid){</pre>
     c[k++]=a[i];
     i++;
  }
  while(j<=high){</pre>
     c[k++]=a[j];
     j++;
  for(i=low;i<=high;i++)\{
     a[i]=c[i];
  }
}
```

Enter the no. of elements:10

Enter the array elements: 8 96 32 75 62 78 63 48 56 100

Sorted array:8 32 48 56 62 63 75 78 96 100

Time taken to sort: 0.000002 seconds

## 4. Sort a given set of N integer elements using Quick Sort technique and compute its time taken.

```
//C program to implement quick sort
#include <stdio.h>
#include<time.h>
int a[20],n;
int partition(int [],int, int);
void quick_sort(int [],int,int);
void swap(int*,int*);
int main()
{
  int i;
  clock_t start, end;
  double time_taken;
  printf("Enter the no. of elements:");
  scanf("%d", &n);
  printf("Enter the array elements:");
  for (i = 0; i < n; i++) {
     scanf("%d", &a[i]);
  }
  start = clock();
  quick_sort(a, 0, n - 1);
  end = clock();
  time_taken = (double)(end - start) / CLOCKS_PER_SEC;
  printf("Sorted array:");
  for (i = 0; i < n; i++)
     printf("%d ", a[i]);
  printf("\n");
  printf("Time taken to sort: %f seconds\n", time_taken);
  return 0;
}
void swap(int *a,int *b){
  int temp=*a;
  *a=*b;
```

```
*b=temp;
}
void quick_sort(int a[],int low,int high){
  if(low<high){</pre>
     int mid=partition(a,low,high);
     quick_sort(a,low,mid-1);
     quick_sort(a,mid+1,high);
  }
}
int partition(int a[],int low,int high){
  int pivot=a[low];
  int i=low;
  int j=high+1;
  while(i \le j)
     do{
       i=i+1;
     }while(a[i]<pivot && i<=high);</pre>
     do{
       j=j-1;
     }while(a[j]>pivot && j>=low);
     if(i < j){
       swap(&a[i],&a[j]);
     }
  }
  swap(&a[j],&a[low]);
  return j;
}
OUTPUT:
Enter the no. of elements:10
Enter the array elements:96 53 26 78 12 63 85 12 06 95
Sorted array:6 12 12 26 53 63 78 85 95 96
Time taken to sort: 0.000002 seconds
```

## 5. Sort a given set of N integer elements using Heap Sort technique and compute its time taken.

```
//C program to implement heapify
#include<stdio.h>
int a[10],n;
void heapify(int[],int);
int main(){
  printf("Enter the number of array elements:");
  scanf("%d",&n);
  int i;
  printf("Enter array elements:");
  for(i=0;i<n;i++){
     scanf("%d",&a[i]);
  }
  heapify(a,n);
  printf("Array elements:");
  for(i=0;i< n;i++)
     printf(" %d",a[i]);
  }
  return 0;
}
void heapify(int a[],int n){
  int k;
  for(k=1;k< n;k++){
     int key=a[k];
     int c=k;
     int p=(c-1)/2;
     while(c>0 \&\& key>a[p]){
       a[c]=a[p];
       c=p;
       p=(c-1)/2;
     }
     a[c]=key;
  }
}
```

#### **OUTPUT:**

Enter the number of array elements:7 Enter array elements:50 25 30 75 100 45 80 Array elements: 100 75 80 25 50 30 45

## 6. Implement 0/1 Knapsack problem using dynamic programming.

```
//C program to implement knapsack problem in dynamic programming
#include <stdio.h>
int n,m,w[10],p[10],v[10][10];
void knapsack(int,int,int[],int[]);
int max(int,int);
int main()
  int i,j;
  printf("Enter the no. of items:");
  scanf("%d",&n);
  printf("Enter the capacity of knapsack:");
  scanf("%d",&m);
  printf("Enter weights:");
  for(i=0;i< n;i++){
     scanf("%d",&w[i]);
  printf("Enter profits:");
  for(i=0;i< n;i++){}
     scanf("%d",&p[i]);
  knapsack(n,m,w,p);
  printf("Optimal Solution:\n");
  for(i=0;i< n;i++){
     for(j=0;j< n;j++)
       printf("\%d",v[i][j]);\\
     }
     printf("\n");
  return 0;
}
void knapsack(int n, int m, int w[],int p[]){
  int i,j;
  for(i=0;i< n;i++){}
     for(j=0;j< m;j++){
       if(i==0 || j==0){
          v[i][j]=0;
        else if(w[i]>j)
          v[i][j]=v[i-1][j];
        }else{
          v[i][j]=max(v[i-1][j],((v[i-1][j-w[i]])+p[i]));
```

```
}
  }
}
int max(int a,int b){
  if(a>b){
     return a;
  }else{
     return b;
  }
}
OUTPUT:
Enter the no. of items:4
Enter the capacity of knapsack:5
Enter weights: 2 1 3 2
Enter profits: 12 10 20 15
Optimal Solution:
0\ 0\ 0\ 0
0 10 10 10
0 10 10 20
0 10 15 25
```

## 7. Implement All Pair Shortest paths problem using Floyd's algorithm.

```
//C program to implement floyd's algorithm
#include <stdio.h>
int a[10][10],D[10][10],n;
void floyd(int [][10],int);
int min(int,int);
int main()
  printf("Enter the no. of vertices:");
  scanf("%d",&n);
  printf("Enter the cost adjacency matrix:\n");
  int i,j;
  for(i=0;i< n;i++){}
     for(j=0;j< n;j++){
        scanf("%d",&a[i][j]);
     }
  floyd(a,n);
  printf("Distance Matrix:\n");
  for(i=0;i< n;i++){}
     for(j=0;j< n;j++){
        printf("%d",D[i][j]);
     printf("\n");
  return 0;
}
void floyd(int a[][10],int n){
  int i,j,k;
  for(i=0;i< n;i++){}
     for(j=0;j< n;j++){}
        D[i][j]=a[i][j];
     }
   }
  for(k=0;k< n;k++){
     for(i=0;i< n;i++)
        for(j=0;j< n;j++){
          D[i][j]=min(D[i][j],(D[i][k]+D[k][j]));
           }
        }
     }
```

```
}
int min(int a,int b){
  if(a < b){
    return a;
  }else{
    return b;
  }
}
OUTPUT:
Enter the no. of vertices:4
Enter the cost adjacency matrix:
0 99 3 99
2 0 99 99
99601
7 99 99 0
Distance Matrix:
0934
2056
8601
7 16 10 0
```

# 8. A. Find Minimum Cost Spanning Tree of a given undirected graph using Prim's algorithm.

```
//C program to implement prim's algorithm
#include <stdio.h>
int cost[10][10], n, t[10][2], sum;
void prims(int cost[10][10], int n);
int main() {
  int i, j;
  printf("Enter the number of vertices: ");
  scanf("%d", &n);
  printf("Enter the cost adjacency matrix:\n");
  for (i = 0; i < n; i++) {
     for (j = 0; j < n; j++) {
        scanf("%d", &cost[i][j]);
     }
  }
  prims(cost, n);
  printf("Edges of the minimal spanning tree:\n");
  for (i = 0; i < n - 1; i++) {
     printf("(%d, %d) ", t[i][0], t[i][1]);
  }
  printf("\nSum of minimal spanning tree: %d\n", sum);
  return 0;
}
void prims(int cost[10][10], int n) {
  int i, j, u, v;
  int min, source;
  int p[10], d[10], s[10];
  min = 999;
  source = 0;
  // Initialize arrays
  for (i = 0; i < n; i++) {
```

```
d[i] = cost[source][i];
    s[i] = 0;
    p[i] = source;
  }
  s[source] = 1;
  sum = 0;
  int k = 0;
  // Find MST
  for (i = 0; i < n - 1; i++) {
    min = 999;
    u = -1;
    // Find the vertex with minimum distance to the MST
    for (j = 0; j < n; j++) {
       if (s[j] == 0 \&\& d[j] < min) {
          min = d[j];
          u = j;
       }
     }
    if (u != -1) {
       // Add edge to MST
       t[k][0] = u;
       t[k][1] = p[u];
       k++;
       sum += cost[u][p[u]];
       s[u] = 1;
       // Update distances
       for (v = 0; v < n; v++) {
          if(s[v] == 0 \&\& cost[u][v] < d[v]) {
            d[v] = cost[u][v];
            p[v] = u;
          }
     }
  }
}
```

Enter the number of vertices: 4 Enter the cost adjacency matrix:

```
0 1 5 2
1 0 99 99
5 99 0 3
2 99 3 0
Edges of the minimal spanning tree:
(1, 0) (3, 0) (2, 3)
Sum of minimal spanning tree: 6
```

## B. Find Minimum Cost Spanning Tree of a given undirected graph using Kruskal's algorithm.

```
//C program to implement Kruskal's algorithm
#include <stdio.h>
int cost[10][10], n, t[10][2], sum;
void kruskal(int cost[10][10], int n);
int find(int parent[10], int i);
int main() {
  int i, j;
  printf("Enter the number of vertices: ");
  scanf("%d", &n);
  printf("Enter the cost adjacency matrix:\n");
  for (i = 0; i < n; i++) {
     for (j = 0; j < n; j++) {
       scanf("%d", &cost[i][j]);
     }
  }
  kruskal(cost, n);
  printf("Edges of the minimal spanning tree:\n");
  for (i = 0; i < n - 1; i++) {
     printf("(%d, %d) ", t[i][0], t[i][1]);
  printf("\nSum of minimal spanning tree: %d\n", sum);
  return 0;
}
void kruskal(int cost[10][10], int n) {
```

```
int min, u, v, count, k;
  int parent[10];
  k = 0;
  sum = 0;
  // Initialize parent array for Union-Find
  for (int i = 0; i < n; i++) {
     parent[i] = i;
  }
  count = 0;
  while (count < n - 1) {
     min = 999;
     u = -1;
     v = -1;
     // Find the minimum edge
     for (int i = 0; i < n; i++) {
       for (int j = 0; j < n; j++) {
          if (find(parent, i) != find(parent, j) && cost[i][j] < min) {
             min = cost[i][j];
             u = i;
             v = j;
          }
       }
     }
     // Perform Union operation
     int root_u = find(parent, u);
     int root_v = find(parent, v);
     if (root_u != root_v) {
       parent[root_u] = root_v;
       t[k][0] = u;
        t[k][1] = v;
        sum += min;
       k++;
       count++;
     }
int find(int parent[10], int i) {
```

}

```
while (parent[i] != i) {
    i = parent[i];
}
return i;
}
```

Enter the number of vertices: 4

Enter the cost adjacency matrix:

0152

1 0 99 99

5 99 0 3

2 99 3 0

Edges of the minimal spanning tree:

(1, 0) (3, 0) (2, 3)

Sum of minimal spanning tree: 6

## 9. Implement fractional Knapsack problem using Greedy technique.

```
#include <stdio.h>
void knapsack(int n, int p[], int w[], int W) {
  int used[n];
  for (int i = 0; i < n; ++i)
     used[i] = 0;
  int cur_w = W;
  float tot_v = 0.0;
  int i, maxi;
  while (cur_w > 0) {
     maxi = -1;
     for (i = 0; i < n; ++i)
       if ((used[i] == 0) \&\&
          ((\max i == -1) \parallel ((float)w[i]/p[i] > (float)w[\max i]/p[\max i])))
          maxi = i;
     used[maxi] = 1;
     if(w[maxi] \le cur_w) \{
       cur_w -= w[maxi];
       tot_v += p[maxi];
       printf("Added object %d (%d, %d) completely in the bag. Space left: %d.\n", maxi + 1,
w[maxi], p[maxi], cur_w);
     } else {
       int taken = cur_w;
       cur_w = 0;
       tot_v += (float)taken/p[maxi] * p[maxi];
       printf("Added %d%% (%d, %d) of object %d in the bag.\n", (int)((float)taken/w[maxi] *
100), w[maxi], p[maxi], maxi + 1;
     }
  }
  printf("Filled the bag with objects worth %.2f.\n", tot_v);
}
int main() {
  int n, W;
  printf("Enter the number of objects: ");
  scanf("%d", &n);
  int p[n], w[n];
  printf("Enter the profits of the objects: ");
  for(int i = 0; i < n; i++){
     scanf("%d", &p[i]);
  printf("Enter the weights of the objects: ");
  for(int i = 0; i < n; i++){
```

```
scanf("%d", &w[i]);
}
printf("Enter the maximum weight of the bag: ");
scanf("%d", &W);
knapsack(n, p, w, W);
return 0;
}
```

Enter the number of objects: 7

Enter the profits of the objects: 5 10 15 7 8 9 4 Enter the weights of the objects: 1 3 5 4 1 3 2

Enter the maximum weight of the bag: 15

Added object 4 (4, 7) completely in the bag. Space left: 11.

Added object 7 (2, 4) completely in the bag. Space left: 9.

Added object 3 (5, 15) completely in the bag. Space left: 4.

Added object 6 (3, 9) completely in the bag. Space left: 1.

Added 33% (3, 10) of object 2 in the bag.

Filled the bag with objects worth 36.00.

## 10. From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm.

```
// C program to implement Dijkstra's algorithm
#include <stdio.h>
int cost[10][10], n, result[10][2], weight[10];
void dijkstras(int [][10], int );
int main()
  int i, j, s;
  printf("Enter the number of vertices: ");
  scanf("%d", &n);
  printf("Enter the cost adjacency matrix:\n");
  for (i = 0; i < n; i++) {
     for (j = 0; j < n; j++) {
        scanf("%d", &cost[i][j]);
     }
  }
  printf("Enter the source vertex: ");
  scanf("%d", &s);
  dijkstras(cost, s);
  printf("Path:\n");
  for (i = 1; i < n; i++) {
     printf("(%d, %d) with weight %d", result[i][0], result[i][1], weight[result[i][1]]);
  return 0;
}
void dijkstras(int cost[][10], int s){
  int d[10], p[10], visited[10];
  int i, j, min, u, v, k;
  for(i = 0; i < 10; i++){
     d[i] = 999;
     visited[i] = 0;
     p[i] = s;
   }
  d[s] = 0;
  visited[s] = 1;
  for(i = 0; i < n; i++){
```

```
min = 999;
     u = 0;
     for(j = 0; j < n; j++){
       if(visited[j] == 0){
          if(d[j] < min){
             min = d[j];
            u = j;
          }
        }
     }
     visited[u] = 1;
     for(v = 0; v < n; v++){
       if(visited[v] == 0 \&\& (d[u] + cost[u][v] < d[v])){
          d[v] = d[u] + cost[u][v];
          p[v] = u;
        }
     }
  }
  for(i = 0; i < n; i++){
     result[i][0] = p[i];
     result[i][1] = i;
     weight[i] = d[i];
  }
}
OUTPUT:
Enter the number of vertices: 4
Enter the cost adjacency matrix:
0\ 1\ 5\ 2
1 0 99 99
5 99 0 3
2 99 3 0
Enter the source vertex: 0
Path:
(0, 1) with weight 1 (0, 2) with weight 5 (0, 3) with weight 2
```

## 11. Implement "N-Queens Problem" using Backtracking.

```
#include <stdio.h>
#include <stdbool.h>
bool place(int[], int);
void printSolution(int[], int);
void nQueens(int);
int main()
{
  int n;
  printf("Enter the number of queens: ");
  scanf("%d",&n);
  nQueens(n);
  return 0;
}
void nQueens(int n){
  int x[10];
  int count=0;
  int k=1;
  while(k!=0){
     x[k]=x[k]+1;
     while(x[k] \le n &\& !place(x,k)){
       x[k]=x[k]+1;
     }
     if(x[k] \le n)
       if(k==n){
          printSolution(x, n);
          printf("Solution found\n");
          count++;
       }else{
          k++;
          x[k]=0;
        }
     }else{
       k---;
     }
  printf("Total solutions: %d\n", count);
}
bool place(int x[10], int k){
  int i;
  for(i=1;i< k;i++){
     if((x[i]==x[k])||(i-x[i]==k-x[k])||(i+x[i]==k+x[k]))
```

```
return false;
     }
  }
  return true;
}
void printSolution(int x[10], int n){
  int i;
  for(i=1;i<=n;i++){}
     printf("%d", x[i]);
  }
  printf("\n");
}
OUTPUT:
```

Enter the number of queens: 4

2413

Solution found

3 1 4 2

Solution found

Total solutions: 2